Mathematical Techniques to Improve the Utility of a Hazard Risk Matrix

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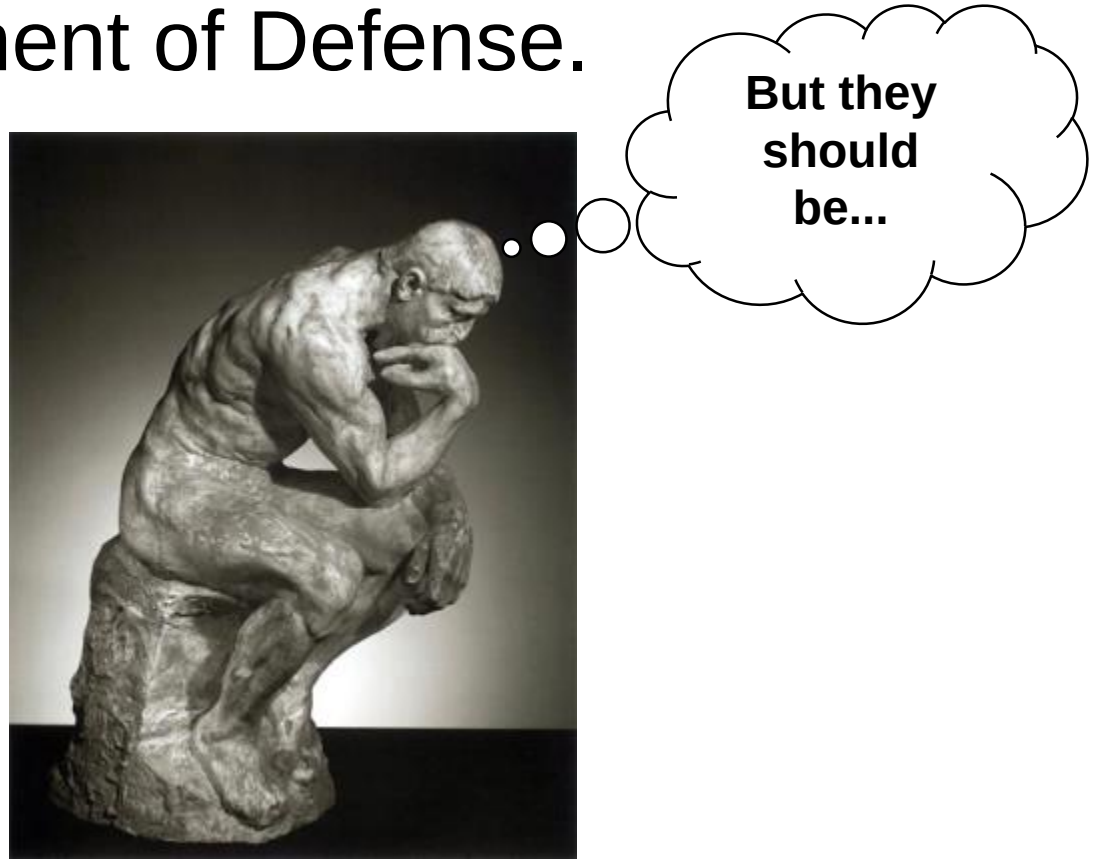
Caveat

Opinions expressed are those of the author and not the coordinated position of AMCOM, Army Materiel Command, the US Army or the Department of Defense.



Topics for this Tutorial

- Purpose of a Hazard Risk Matrix
- Understanding the Attributes of a well-designed risk assessment matrix
- How to Assign a Risk Assessment Code
- Understanding Probability
- Building an Expanded Matrix
- Plotting Accidents on a Matrix
- Using Relative Risk Values
- Building Hazard Risk Profiles

Source of the DOD Hazard Risk Matrix

Purpose of a Hazard Risk Matrix

- Determine who accepts the risk of a particular hazard

"…The Program Manager will use the methodology in MIL-STD-882E…Prior to exposing people, equipment, or the environment to known system-related ESOH hazards, the Program Manager will document that the associated risks have been accepted by the following acceptance authorities: the CAE for high risks, Program Executive Officer-level for serious risks, and the Program Manager for medium and low risks…" - Department of Defense Instruction 5000.02, January 7, 2015.

Purpose of a Hazard Risk Matrix

- Inform the risk acceptor of the nature of the risk.
- “It’s a 1D, Serious” does not really do that.

“The standard for risk management is leadership at the appropriate level of authority making **informed** decisions to control hazards or accept risks.”

Army Regulation 385-10

The Army Safety Program

29 February 2000

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- **Understanding the Attributes of a well-designed risk assessment matrix**
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Attributes of a well-designed risk assessment matrix

Severity		1	2	3	4	5	6	7	8
		≥$2k	≥$20k	≥$200k	≥$2M	≥$20M	≥$200M	≥$2B	≥$20B
Frequency		Injury, no lost work day	Lost Work Day	Permanent partial disability	≥1 Fatality	≥10 Fatalities	≥100 Fatalities	≥1,000 Fatalities	≥10,000 Fatalities
A	>100								
B	>10								
C	>1								
D	>0.1								
E	>0.01								
F	>0.001								
G	>0.0001								
H	>0.00001								
I	> 0.000001								
J	≤ 0.000001								

Prohibitive SECDEF

High - CAE

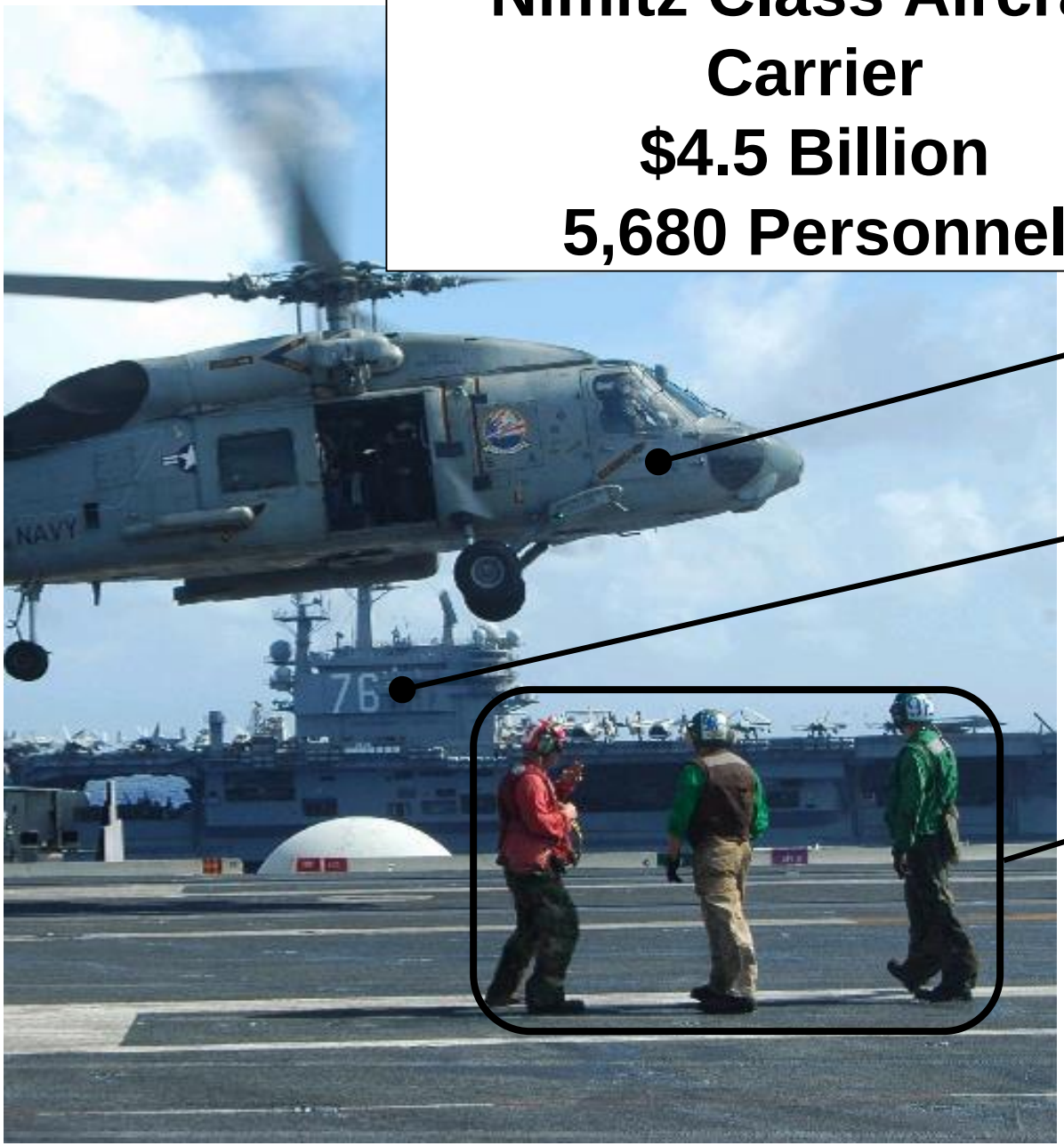
Serious - PEO

Medium - PM

Low – SSWG/Principal for Safety

Proposed DOD Matrix

Nimitz Class Aircraft Carrier
$4.5 Billion
5,680 Personnel



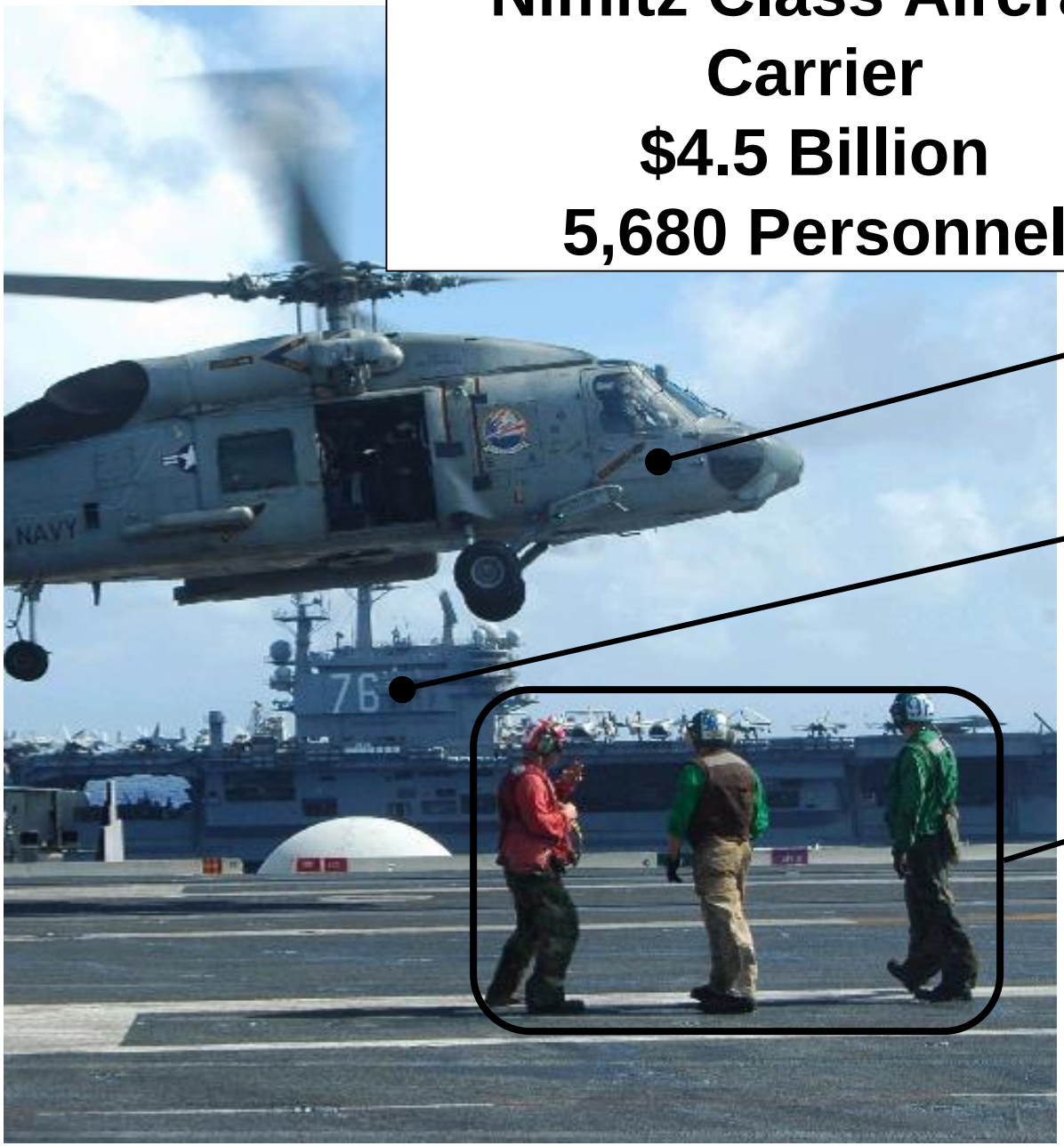
Today

Severity 1

Severity 1

Severity 1

Nimitz Class Aircraft Carrier
$4.5 Billion
5,680 Personnel



Severity 5

Severity 7

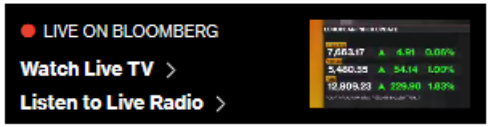
Severity 4

Politics

Navy Seeks $30 Million to Fix Gear That Hobbled Its New Carrier

By Anthony Capaccio
July 25, 2018, 10:04 AM CDT

- Congress asked to shift funds to repair Ford aircraft carrier
- Huntington Ingalls continues talks with General Electric



LISTEN TO ARTICLE

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The Navy is asking Congress to shift $30 million from other accounts to start repairing a damaged gear on the service's costliest warship, the Gerald R. Ford aircraft carrier.

The request for funds to repair the $13 billion carrier is part of a Pentagon package asking congressional approval to shift $4.7 billion in previously approved Army, Air Force and Navy funding into new programs or higher-priority projects. The package must be approved by all four congressional defense committees, where it's pending.

Attributes of a well-designed risk assessment matrix

2	Severity	1	2	3	4	5	6	7	8
		≥$2k	≥$20k	≥$200k	≥$2M	≥$20M	≥$200M	≥$2B	≥$20B
		Injury, no		Permanent					
	Frequency	**Probability calibrated with reference to an exposure interval (accidents per 1,000 troops per year, accidents per 100,000 FH, accidents per 1,000,000 missile firings, etc.)**							
A	>100								
B	>10								
C	>1								
D	>0.1								
E	>0.01								
F	>0.001								
G	>0.0001								
H	>0.00001								
I	> 0.000001								
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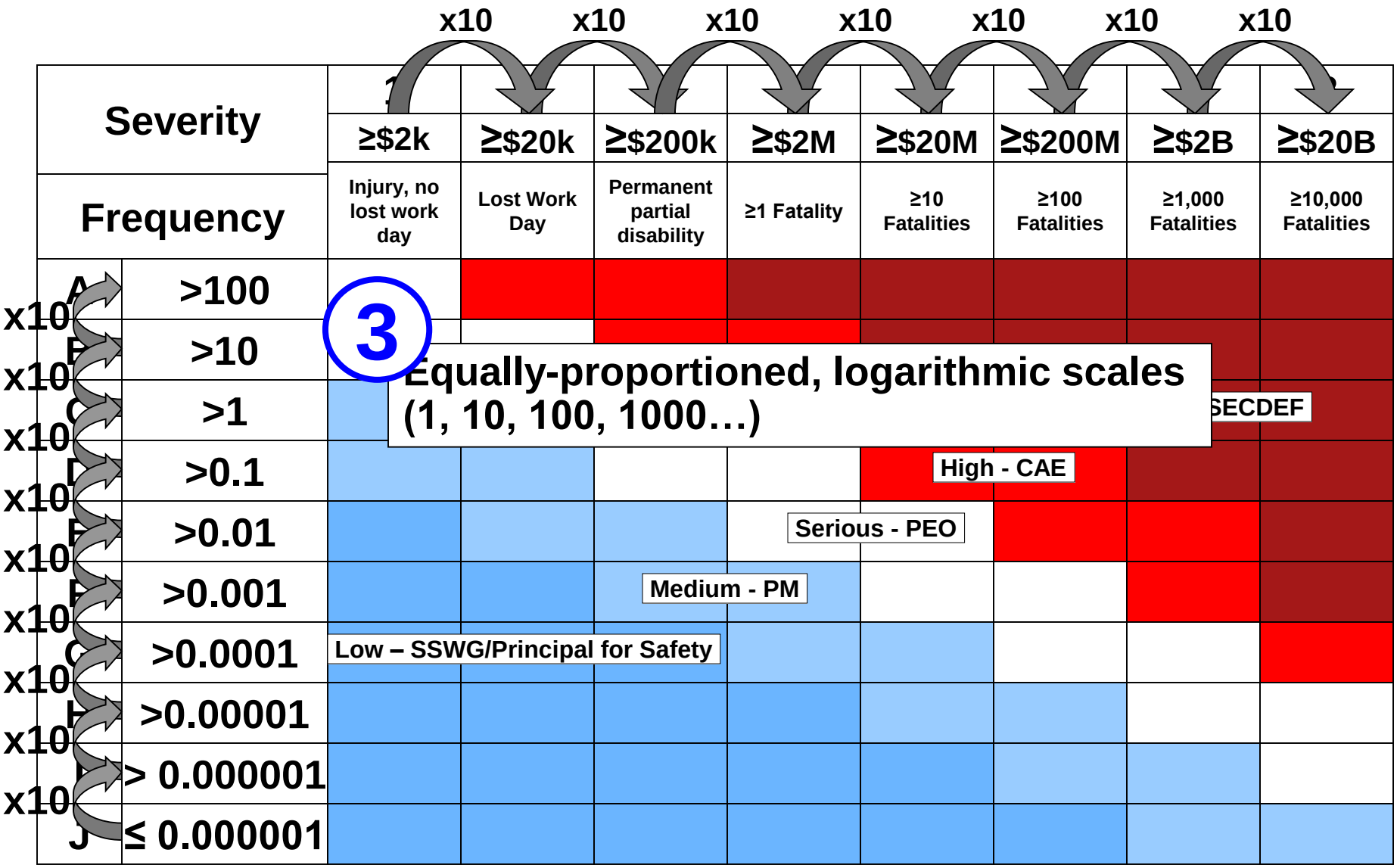
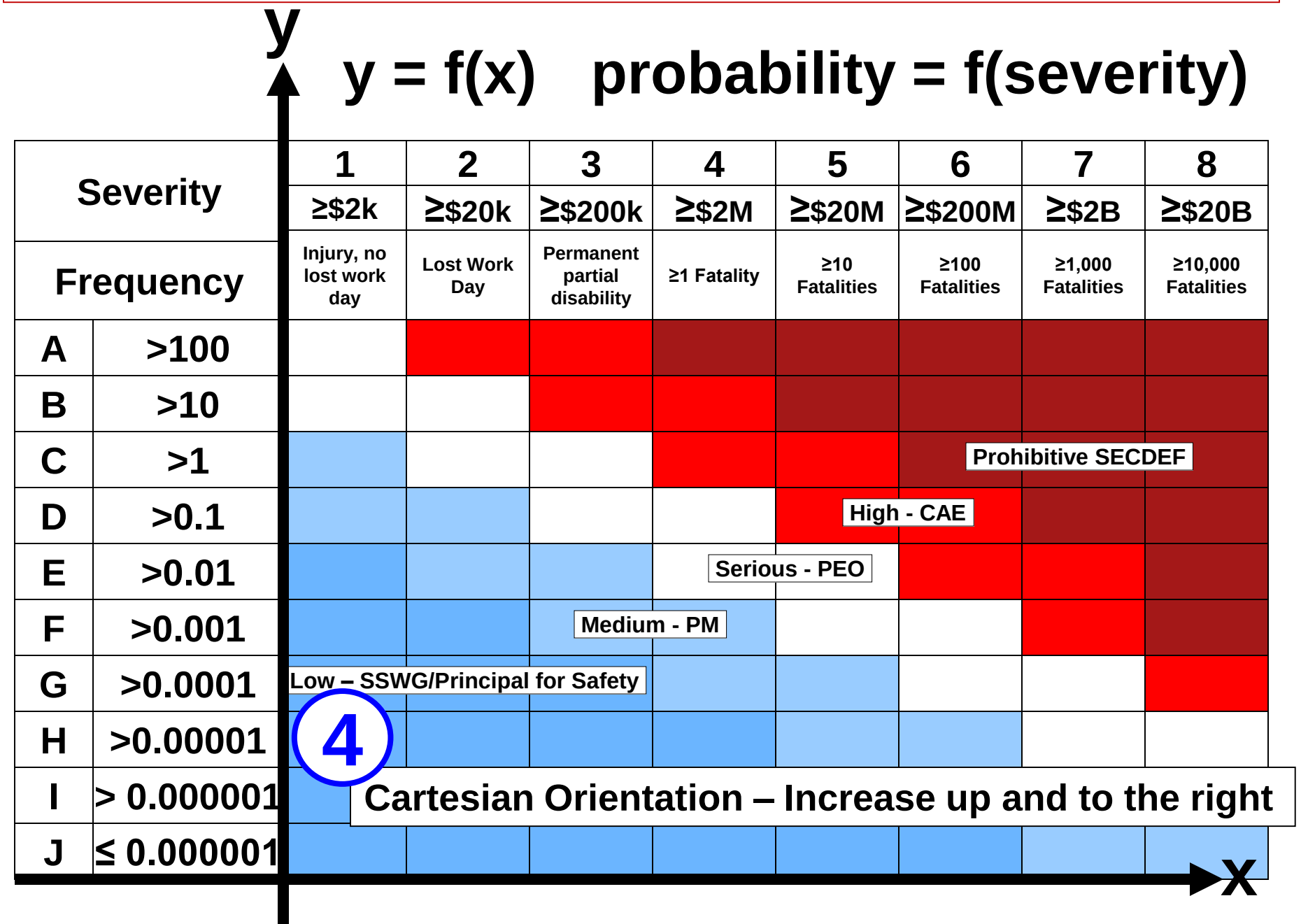
Attributes of a well-designed risk assessment matrix



Attributes of a well-designed risk assessment matrix



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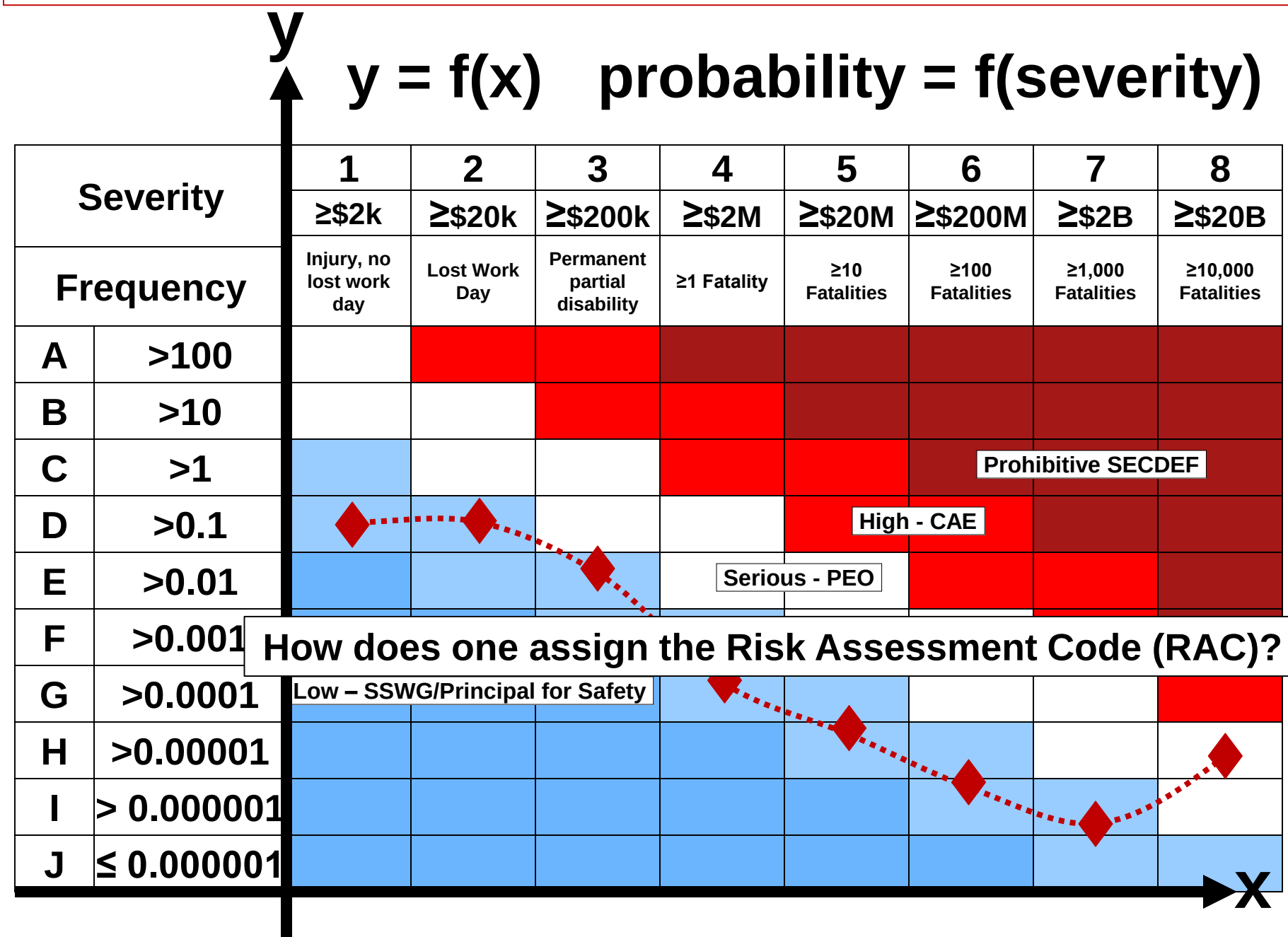
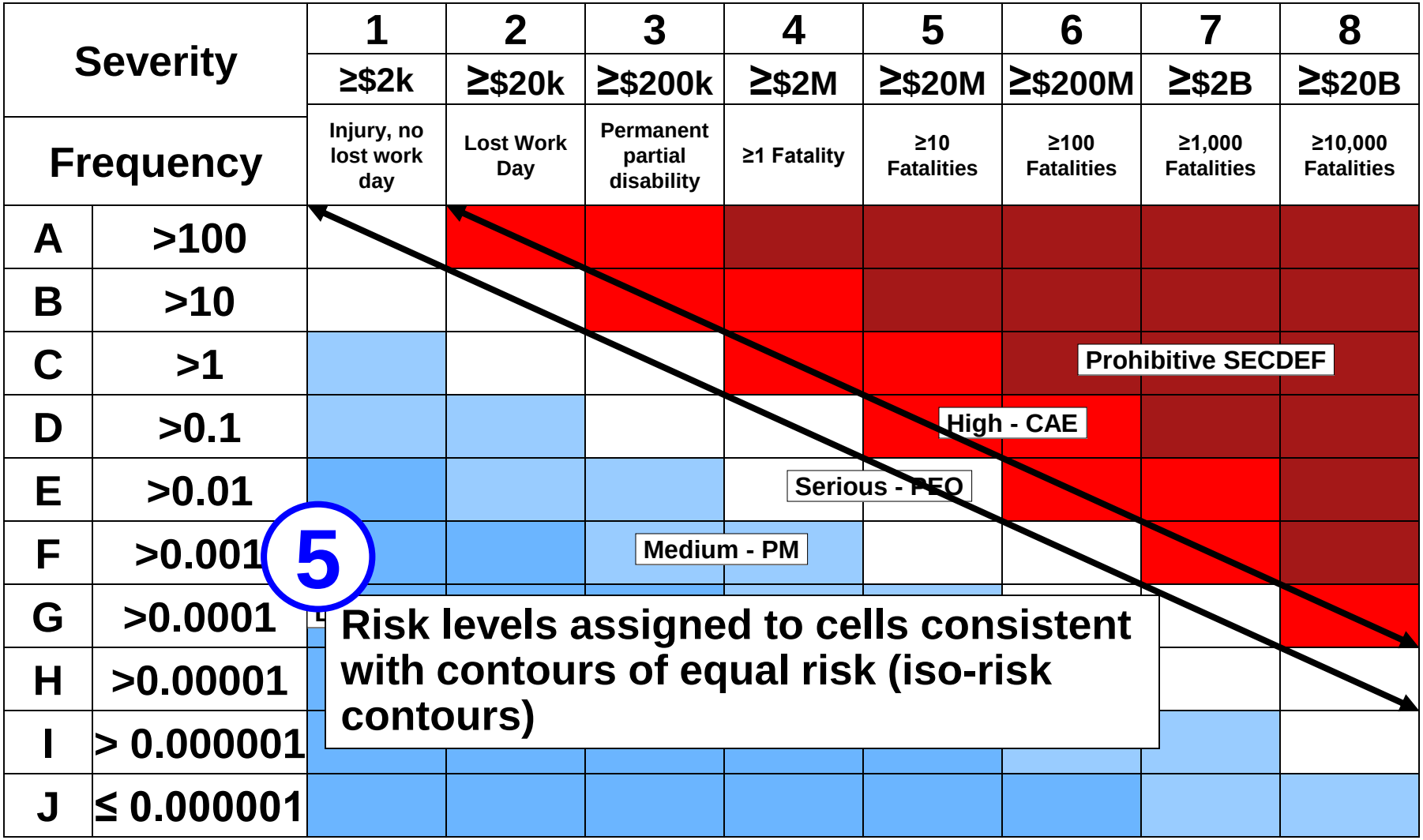


Attributes of a well-designed risk assessment matrix



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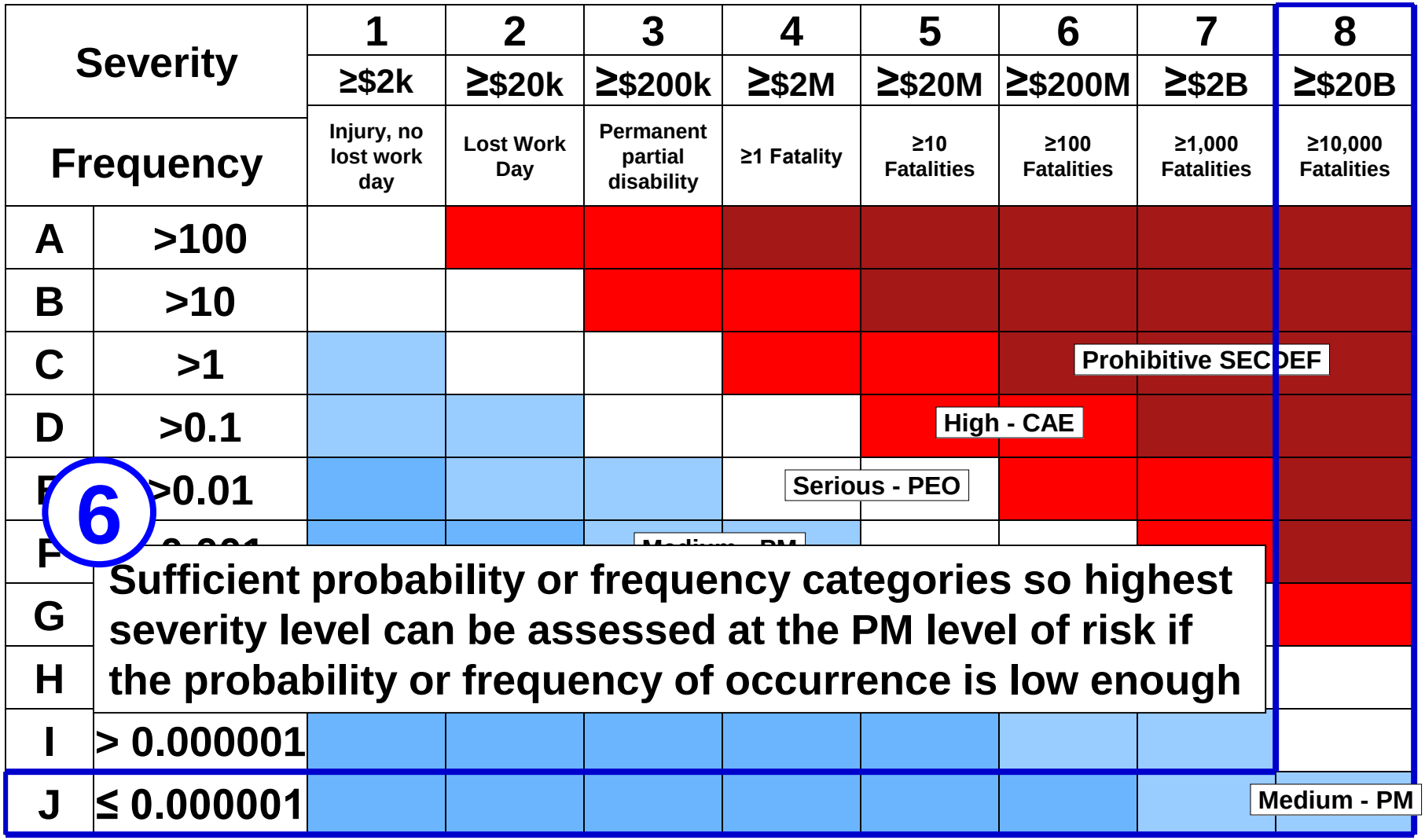

7 Attributes of a well-designed risk assessment matrix

ent code for hazards whose risk has been
ggest: 0R “Zero R” as in Zero Risk in lieu of F.

Frequency Category Letters Increase with Decreasing Frequency

		1	2	3	4	5	6	7	8
		≥$2k	≥$20k	≥$200k	≥$2M	≥$20M	≥$200M	≥$2B	≥$20B
		Injury, no lost work day	Lost Work Day	Permanent partial disability	≥1 Fatality	≥10 Fatalities	≥100 Fatalities	≥1,000 Fatalities	≥10,000 Fatalities
A	>100								
B	>10								
C	>1						Prohibitive SECDEF		
D	>0.1					High - CAE			
E	>0.01				Serious - PEO				
F	>0.001			Medium - PM					
G	>0.0001	Low – SSWG/Principal for Safety							
H	>0.00001								
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7 Attributes of a well-designed risk assessment matrix

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A	>100								
B	>10								
C	>1						Prohibitive SECDEF		
D	>0.1					High - CAE			
E	>0.01				Serious - PEO				
F		MIL-STD-882E Eliminated							

8 Attributes of a well-designed risk assessment matrix

A risk assessment code for hazards whose risk has been eliminated. Suggest: 0R "Zero R" as in Zero Risk in lieu of F.

Severity		1	2	3	4	5	6	7	8
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	>0.00001								
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Prohibitive SECDEF

High - CAE

Serio

5E

Medium - PM

Low – SSWG/Principal for Safety

9

Easily tailored with reporting of risk consistent with other systems within the family of systems.

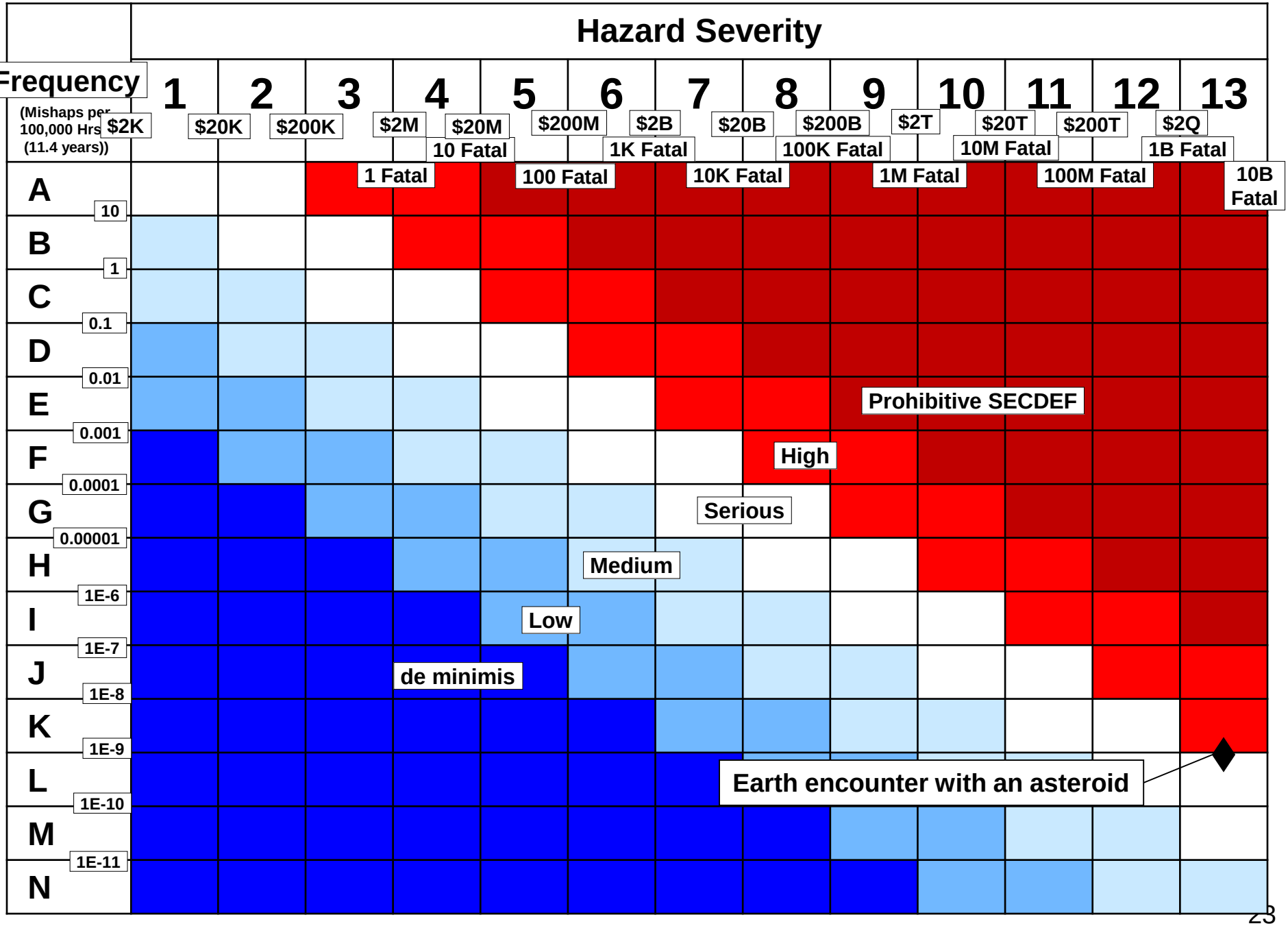
Attributes of a well-designed risk assessment matrix

10

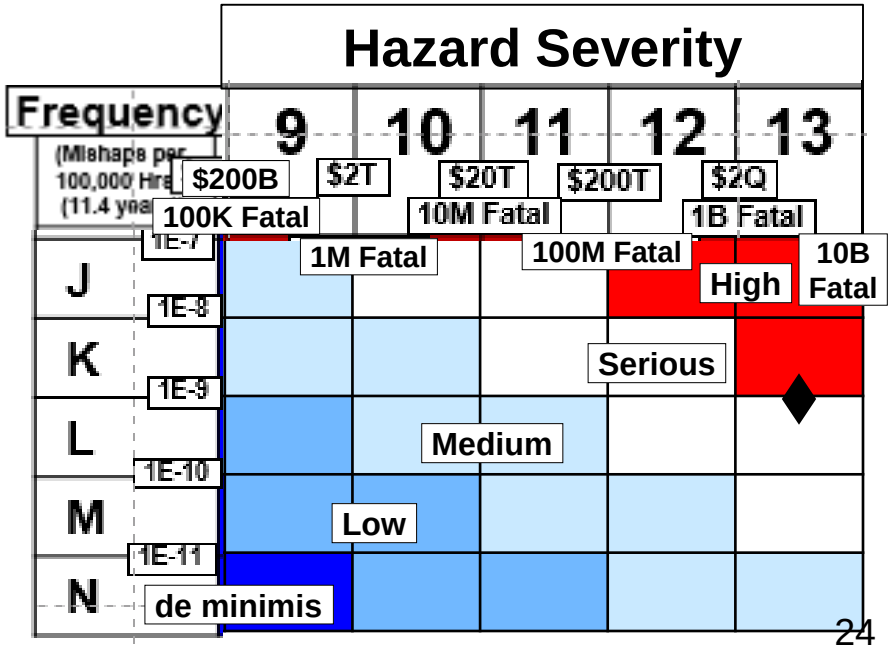
Severity Category numbers increase with increasing Severity

Severity		1	2	3	4	5	6	7
		≥$2k	≥$20k	≥$200k	≥$2M	≥$20M		
Frequency		Injury, no lost work day	Lost Work Day	Permanent partial disability	≥1 Fatality	≥10 Fatalities		
A	>100				Prohibitive SECDEF			
B	>10							
C	>1							
D	>0.1					High - CAE		
E	>0.01				Serio	5E		
F	>0.001			Medium - PM				
G	>0.0001	Low – SSWG/Principal for Safety						

Mother of All Risk Assessment Matrices (Spaceship Earth)

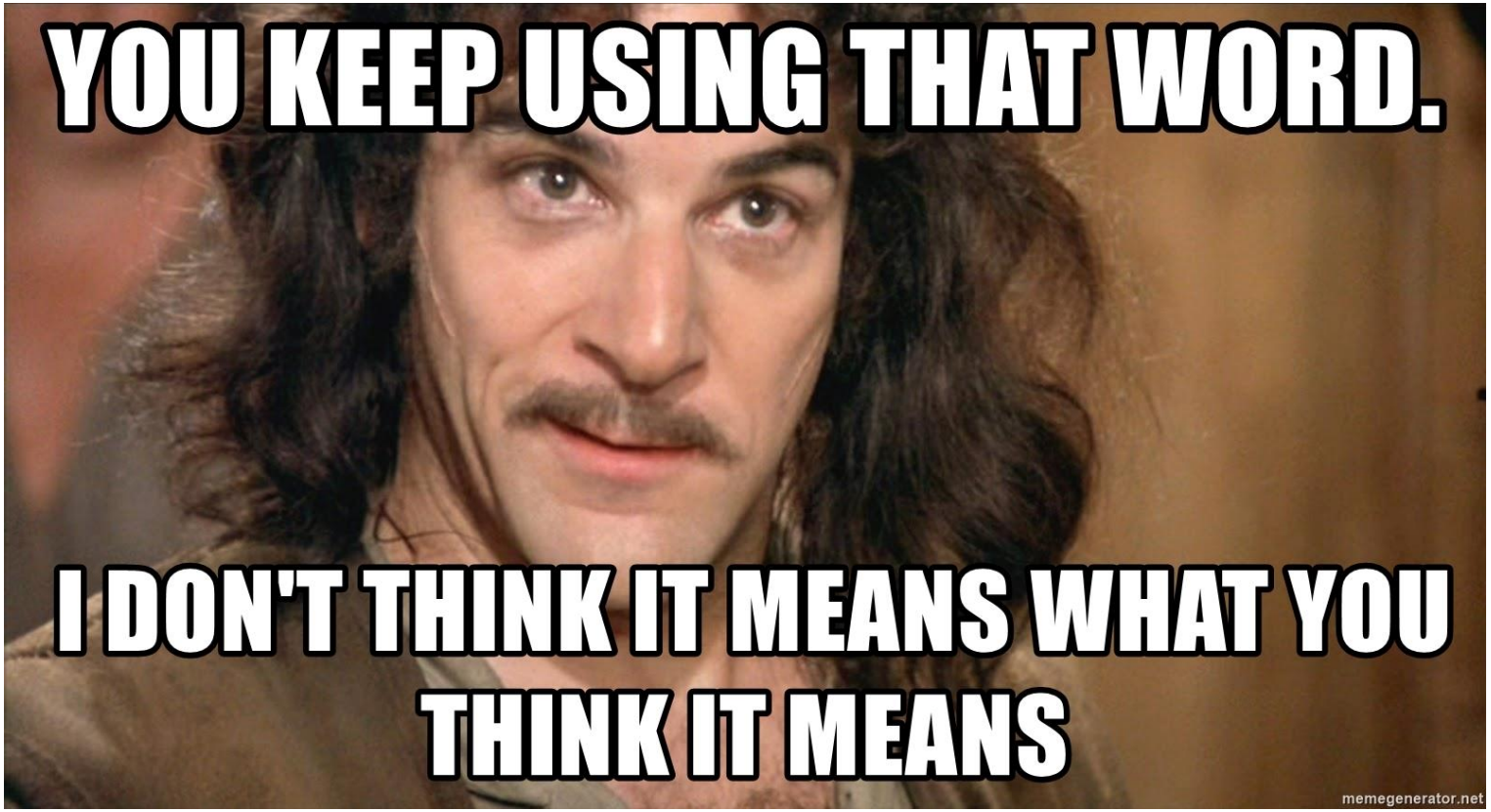


Even the Mother of All Risk Assessment Matrices can be tailored to the area most useful for the user.



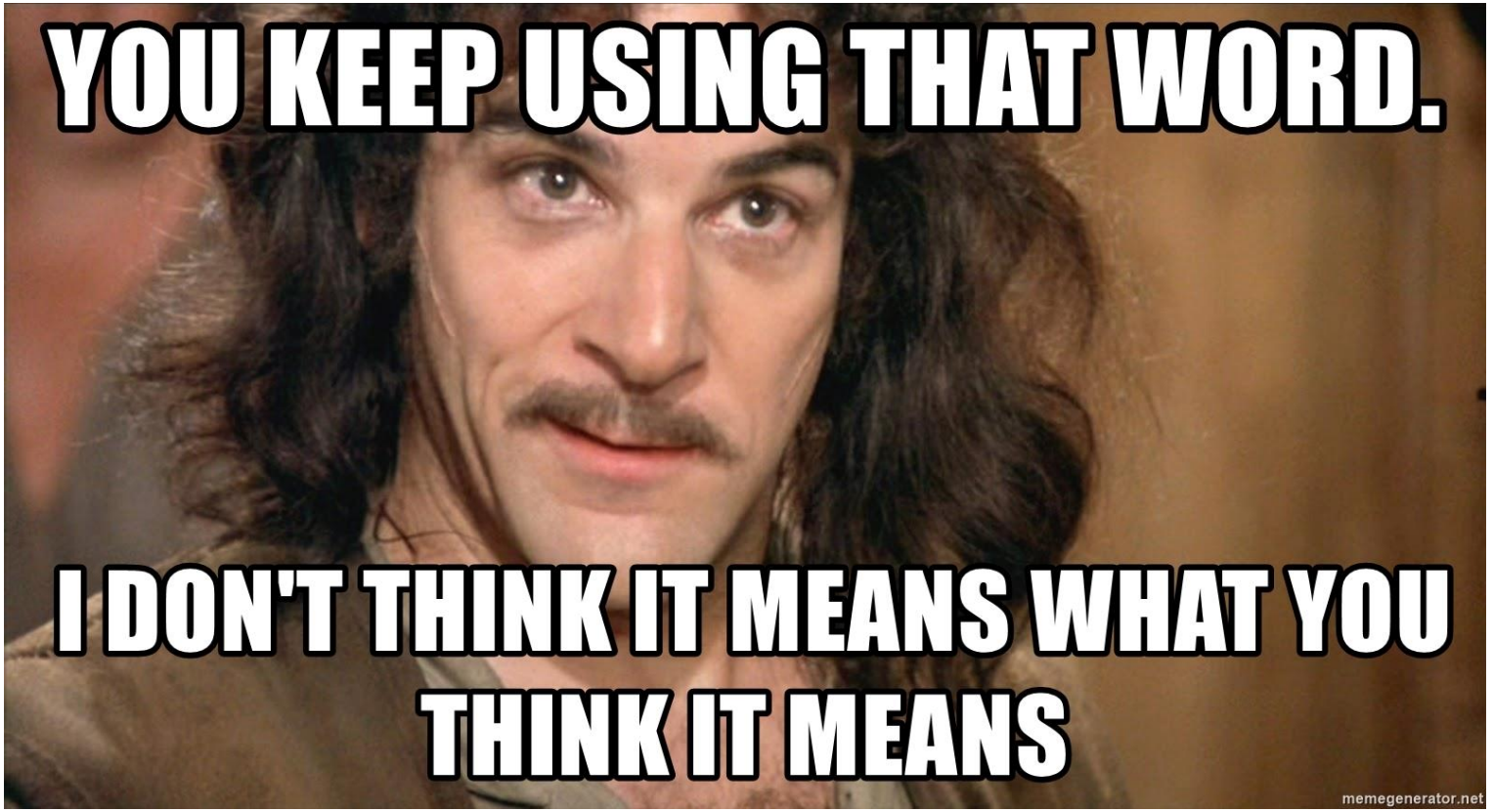
Additional Recommendation

- Eliminate one-word labels for Severity (Catastrophic, Critical, Marginal, Negligible) and Probability (Frequent, Probable, Occasional, Remote, Improbable)



Additional Recommendation

- Just use Severity 1, Severity 2, Probability C, etc.



MIL-STD-882D Matrix

RISK ASSESSMENT MATRIX				
SEVERITY / PROBABILITY	Catastrophic (1) $1M	Critical (2) $200K	Marginal (3) $10K	Negligible (4) $2K
Frequent (A)	High	High	Serious	Medium
Probable (B)	High	High	Serious	Medium
Occasional (C)	High	Serious	Medium	Low
Remote (D)	Serious	Medium	Medium	Low
Improbable (E)	Medium	Medium	Medium	Low

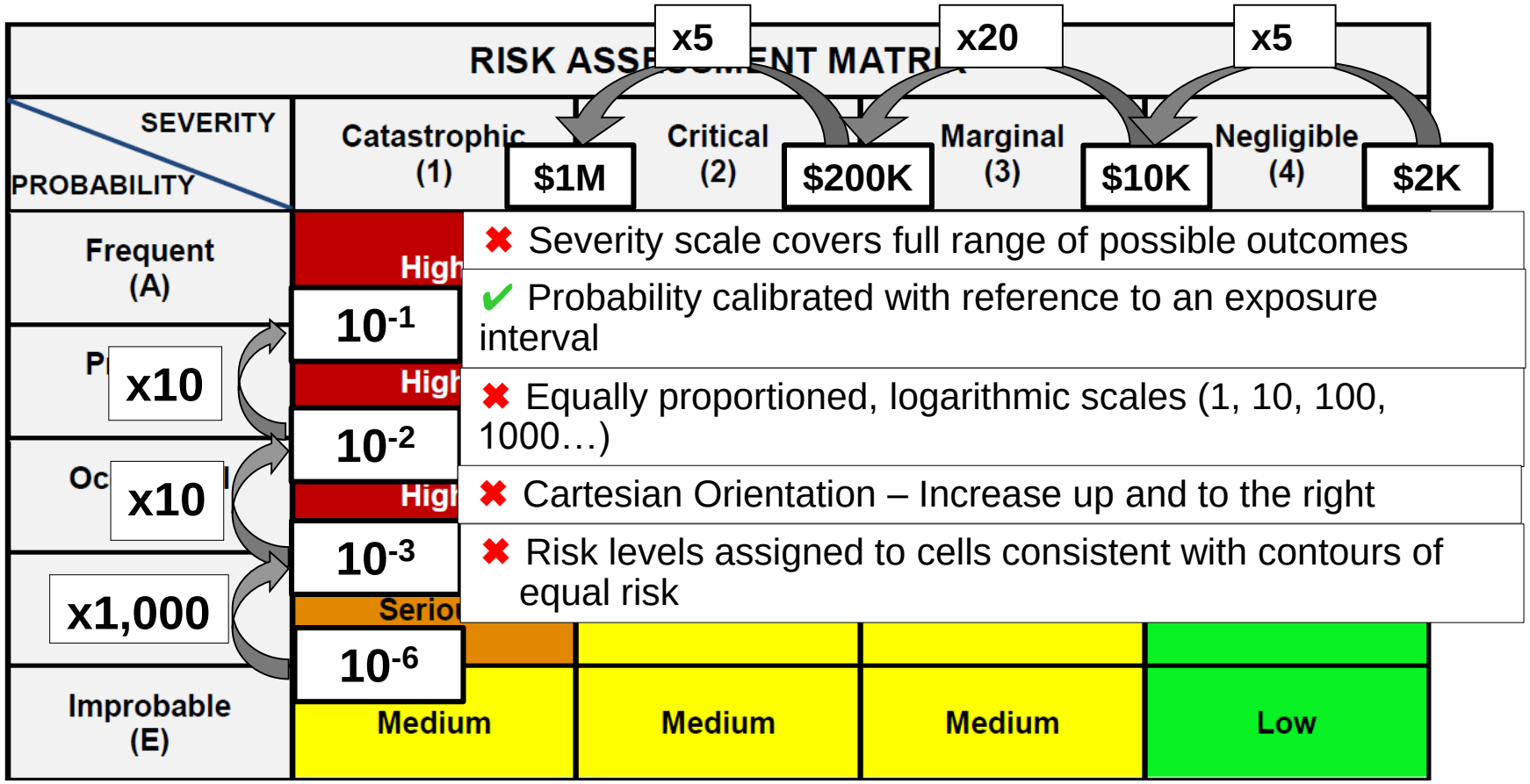
10^{-1}

10^{-2}

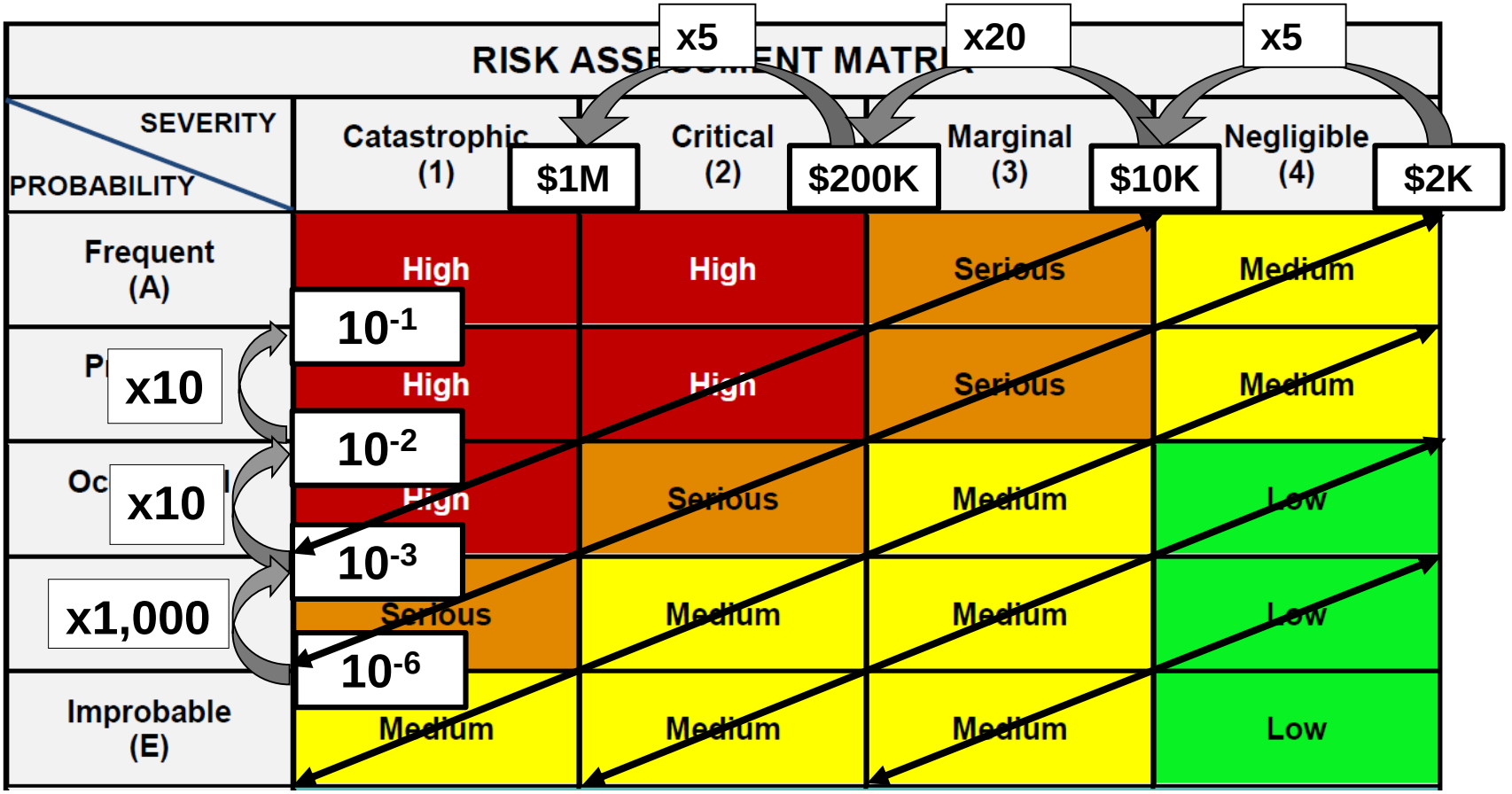
10^{-3}

10^{-6}

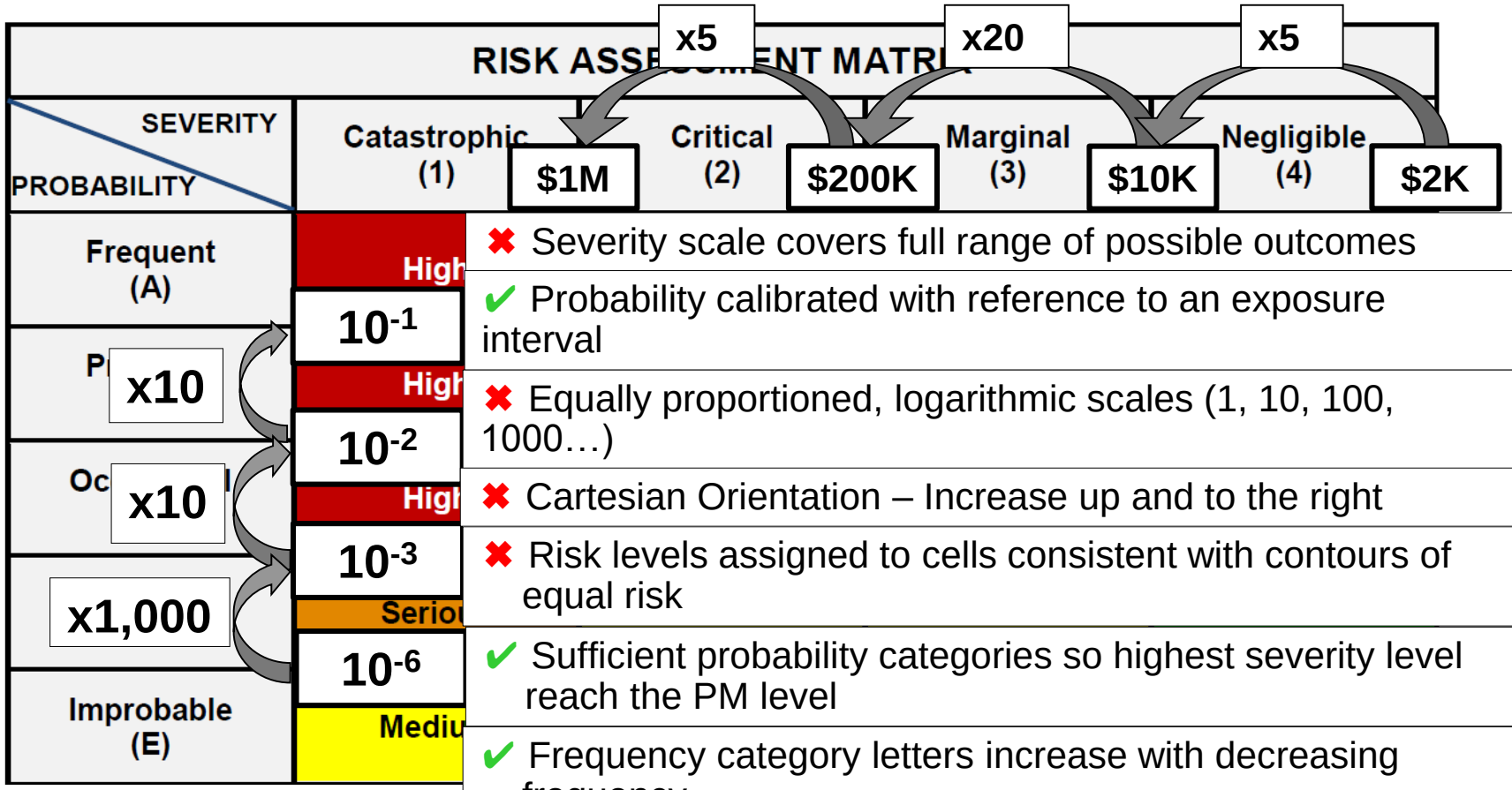
MIL-STD-882D Matrix



MIL-STD-882D Matrix



MIL-STD-882D Matrix

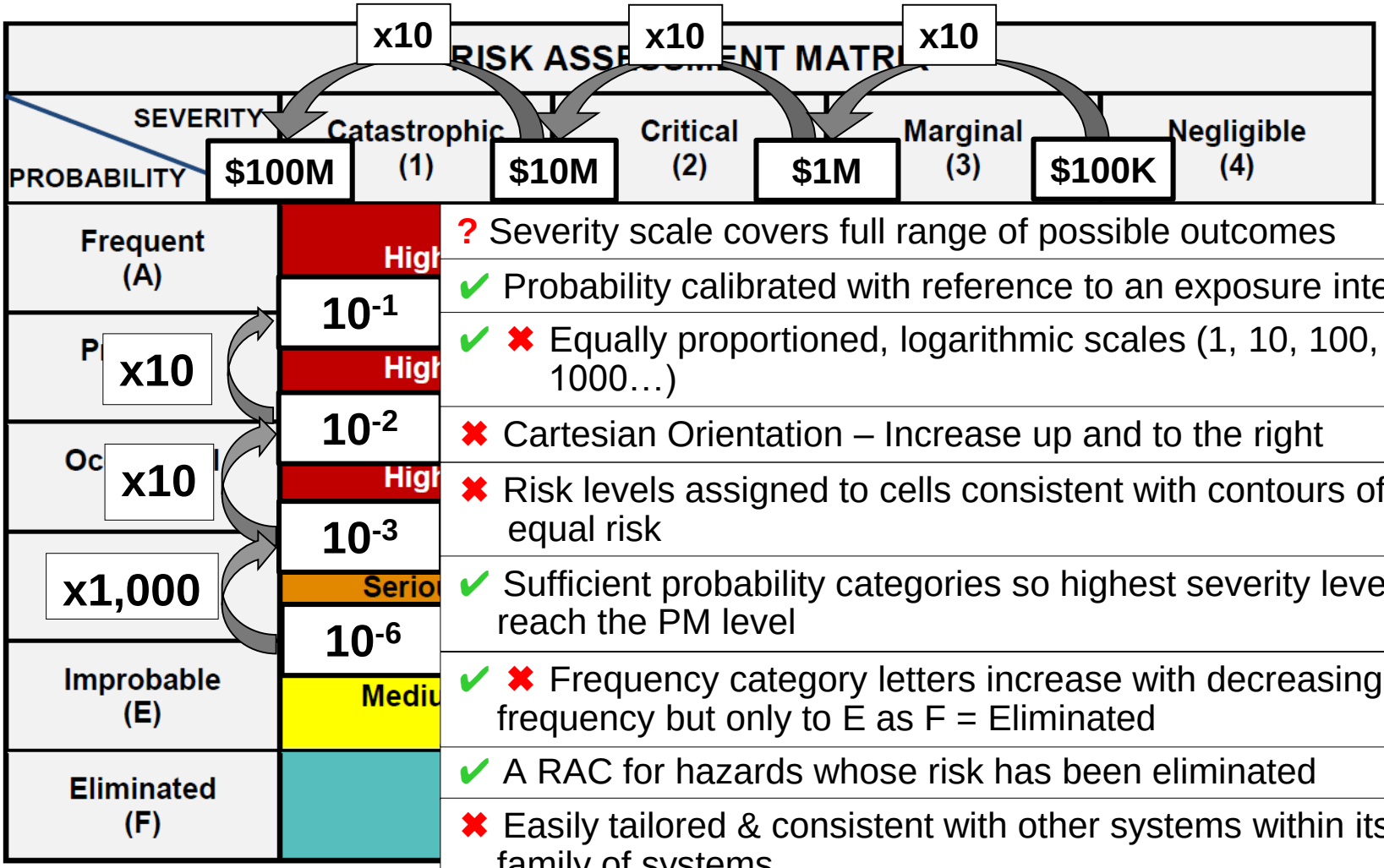


- ✖ Severity scale covers full range of possible outcomes
- ✔ Probability calibrated with reference to an exposure interval
- ✖ Equally proportioned, logarithmic scales (1, 10, 100, 1000…)
- ✖ Cartesian Orientation – Increase up and to the right
- ✖ Risk levels assigned to cells consistent with contours of equal risk
- ✔ Sufficient probability categories so highest severity level reach the PM level
- ✔ Frequency category letters increase with decreasing frequency
- ✖ A RAC for hazards whose risk has been eliminated
- ✖ Easily tailored & consistent with other systems within its family of systems
- ✖ Severity Category numbers increase with increasing Severity

MIL-STD-882E Matrix

RISK ASSESSMENT MATRIX				
SEVERITY / PROBABILITY	Catastrophic (1)	Critical (2)	Marginal (3)	Negligible (4)
	$10M	$1M	$100K	
Frequent (A)	High	High	Serious	Medium
	10^{-1}			
Probable (B)	High	High	Serious	Medium
	10^{-2}			
Occasional (C)	High	Serious	Medium	Low
	10^{-3}			
Remote (D)	Serious	Medium	Medium	Low
	10^{-6}			
Improbable (E)	Medium	Medium	Medium	Low
Eliminated (F)	Eliminated			

MIL-STD-882E Matrix



? Severity scale covers full range of possible outcomes
✔ Probability calibrated with reference to an exposure interval
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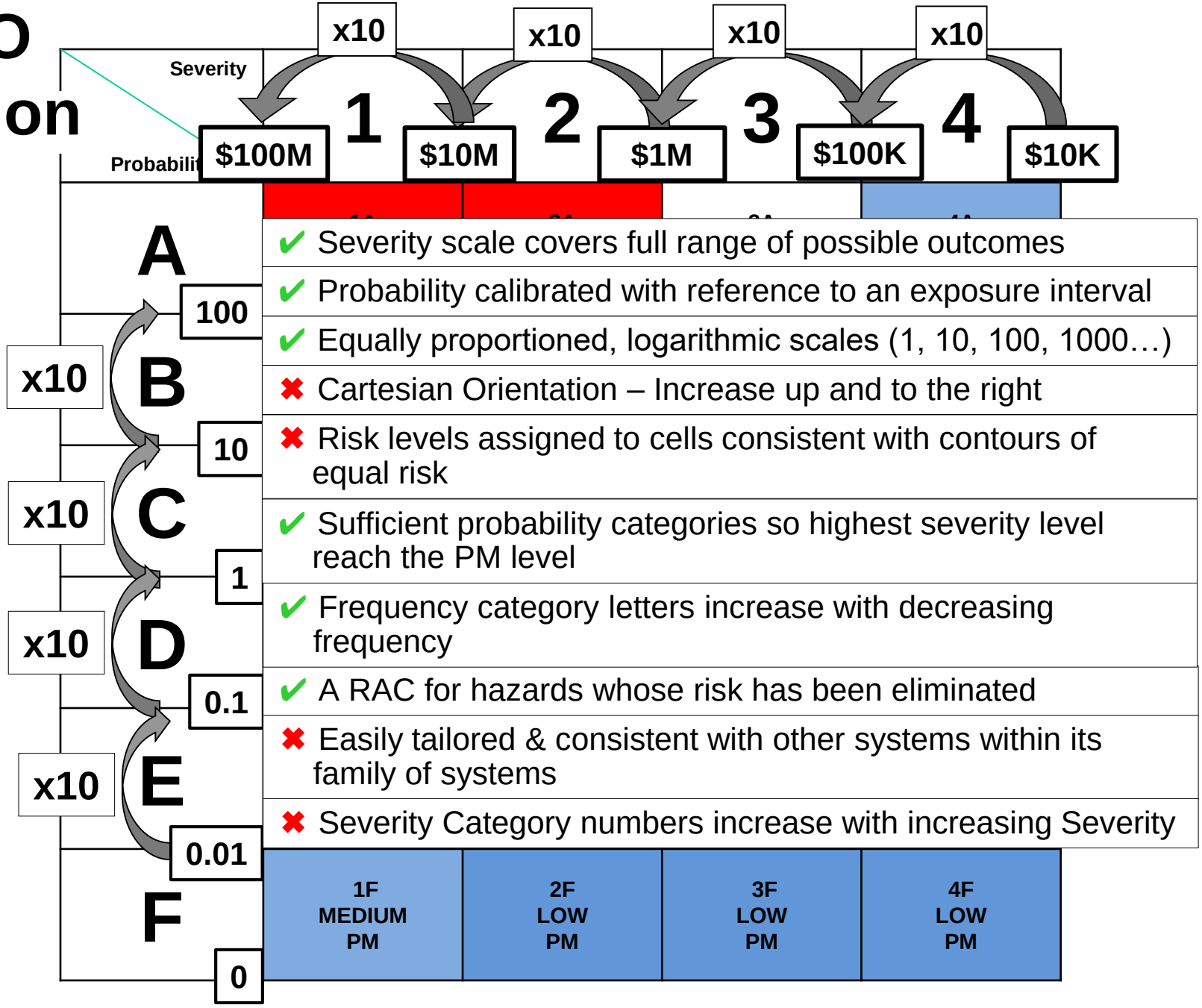
✖ Cartesian Orientation – Increase up and to the right
✖ Risk levels assigned to cells consistent with contours of equal risk
✔ Sufficient probability categories so highest severity level reach the PM level
✔ ✖ Frequency category letters increase with decreasing frequency but only to E as F = Eliminated
✔ A RAC for hazards whose risk has been eliminated
✖ Easily tailored & consistent with other systems within its family of systems
✖ Severity Category numbers increase with increasing Severity

PEO Aviation

Probability \ Severity	1 $10M	2 $1M	3 $100K	4 $10K
A 100	1A HIGH AAE	2A HIGH AAE	3A SERIOUS PEO	4A MEDIUM PM
B 10	1B HIGH AAE	2B HIGH AAE	3B SERIOUS PEO	4B MEDIUM PM
C 1	1C HIGH AAE	2C SERIOUS PEO	3C SERIOUS PEO	4C MEDIUM PM
D 0.1	1D SERIOUS PEO	2D SERIOUS PEO	3D MEDIUM PM	4D MEDIUM PM
E 0.01	1E SERIOUS PEO	2E MEDIUM PM	3E MEDIUM PM	4E LOW PM
F 0	1F MEDIUM PM	2F LOW PM	3F LOW PM	4F LOW PM

0R

PEO Aviation



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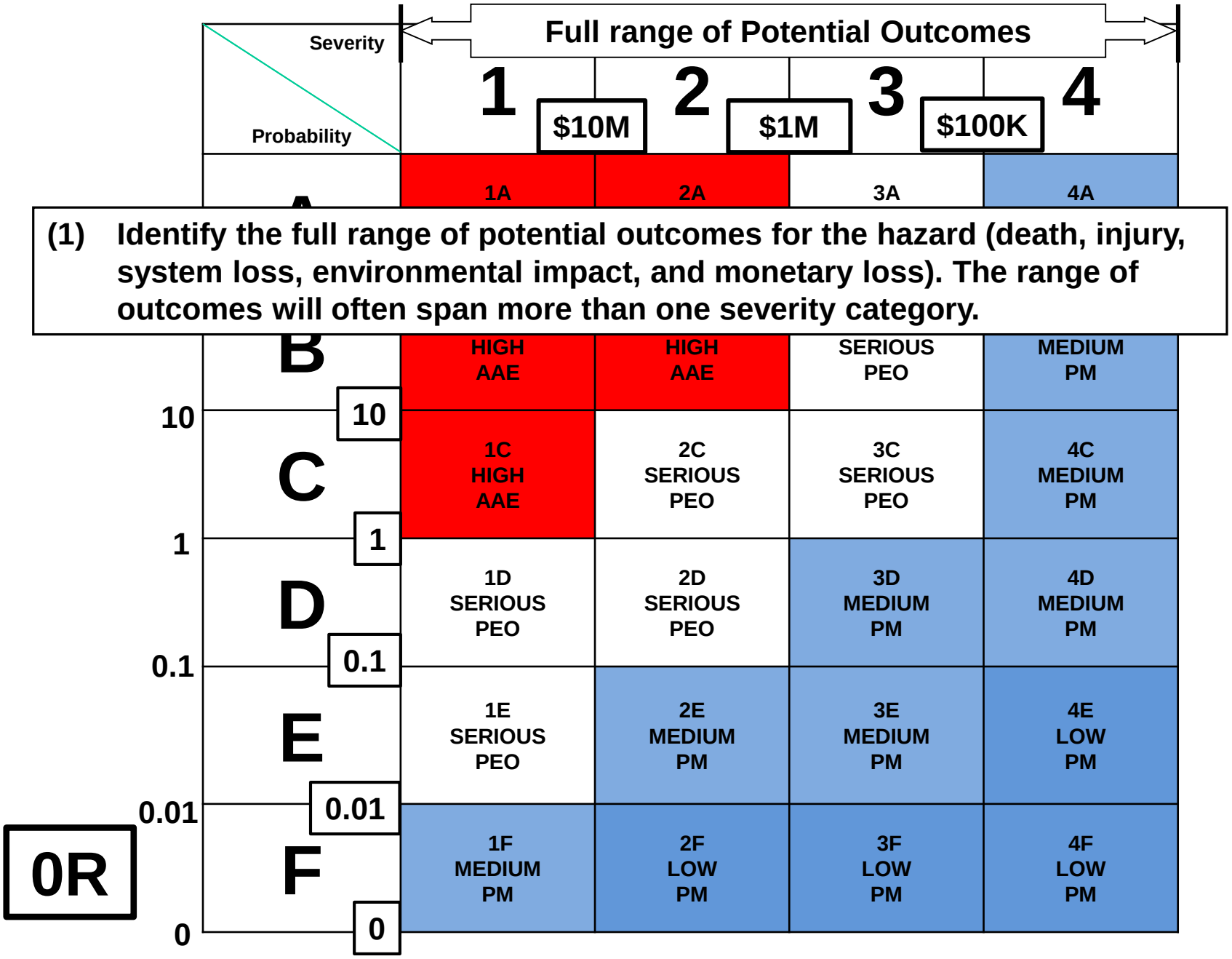
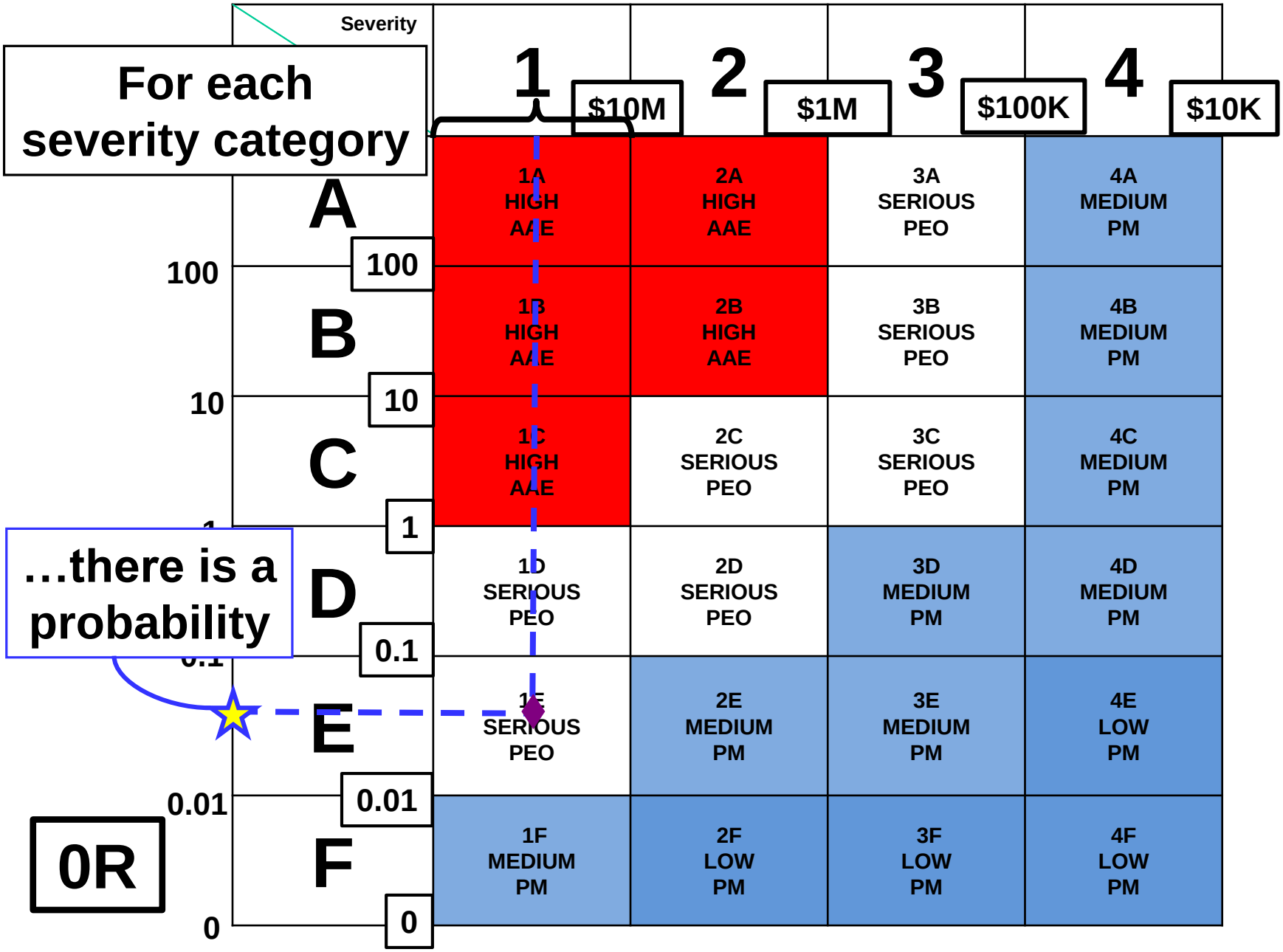
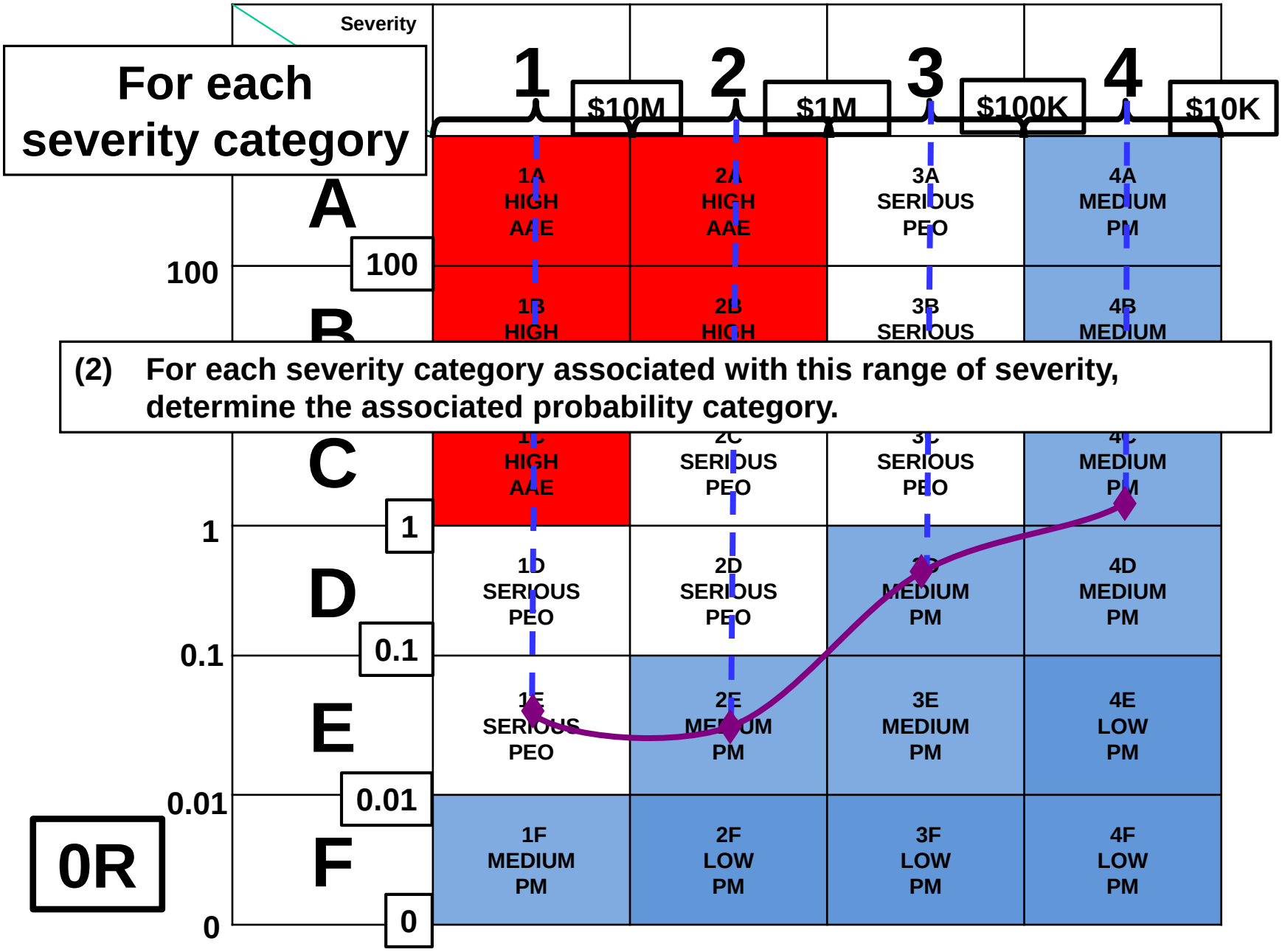

Full range of Potential Outcomes
Severity
Probability
1
$10M
2
$1M
3
$100K
4
1A
2A
3A
4A
(1) Identify the full range of potential outcomes for the hazard (death, injury, system loss, environmental impact, and monetary loss). The range of outcomes will often span more than one severity category.
B
HIGH AAE
HIGH AAE
SERIOUS PEO
MEDIUM PM
10
10
C
1C HIGH AAE
2C SERIOUS PEO
3C SERIOUS PEO
4C MEDIUM PM
1
1
D
1D SERIOUS PEO
2D SERIOUS PEO
3D MEDIUM PM
4D MEDIUM PM
0.1
0.1
E
1E SERIOUS PEO
2E MEDIUM PM
3E MEDIUM PM
4E LOW PM
0.01
0.01
F
1F MEDIUM PM
2F LOW PM
3F LOW PM
4F LOW PM
0
0
0R

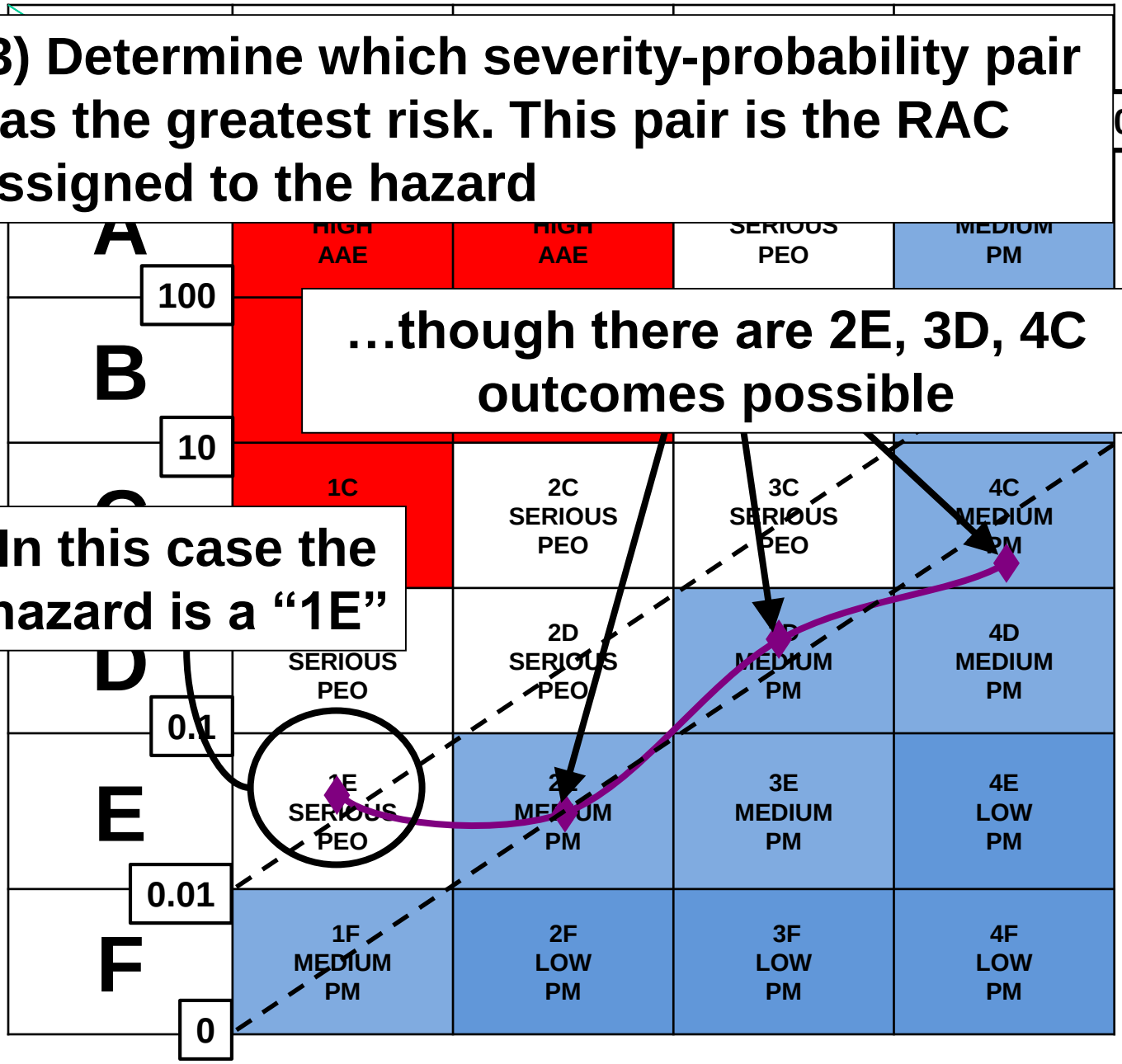

For each severity category
…there is a probability
0R
Severity
1
$10M
2
$1M
3
$100K
4
$10K
A
100
B
10
C
1
D
0.1
E
0.01
F
0
1A HIGH AAE
2A HIGH AAE
3A SERIOUS PEO
4A MEDIUM PM
1B HIGH AAE
2B HIGH AAE
3B SERIOUS PEO
4B MEDIUM PM
1C HIGH AAE
2C SERIOUS PEO
3C SERIOUS PEO
4C MEDIUM PM
1D SERIOUS PEO
2D SERIOUS PEO
3D MEDIUM PM
4D MEDIUM PM
1E SERIOUS PEO
2E MEDIUM PM
3E MEDIUM PM
4E LOW PM
1F MEDIUM PM
2F LOW PM
3F LOW PM
4F LOW PM

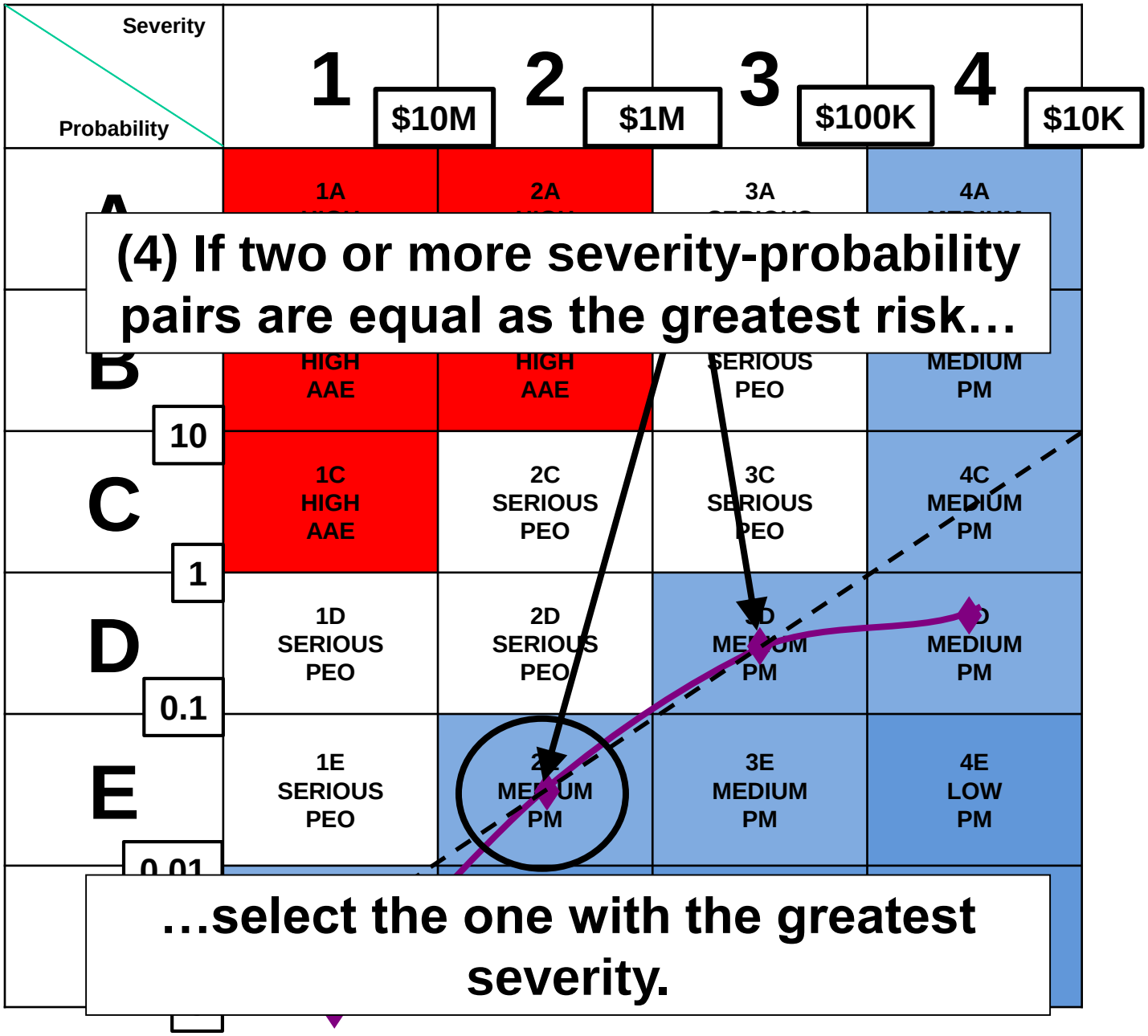

For each severity category
Severity
1
$10M
2
$1M
3
$100K
4
$10K
A
100
1A HIGH AAE
2A HIGH AAE
3A SERIOUS PEO
4A MEDIUM PM
B
1B HIGH
2B HIGH
3B SERIOUS
4B MEDIUM
C
1C HIGH AAE
2C SERIOUS PEO
3C SERIOUS PEO
4C MEDIUM PM
1
D
0.1
1D SERIOUS PEO
2D SERIOUS PEO
3D MEDIUM PM
4D MEDIUM PM
E
0.01
1E SERIOUS PEO
2E MEDIUM PM
3E MEDIUM PM
4E LOW PM
F
0
1F MEDIUM PM
2F LOW PM
3F LOW PM
4F LOW PM
0R
(2) For each severity category associated with this range of severity, determine the associated probability category.

(3) Determine which severity-probability pair has the greatest risk. This pair is the RAC assigned to the hazard

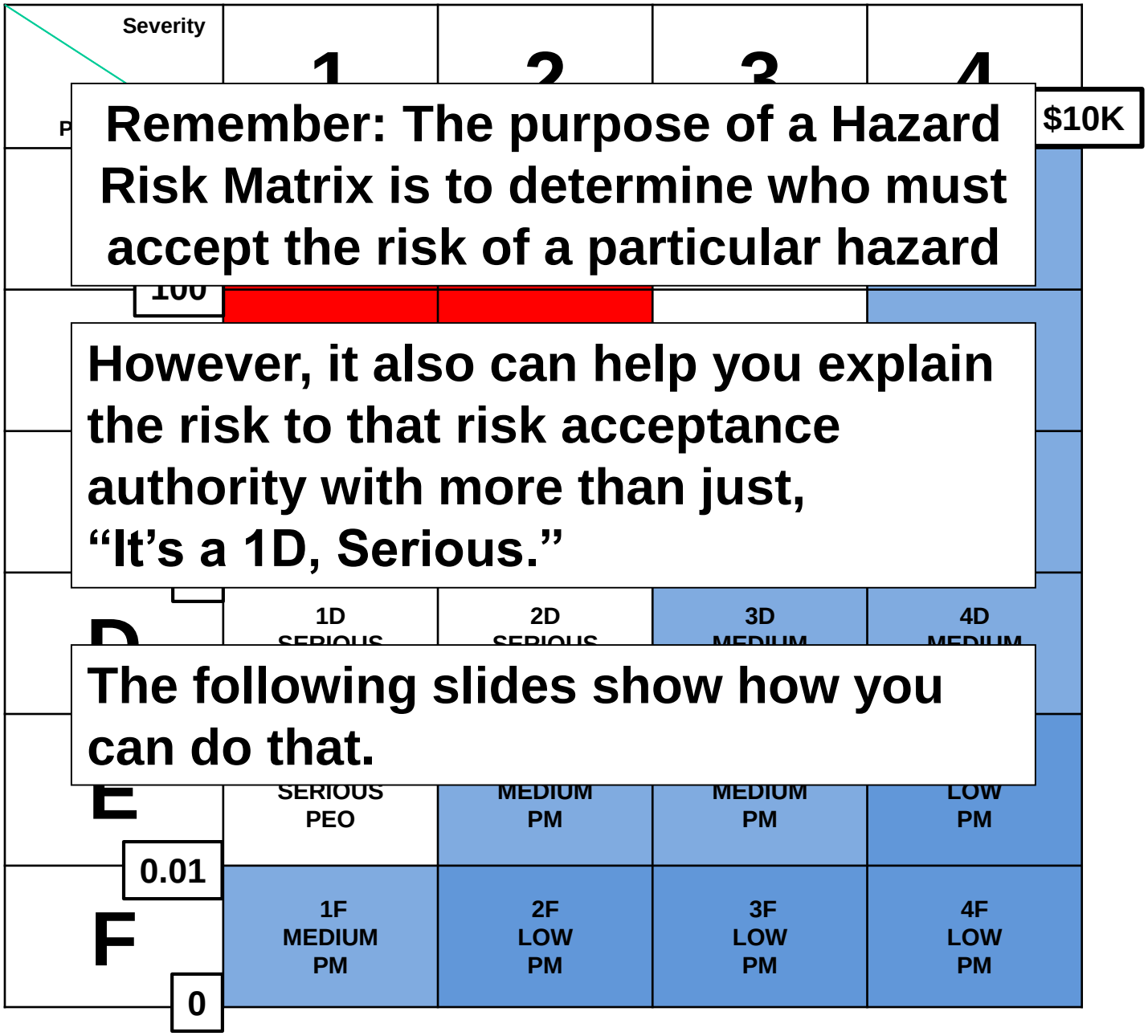
…though there are 2E, 3D, 4C outcomes possible

In this case the hazard is a "1E"




Severity
Probability
1
$10M
2
$1M
3
$100K
4
$10K
A
B
10
C
1
D
0.1
E
0.01
1A
2A
3A
4A
HIGH
AAE
HIGH
AAE
SERIOUS
PEO
MEDIUM
PM
1C
HIGH
AAE
2C
SERIOUS
PEO
3C
SERIOUS
PEO
4C
MEDIUM
PM
1D
SERIOUS
PEO
2D
SERIOUS
PEO
MEDIUM
PM
MEDIUM
PM
1E
SERIOUS
PEO
MEDIUM
PM
3E
MEDIUM
PM
4E
LOW
PM
(4) If two or more severity-probability pairs are equal as the greatest risk…
…select the one with the greatest severity.

0R



Remember: The purpose of a Hazard Risk Matrix is to determine who must accept the risk of a particular hazard

However, it also can help you explain the risk to that risk acceptance authority with more than just, "It's a 1D, Serious."

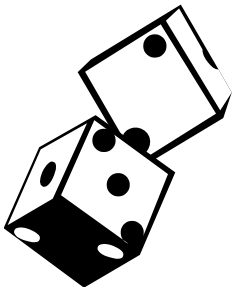
The following slides show how you can do that.

0R

Topics for this Tutorial

- Purpose of a Hazard Risk Matrix
- Understanding the Attributes of a well-designed risk assessment matrix
- How to Assign a Risk Assessment Code
- **Understanding Probability**
- Building an Expanded Matrix
- Plotting Accidents on a Matrix
- Using Relative Risk Values
- Building Hazard Risk Profiles

Understanding Probability

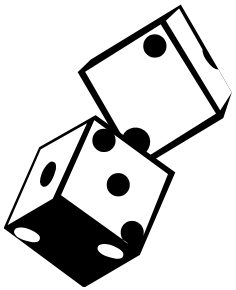


Probability:

“A number expressing the likelihood that a specific event will occur, expressed as the ratio of the number of actual occurrences to the number of possible occurrences.”

- The American Heritage® Dictionary of the English Language, Fourth Edition

Understanding Probability



Math Definition:

- **Repeat a random experiment “n” number of times.**
- **If a specific outcome has occurred “f” times in these n trials, the number “f” is the frequency of the outcome.**
- **The ratio f/n is the relative frequency of the outcome.**
- **A relative frequency is usually very unstable for small values of “n,” but it tends to stabilize about some number “p” as “n” increases.**
- **The number “p” is the probability of the outcome.**

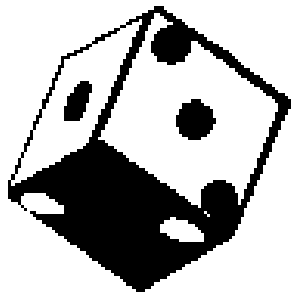
$$p = f / n$$

for very large values of n

Understanding Probability

Simple example:

Probability of rolling a “3” with one die.



Roll #1 - “5”, f/n = 0/1 = 0

Roll #2 - “2”, f/n = 0/2 = 0

Roll #3 - “3”, f/n = 1/3 = .333…

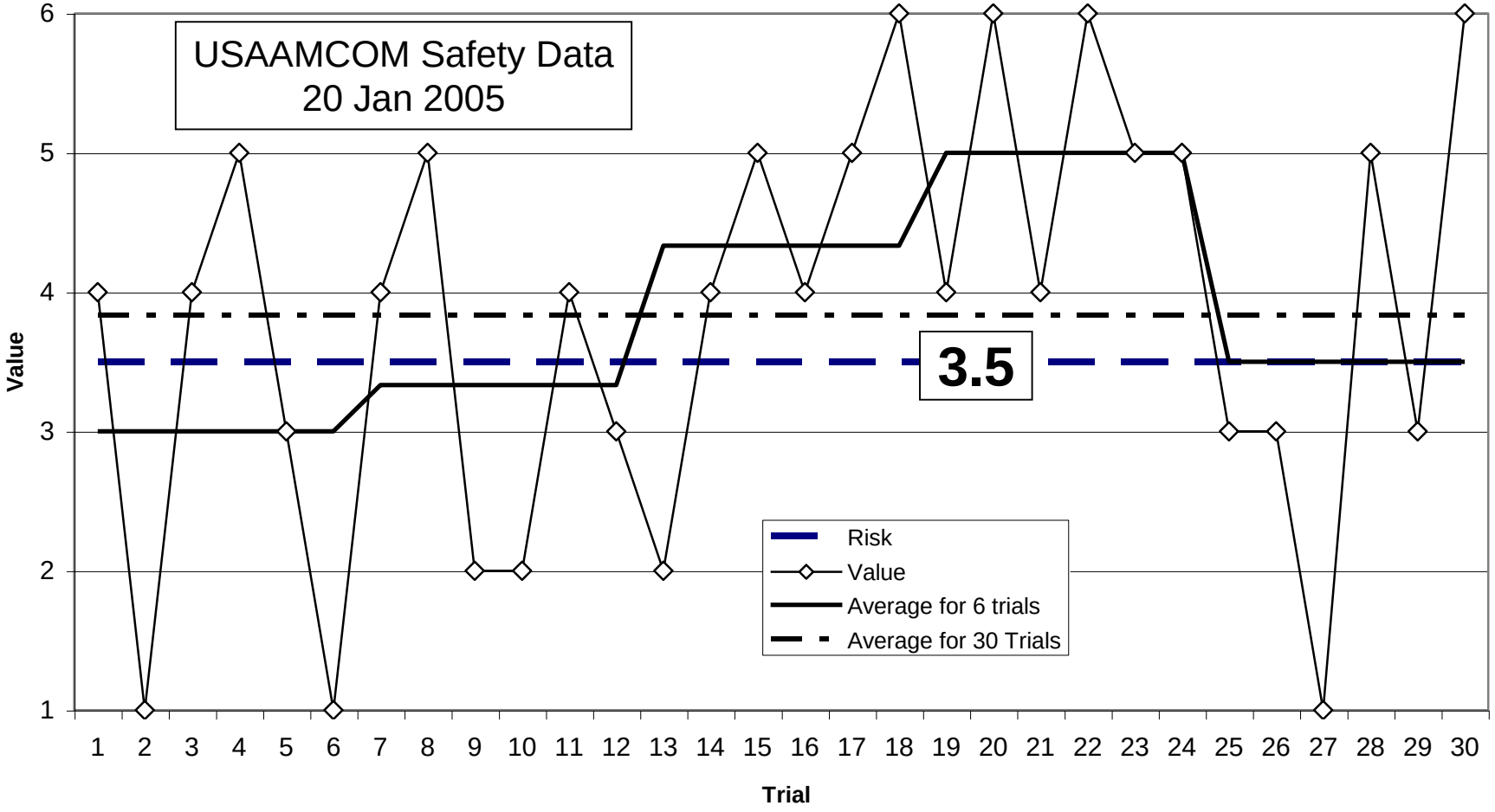
Roll #4 - “4”, f/n = 1/4 = .25

Roll #1,000: 163 “3”s, f/n = 163/1000 = .163

Rolls approach infinity f/n = .166666….

Rolling Dice

Roll a single die 30 times. The expected value of each roll is 3.5. What you actually get is somewhat different.



Understanding Probability

Hazard: Helicopter strikes wire; results in Class A mishap

Probability: 4.406E-06 occurrences per flight hour

1 Flight Hr, no mishap, rate = 0

1,000 Flight Hrs, no mishap, rate = 0

176,182 Flight Hrs, 1st mishap, rate = 5.676E-06 /flt hr

274,539 Flight Hrs, 2nd mishap, rate = 7.285E-06 /flt hr

700,462 Flt Hrs, 3rd mishap, rate = 4.283E-06 /flt hr

10,000,000 Flt Hrs, 46 mishaps, rate = 4.600E-06 /flt hr

1,000,000,000 Hrs, 4407 mishaps, rate = 4.407E-06 /flt hr

Flight hours approach infinity, rate = 4.406E-06 /flt hr

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PEO Aviation Risk Decision Authority Matrix

Probability \ Severity	1 $10M	2 $1M	3 $100K	4 $10K
A 100	1A HIGH AAE	2A HIGH AAE	3A SERIOUS PEO	4A MEDIUM PM
B 10	1B HIGH AAE	2B HIGH AAE	3B SERIOUS PEO	4B MEDIUM PM
C 1	1C HIGH AAE	2C SERIOUS PEO	3C SERIOUS PEO	4C MEDIUM PM
D 0.1	1D SERIOUS PEO	2D SERIOUS PEO	3D MEDIUM PM	4D MEDIUM PM
E 0.01	1E SERIOUS PEO	2E MEDIUM PM	3E MEDIUM PM	4E LOW PM
F 0	1F MEDIUM PM	2F LOW PM	3F LOW PM	4F LOW PM

0R

Applying Probability Classifications to a military helicopter

Fleet Size = 368 aircraft

Utilization = 240 hours/year

Life = 12 years/aircraft

Aircraft Life = 240 x 12
= 2,880 hours

Fleet Exposure Hours = 368 x 240 x 12
= 1,059,840 hours

Fleet Hours per Year = 368 x 240
= 88,320 hours

US Army PEO Aviation Enhanced Matrix

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	Events per Year	Years per Event
Frequent **A**	10^{-3}	1,000	100	88.32	0.0113
Probable **B**	10^{-4}	10,000	10	8.832	0.113
Occasional **C**	10^{-5}	100,000	1	0.8832	1.13
Remote **D**	10^{-6}	1,000,000	0.1	0.0883	11.3
Improbable **E**	10^{-7}	10,000,000	0.01	0.00883	113
Very Improbable **F**	0		0	0	
Zero Risk **0R**					

US Army PEO Aviation Enhanced Matrix

$$\frac{88{,}320 \text{ flt hrs}}{\text{Year}} \times \frac{10 \text{ Events}}{100{,}000 \text{ flt hrs}} = \frac{8.832 \text{ Events}}{\text{Year}}$$

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	Events per Year	Years per Event
Probable B	10^{-4}	10,000	10	8.832	0.113
Occasional C	10^{-5}	100,000	1	0.8832	1.13
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Improbable E	10^{-7}	10,000,000	0.01	0.00883	113
Very Improbable F	0		0	0	
Zero Risk 0R					

US Army PEO Aviation Enhanced Matrix

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	Events per Year	Years per Event	Event per Fleet Life	Fleet Life per Event
Frequent **A**	10^{-3}	1,000	100	88.32	0.0113	1,060	0.000944
Probable **B**	10^{-4}	10,000	10	8.832	0.113	105.98	0.00944
Occasional **C**	10^{-5}	100,000	1	0.8832	1.13	10.598	0.0944
Remote **D**	10^{-6}	1,000,000	0.1	0.0883	11.3	1.0598	0.944
Improbable **E**	10^{-7}	10,000,000	0.01	0.00883	113	0.106	9.44
Very Improbable **F**	0		0	0		0	
Zero Risk **0R**							

US Army PEO Aviation Enhanced Matrix

$$\frac{1{,}059{,}840 \text{ flt hrs}}{1 \text{ fleet life}} \times \frac{10 \text{ Events}}{100{,}000 \text{ flt hrs}} = \frac{105.98 \text{ Events}}{1 \text{ Fleet Life}}$$

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	Events per Year	Years per Event	Event per Fleet Life	Fleet Life per Event
Probable B	10^{-4}	10,000	10	8.832	0.113	105.98	0.00944
Occasional C	10^{-5}	100,000	1	0.8832	1.13	10.598	0.0944
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Improbable E	10^{-7}	10,000,000	0.01	0.00883	113	0.106	9.44
Very Improbable F	0		0	0		0	
Zero Risk 0R							

US Army PEO Aviation Enhanced Matrix

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	Events per Year	Years per Event	Event per Fleet Life	Fleet Life per Event
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Improbable **E**	10^{-7}	10,000,000	0.01	0.00883	113	0.106	9.44
Very Improbable **F**	0		0	0		0	
Zero Risk **0R**							

Numbers greater than 1 are easier to comprehend

US Army PEO Aviation Enhanced Matrix

Input
Calculated

Assumptions	
Fleet Size:	368 aircraft
Utilization:	240.0 hours/yr
Aircraft Life:	12 years
Calculations	
Aircraft Exposure Hours:	2,880 hours
Fleet Exposure Hours:	1,059,840 hours
Fleet Hours per Year:	88,320 hours

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	1 ($10M)	2 ($1M)	3 ($100K)	4	Fleet-wide: Events per Year	Years per Event	Event per Fleet Life	Fleet Life per Event
A	10^{-3}	1,000	100	1A	2A	3A	4A	88.32	0.0113	1,060	0.000944
B	10^{-4}	10,000	10	1B	2B	3B	4B	8.832	0.113	105.98	0.00944
C	10^{-5}	100,000	1	1C	2C	3C	4C	0.8832	1.13	10.598	0.0944
D	10^{-6}	1,000,000	0.1	1D	2D	3D	4D	0.0883	11.3	1.0598	0.944
E	10^{-7}	10,000,000	0.01	1E	2E	3E	4E	0.00883	113	0.106	9.44
F	0		0	1F	2F	3F	4F	0		0	
0R											

High AAE
Serious PEO
Medium PM
Low PM

Consequences of Risk Acceptance

Consequences of Risk Acceptance:
On the order of 2 to 10 Class A accidents due to this hazard over the remaining life cycle of the aircraft.

				Aircraft Exposure Hours: 2,880 hours Fleet Exposure Hours: 1,059,840 hours Fleet Hours per Year: 88,320 hours				Fleet-wide			
	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	1	2	3	4	Events per Year	Years per Event	Event per Fleet Life	Fleet Life per Event
					$10M	$1M	$100K				
A	10^{-3}	1,000	100	1A	2A	3A	4A	88.32	0.0113	1,060	0.000944
B	10^{-4}	10,000	10	1B	2B	3B	4B	8.832	0.113	105.98	0.00944
C	10^{-5}	100,000	1	1C	2C	3C	4C	0.8832	1.13	10.598	0.0944
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E	10^{-7}	10,000,000	0.01	1E	2E	3E	4E	0.00883	113	0.106	9.44
F	0		0	1F	2F	3F	4F	0		0	
0R											

High AAE

Serious PEO

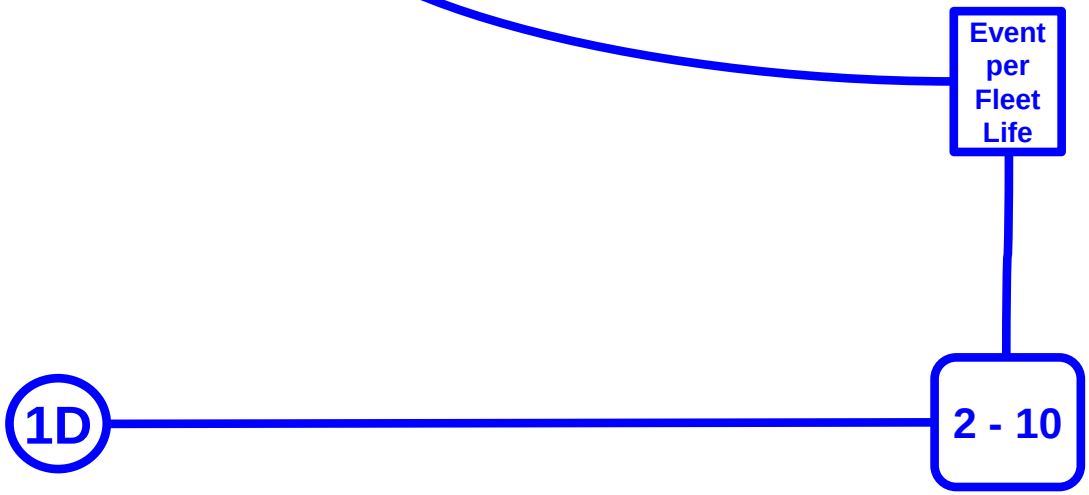
Medium PM

Low PM

2 - 10

Consequences of Risk Acceptance

Consequences of Risk Acceptance:
On the order of 2 to 10 Class A accidents due to this hazard over the remaining life cycle of the aircraft.



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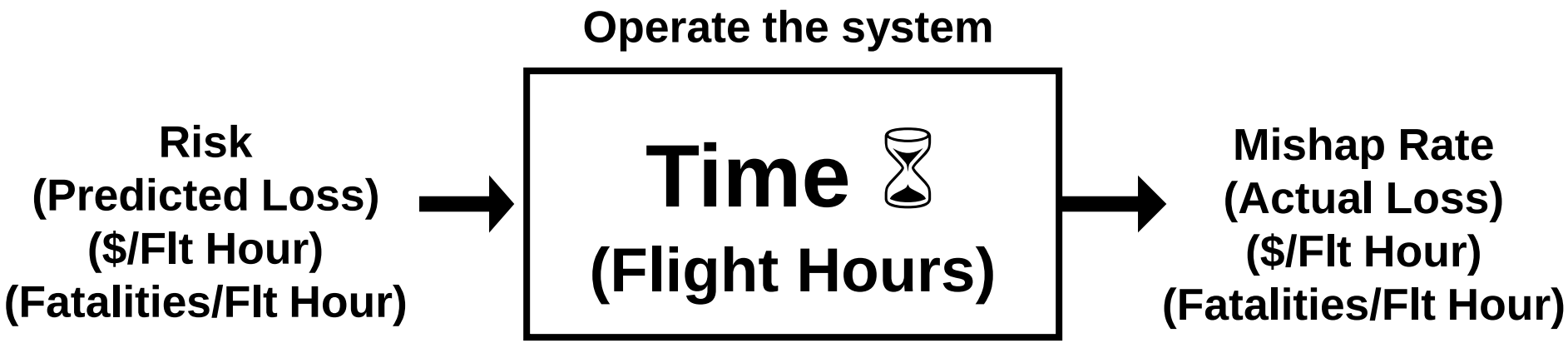
Mishap Risk & Mishap Loss

Mishap Risk over Time results in Mishap Loss



Mishap History

Based on this relationship between mishap risk and mishap loss, we can plot mishap histories on a risk matrix as follows:

$$\text{Severity} = \frac{\text{Total Cost from Class A mishaps}}{\text{Total Number of Class A mishaps}}$$

$$= \frac{\$361,671,038}{59} = \$\ 6,130,018$$

$$\text{Probability} = \frac{\text{Total Number of Class A mishaps}}{\text{Total Hours Flown}}$$

$$= \frac{59}{1,588,597} = 3.714 \text{ mishaps / 100,000 Flt Hrs}$$

Mishap History

Class	No	Total Cost	Cost/Mishap	Mishaps per 100,000 Flt Hrs
A	59	$361,671,038	$6,130,018	3.714
B	39	$18,854,121	$483,439	2.455
C	245	$17,114,206	$69,854	15.422
D	112	$970,148	$8,662	7.050
Total	455	$398,609,513		

Mishaps

The numbers plot on a chart like this.

Class	No	Total Cost	Cost/Mishap	Mishaps per 100,000 Flt Hrs
A	59	$361,671,038	$6,130,018	3.714
B	39	$18,854,121	$483,439	2.455
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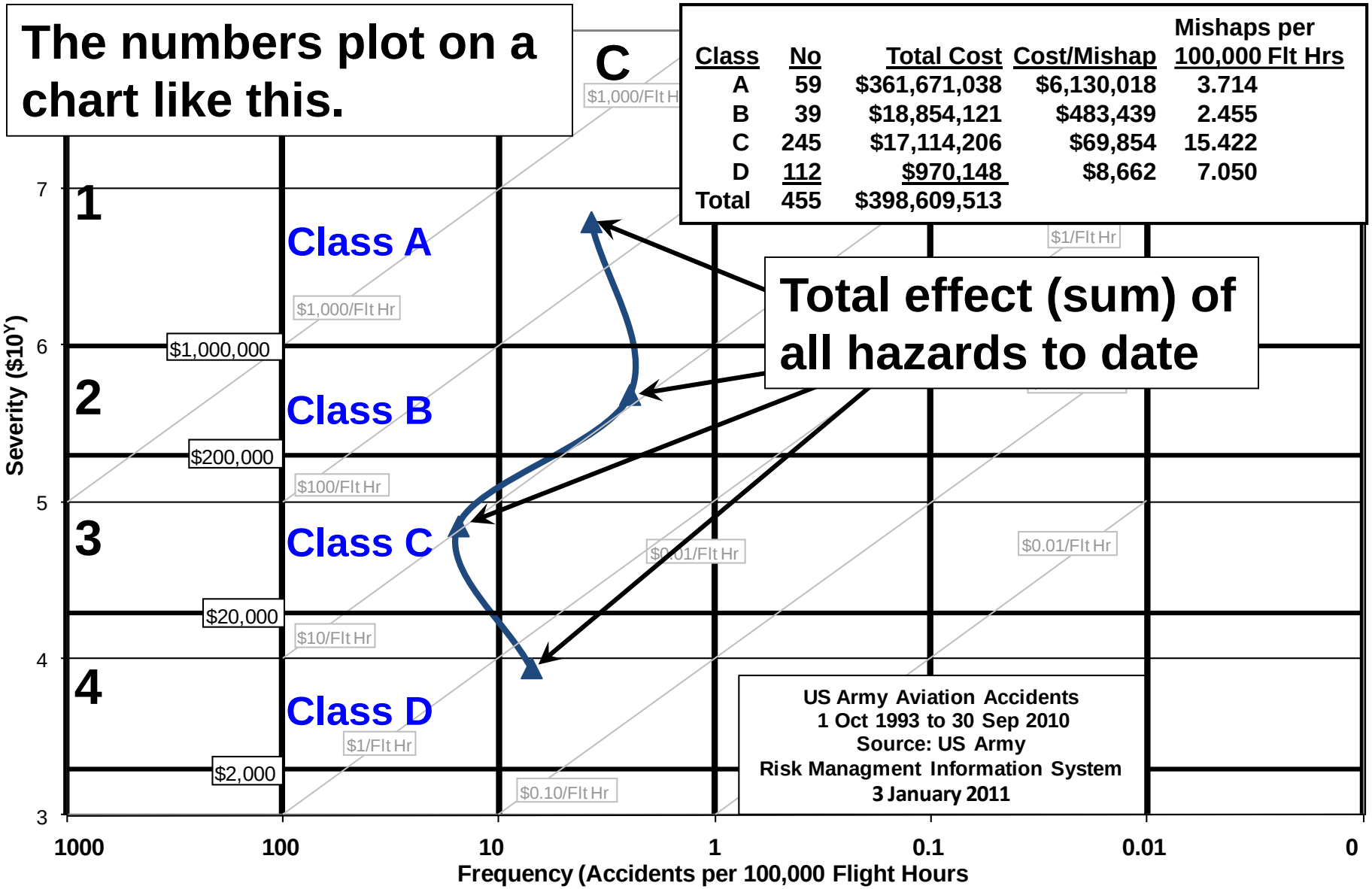
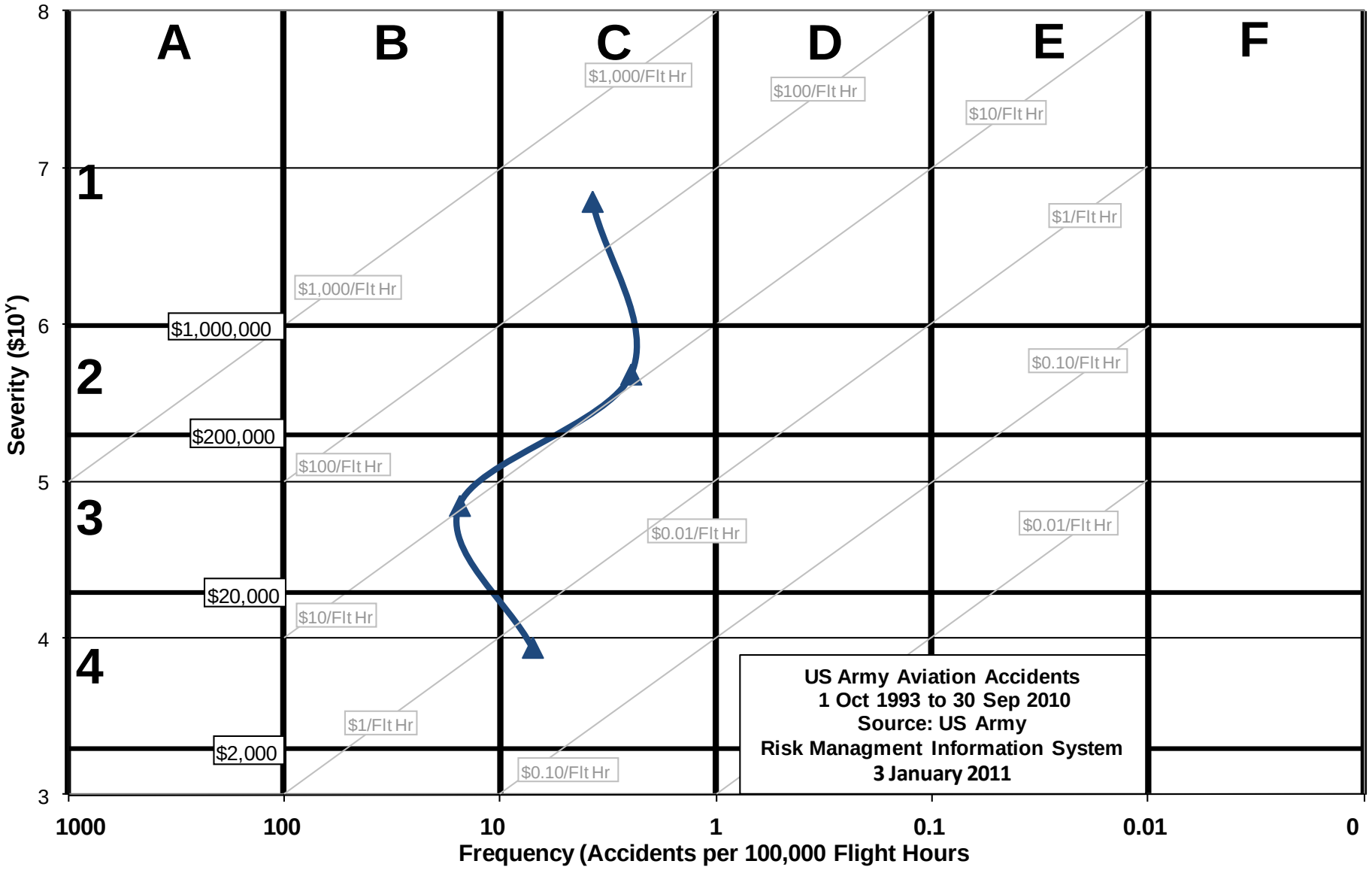
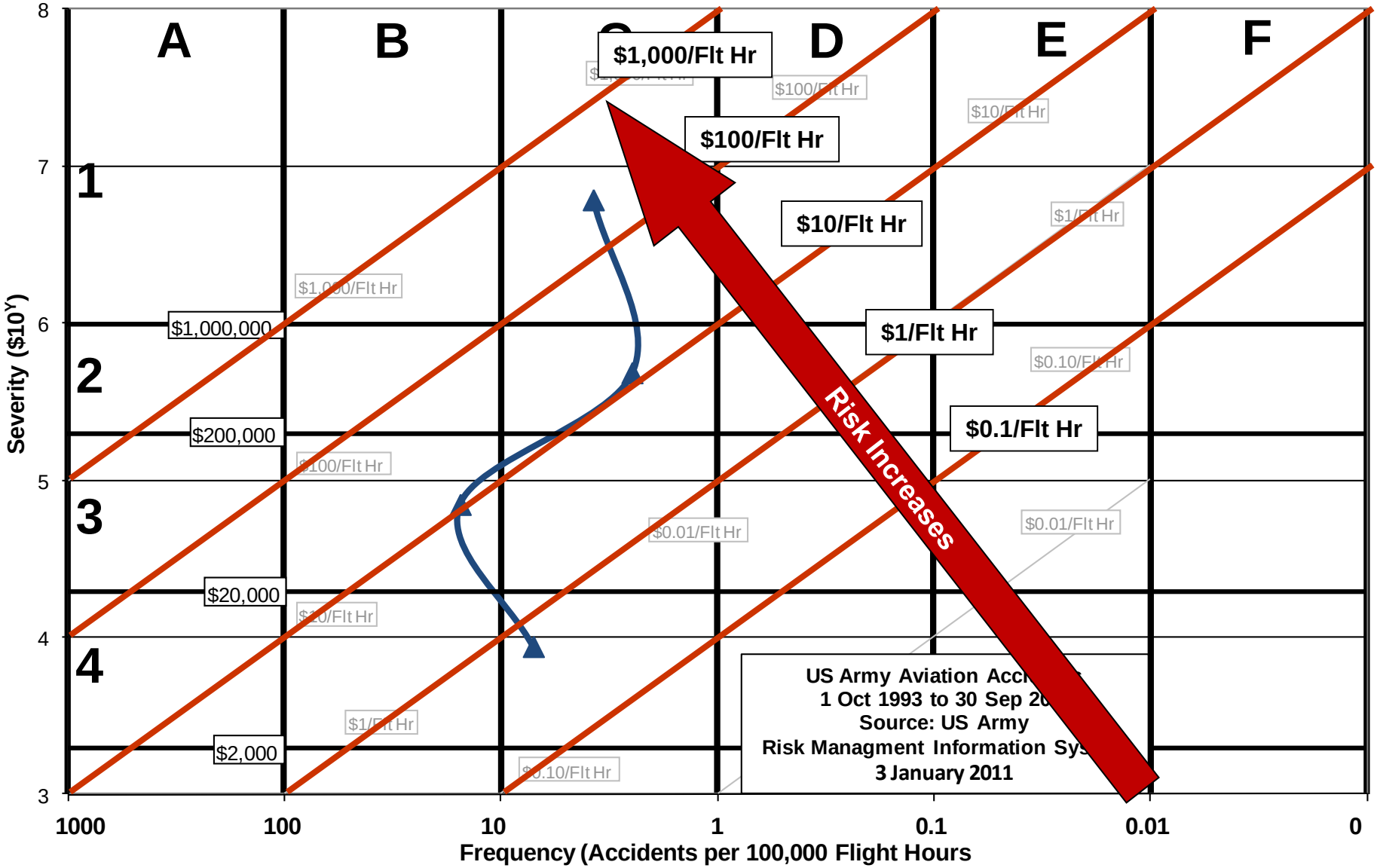
Total	455	$398,609,513		

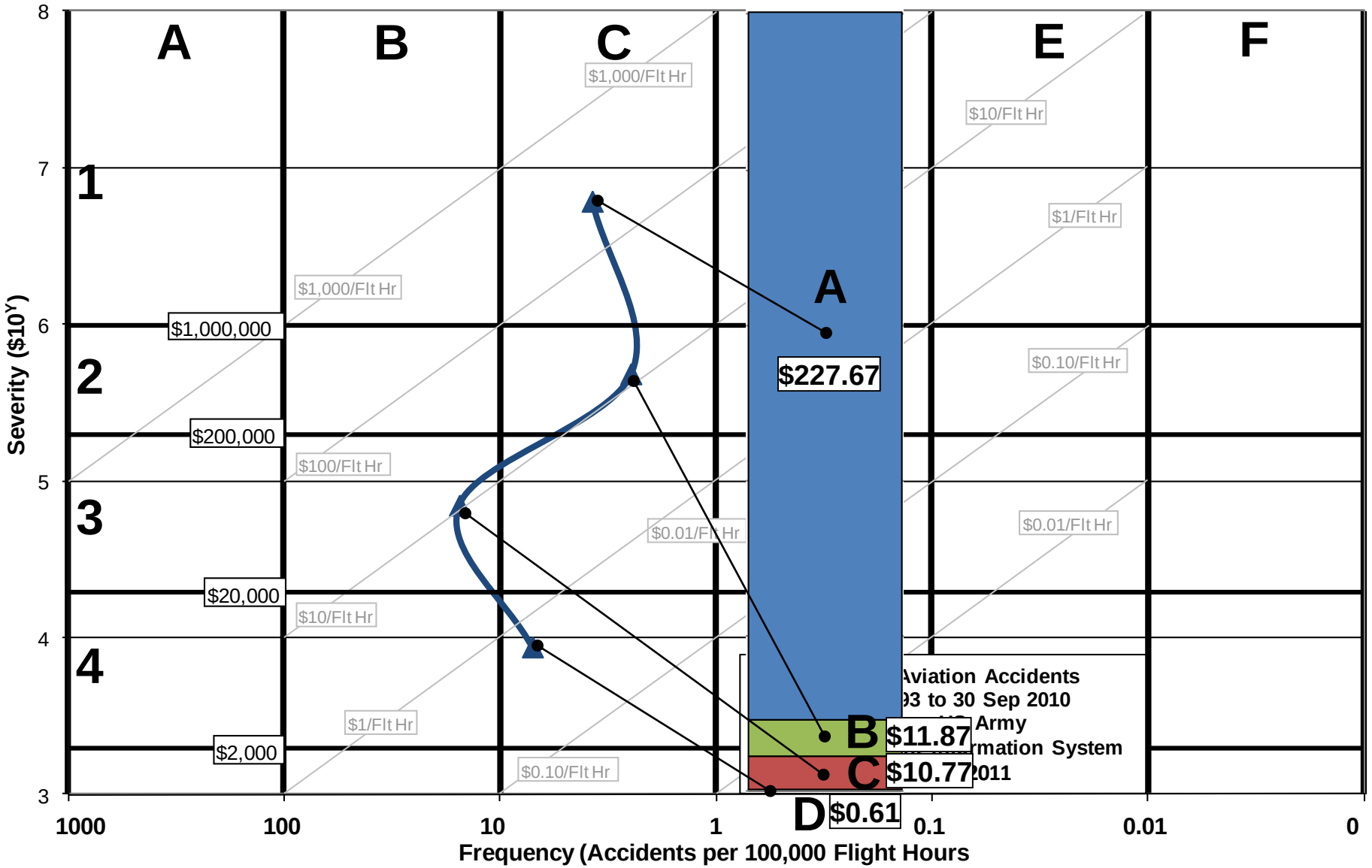



A
B
C
D
E
F
1
2
3
4
$1,000,000
$200,000
$20,000
$2,000
$1,000/Flt Hr
$100/Flt Hr
$10/Flt Hr
$1/Flt Hr
$0.10/Flt Hr
$0.01/Flt Hr
US Army Aviation Accidents
1 Oct 1993 to 30 Sep 2010
Source: US Army
Risk Managment Information System
3 January 2011
Severity ($10^Y)
8
7
6
5
4
3
1000
100
10
1
0.1
0.01
0
Frequency (Accidents per 100,000 Flight Hours

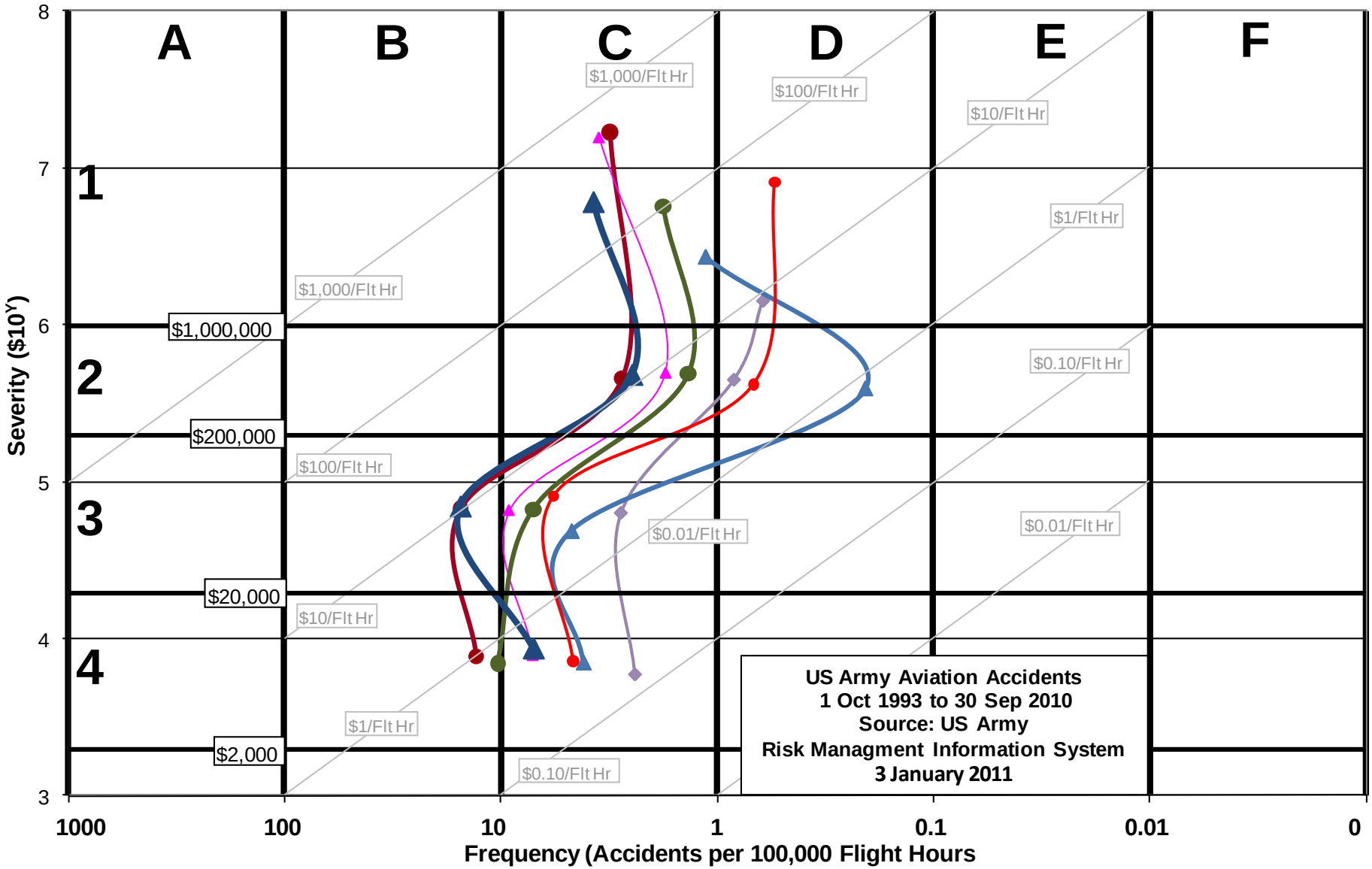
Mishaps


A
B
C
D
E
F
1
2
3
4
$1,000/Flt Hr
$100/Flt Hr
$10/Flt Hr
$1/Flt Hr
$0.1/Flt Hr
$1,000,000
$200,000
$20,000
$2,000
Risk Increases
US Army Aviation Acci
1 Oct 1993 to 30 Sep 20
Source: US Army
Risk Managment Information Sys
3 January 2011
Severity ($10^Y)
8
7
6
5
4
3
1000
100
10
1
0.1
0.01
0
Frequency (Accidents per 100,000 Flight Hours

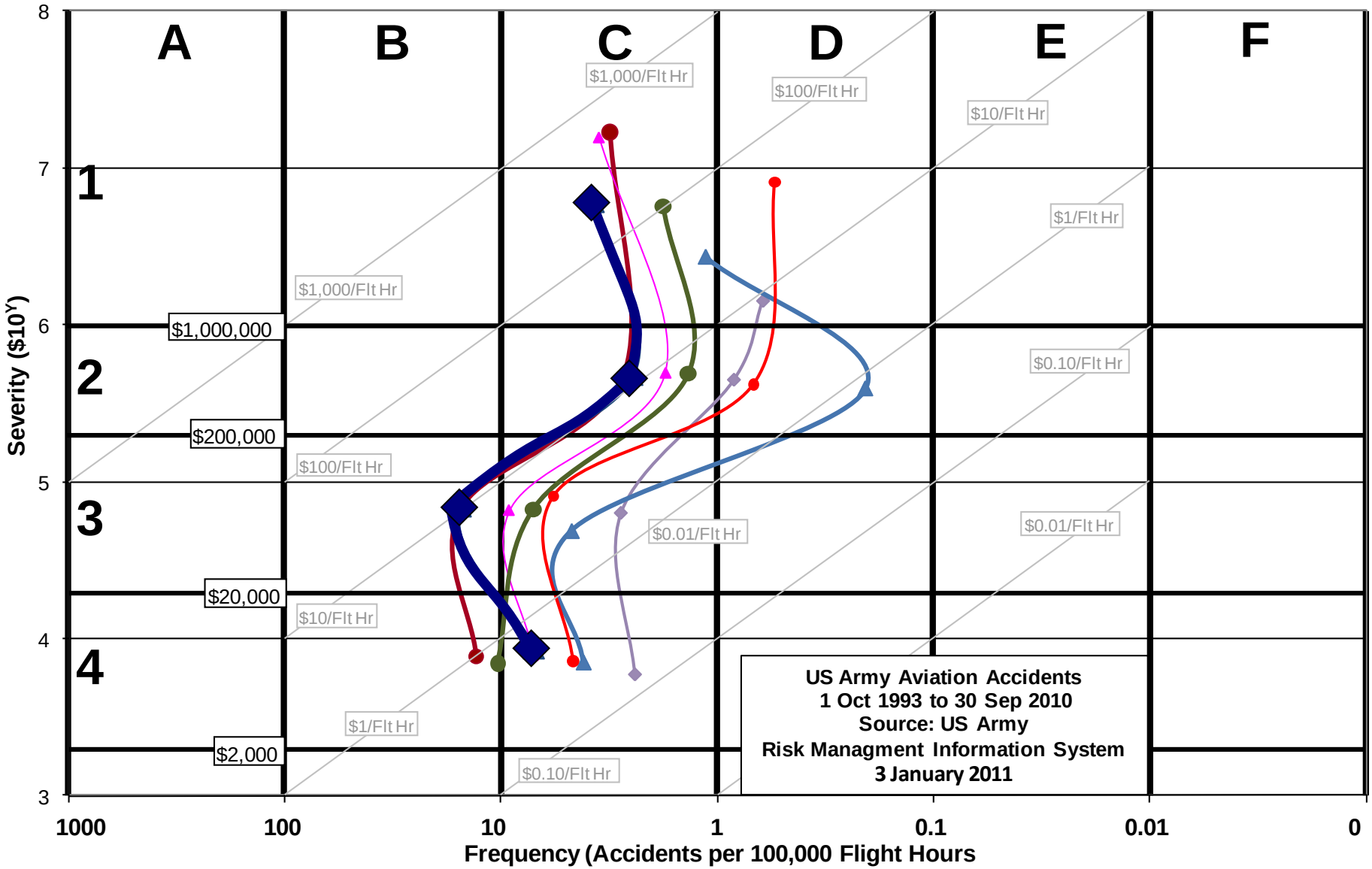
Mishaps


A
B
C
E
F
1
2
3
4
$1,000/Flt Hr
$10/Flt Hr
$1/Flt Hr
$0.10/Flt Hr
$0.01/Flt Hr
$100/Flt Hr
$1,000,000
$200,000
$20,000
$2,000
A
$227.67
B
$11.87
C
$10.77
D
$0.61
Aviation Accidents
93 to 30 Sep 2010
Army
rmation System
2011
Severity ($10^Y)
8
7
6
5
4
3
1000
100
10
1
0.1
0.01
0
Frequency (Accidents per 100,000 Flight Hours

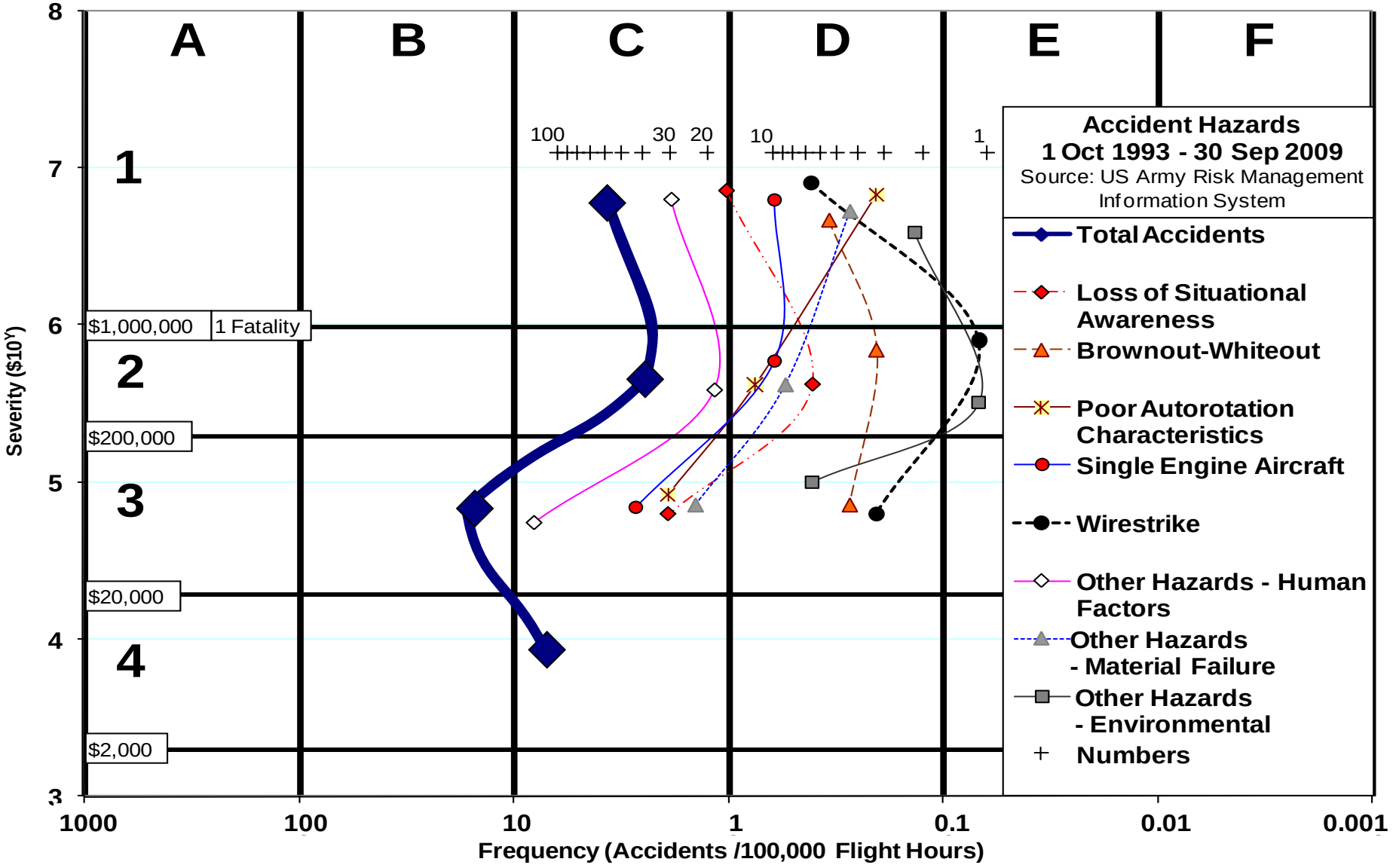
US Army Aviation Mishaps



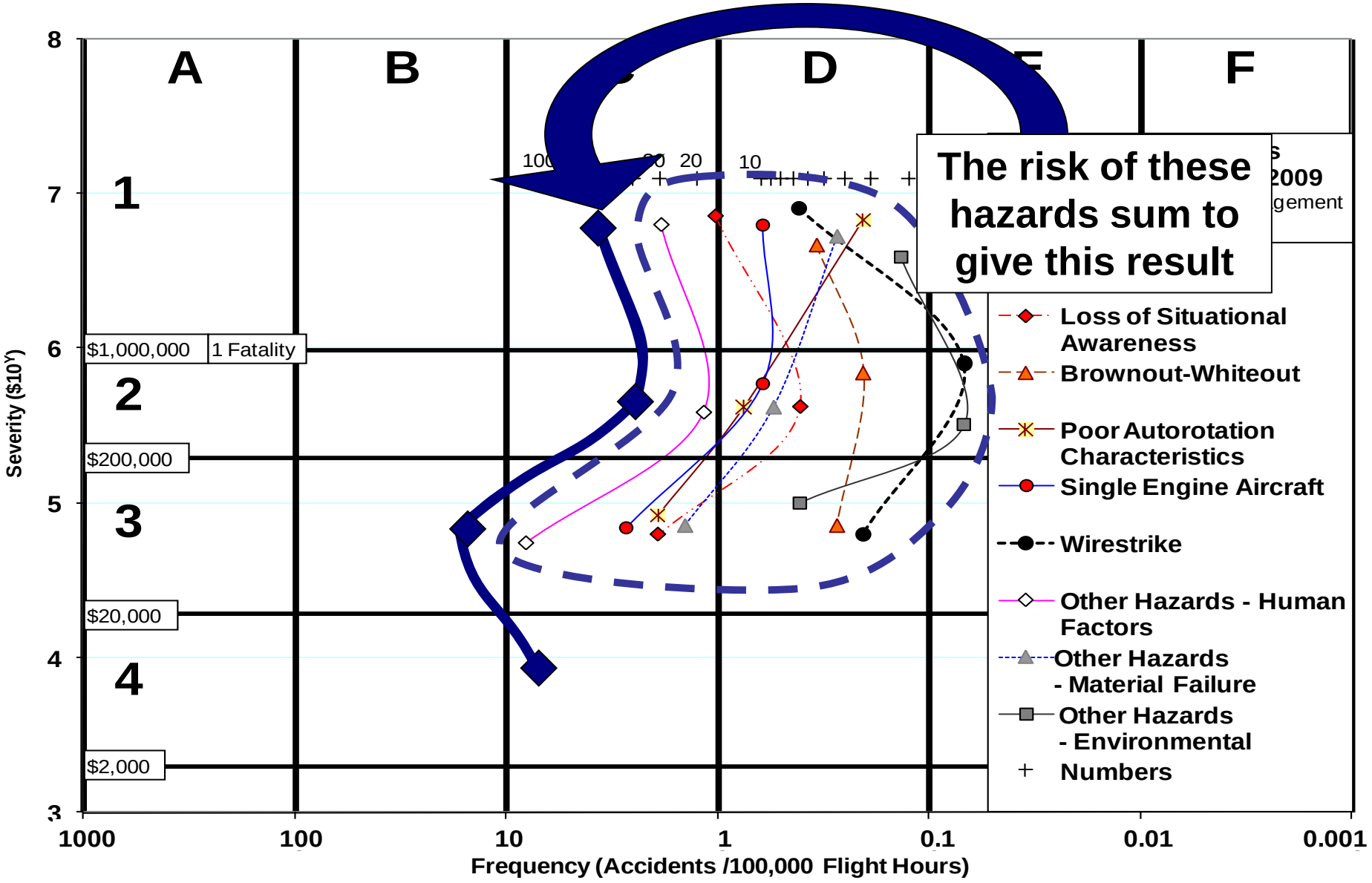
US Army Aviation Mishaps



US Army Aviation Mishaps



US Army Aviation Mishaps



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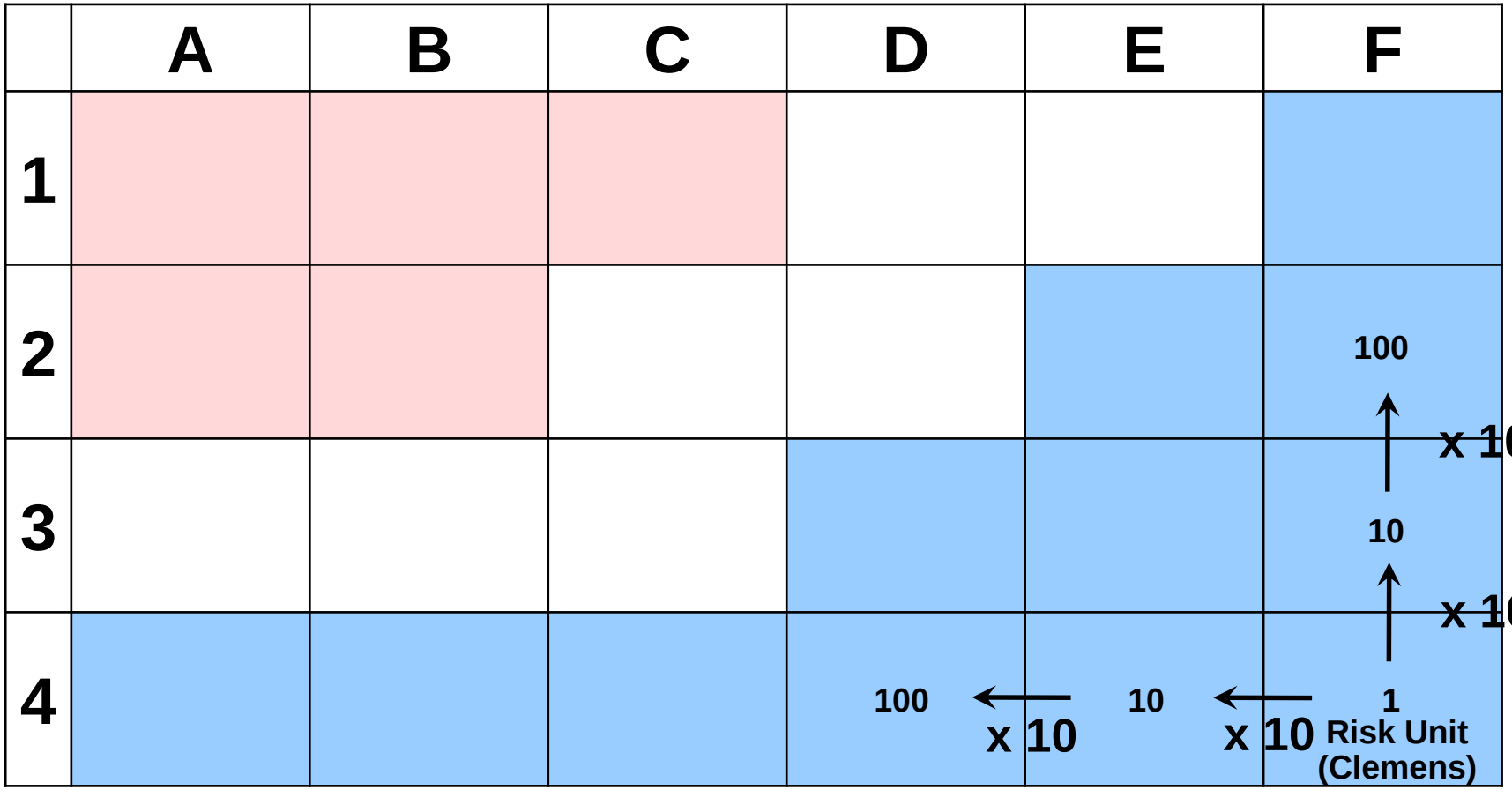
Matrix Relative Risk Values
(Risk Units)(Clemens)



Matrix Relative Risk Values (Clemens)

	A	B	C	D	E	F
1	100,000,000	10,000,000	1,000,000	100,000	10,000	1,000
2	10,000,000	1,000,000	100,000	10,000	1,000	100
3	1,000,000	100,000	10,000	1,000	100	10
4	100,000	10,000	1,000	100	10	1

Helo A Hazard Distribution

	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

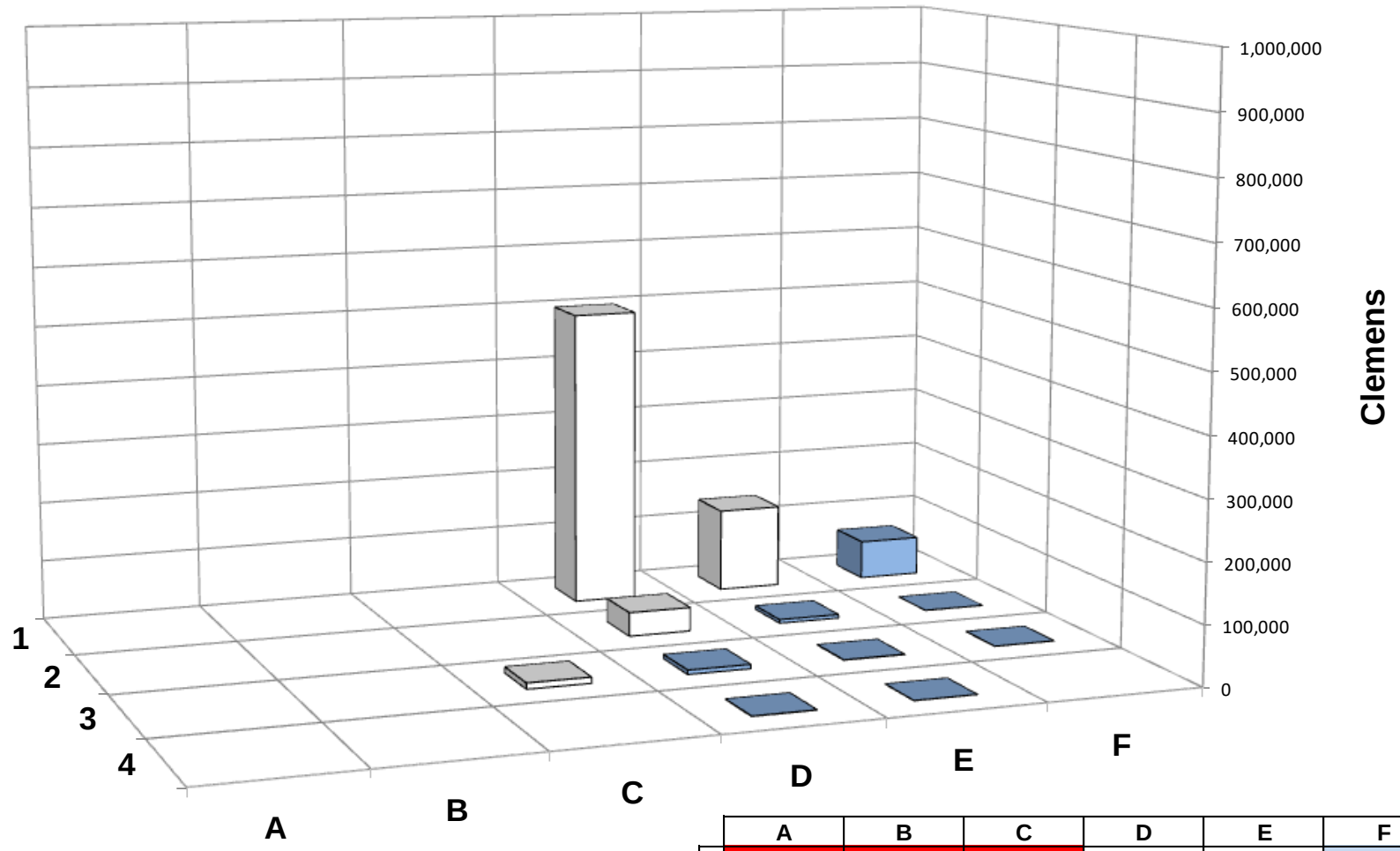
Helo A Matrix
Relative Values (Clemens)

	A	B	C	D	E	F
1				5 x 100,000 = 500,000	14 x 10,000 = 140,000	65 x 1,000 = 65,000
2				4 x 10,000 = 40,000	6 x 1,000 = 6,000	2 x 100 = 200
3			1 x 10,000 = 10,000	7 x 1,000 = 7,000	5 x 100 = 500	4 x 10 = 40
4				2 x 100 = 200	1 x 10 = 10	

Helo A Matrix
Relative Values (Clemens)

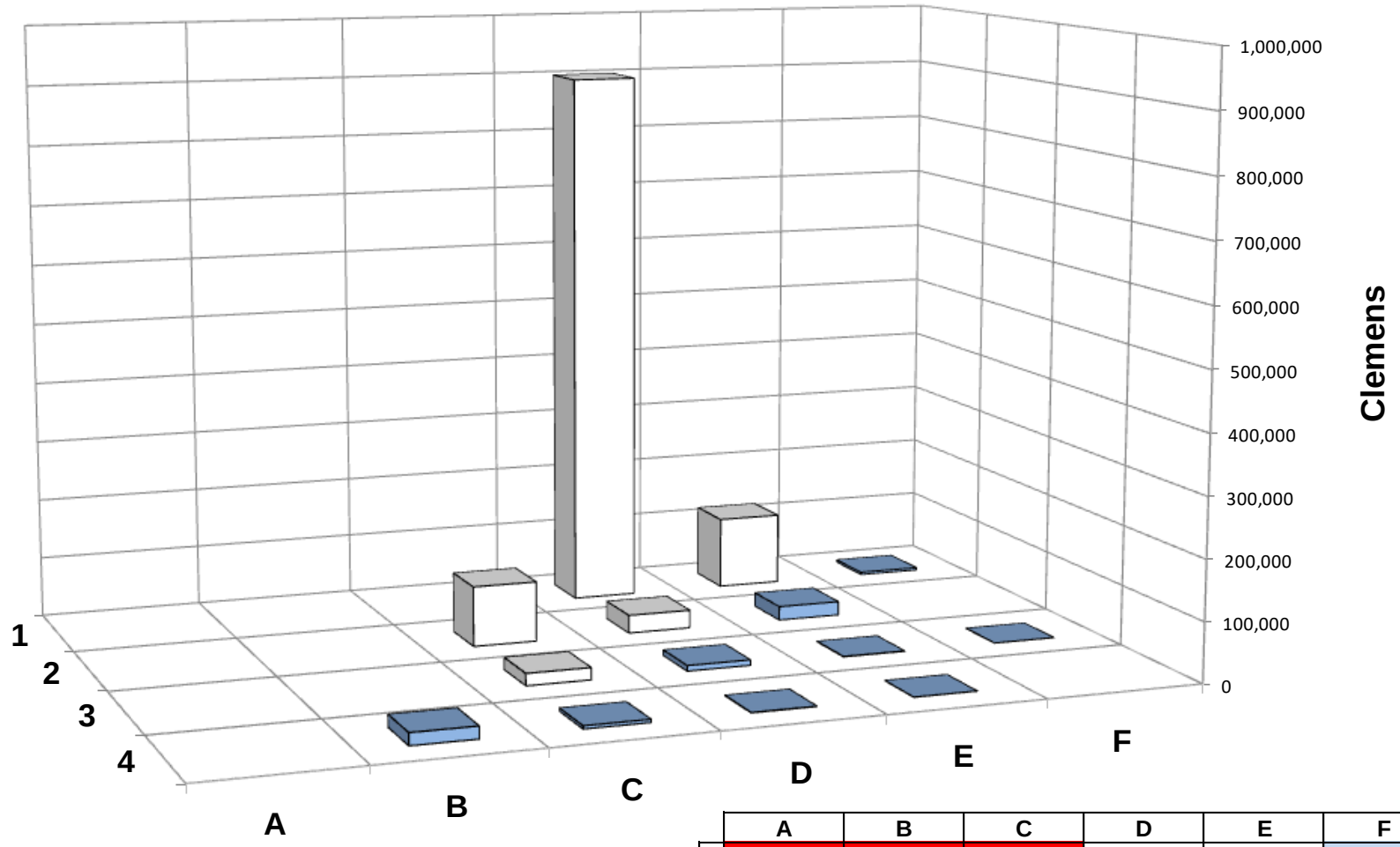
	A	B	C	D	E	F
1				500,000	140,000	65,000
2				40,000	6,000	200
3			10,000	7,000	500	40
4				200	10	

Helicopter A



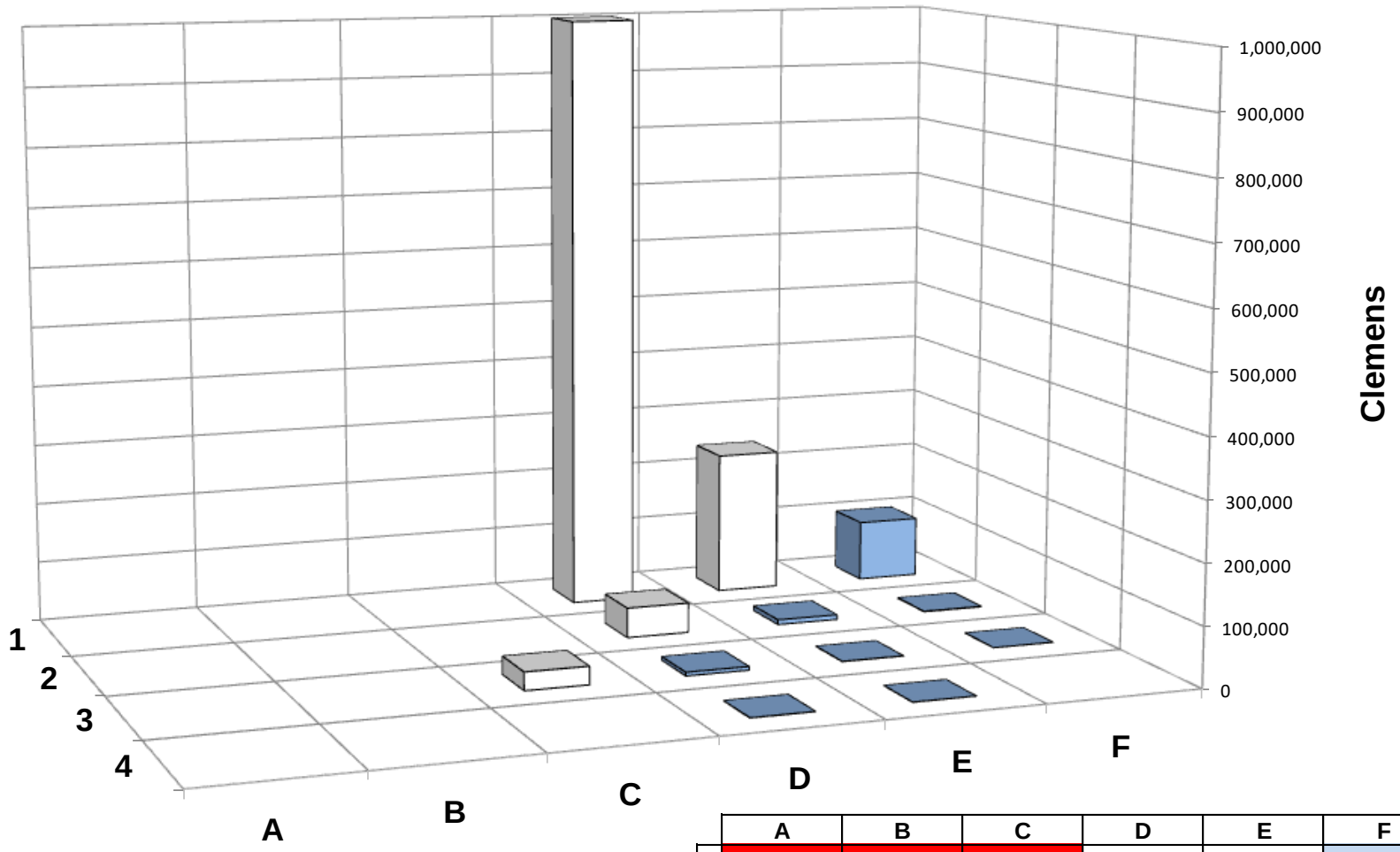
	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Helicopter B



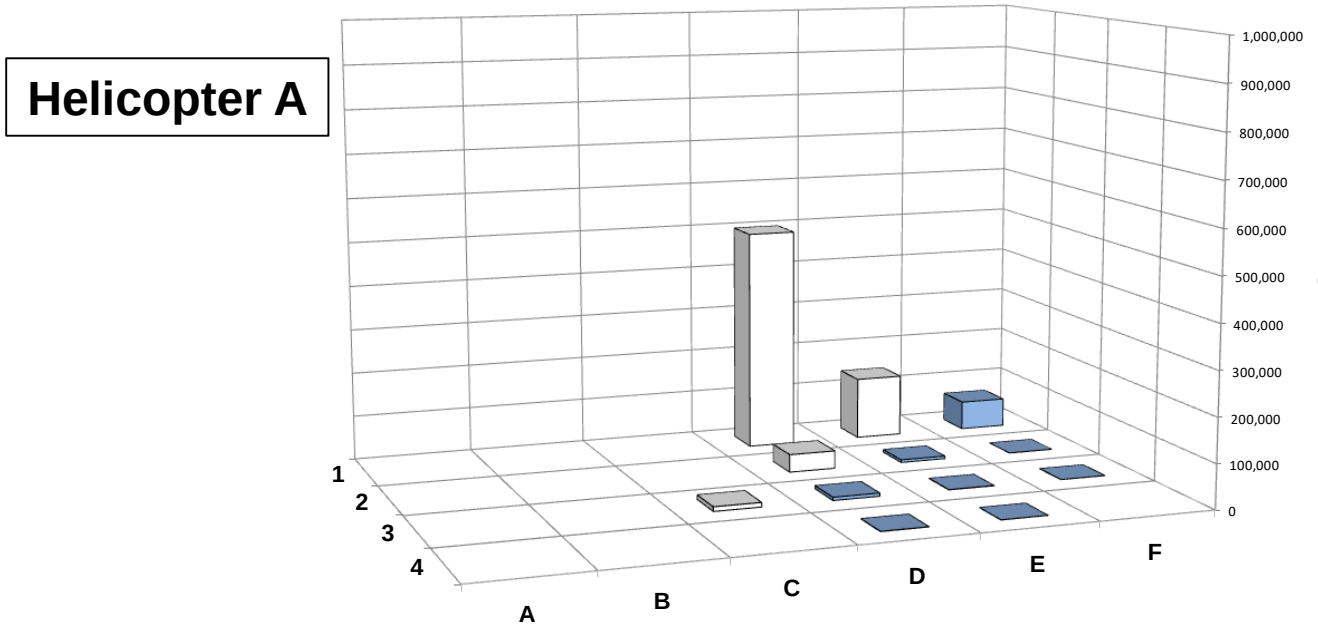
	A	B	C	D	E	F
1				9	12	4
2			1	3	23	
3			2	9	6	1
4		2	5	5	2	

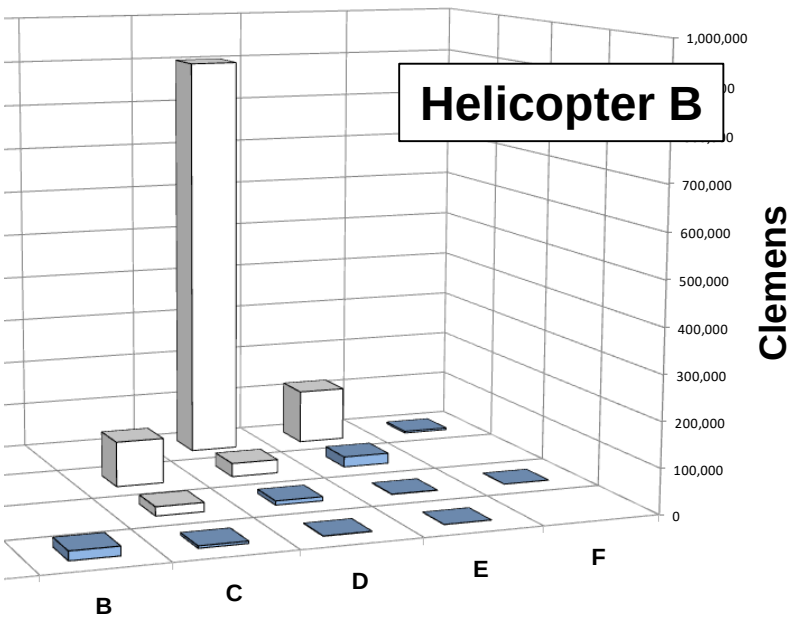
Helicopter C

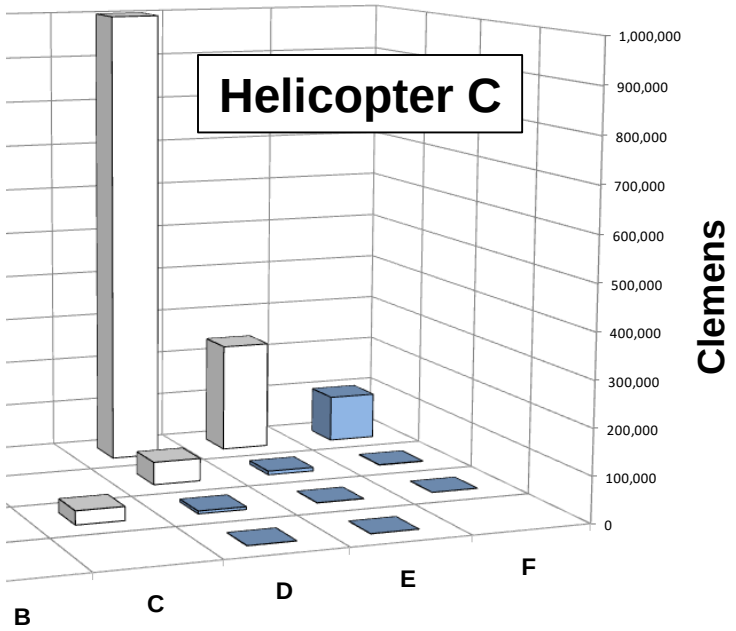


	A	B	C	D	E	F
1				10	24	102
2				5	8	8
3			3	6	3	2
4				1	1	

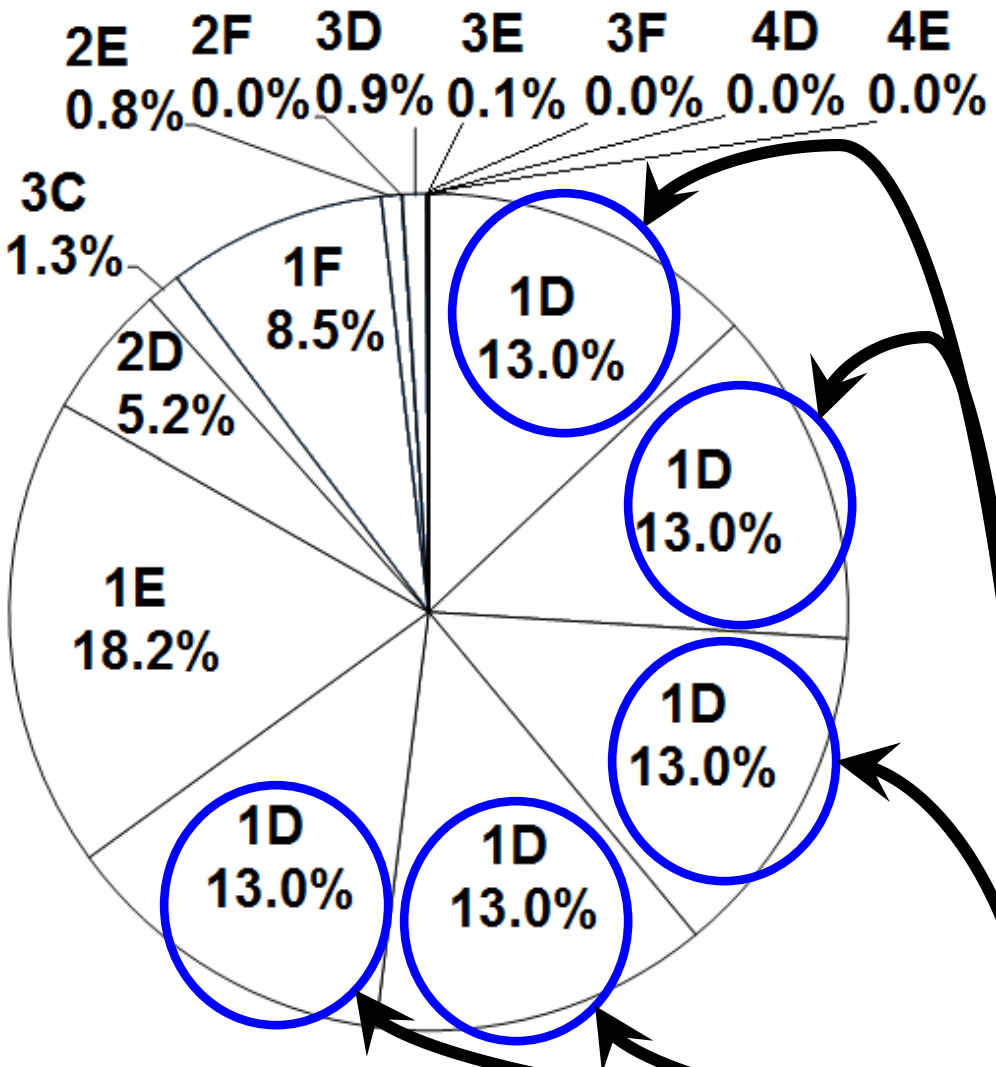
Side by Side Relative Risk by RAC





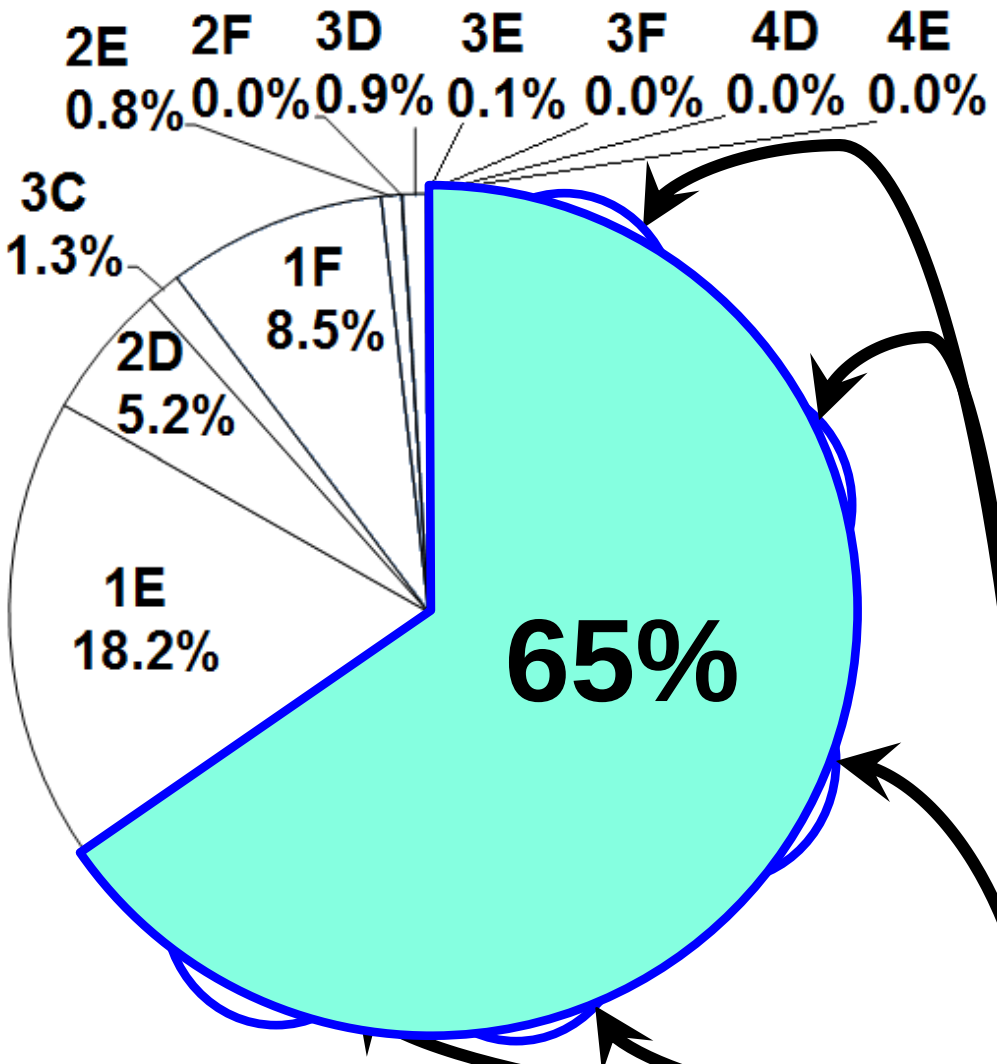


Risk Pie Chart by RAC



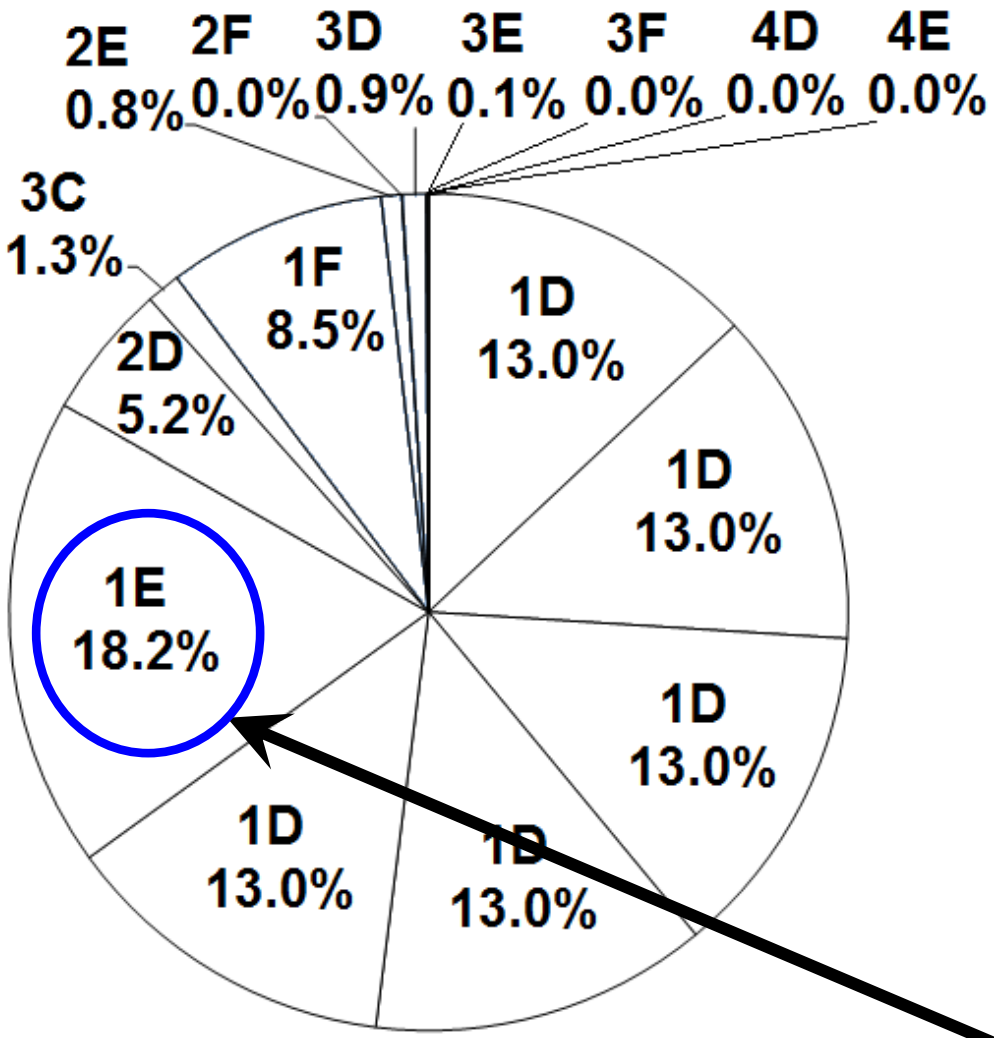
	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Risk Pie Chart by RAC



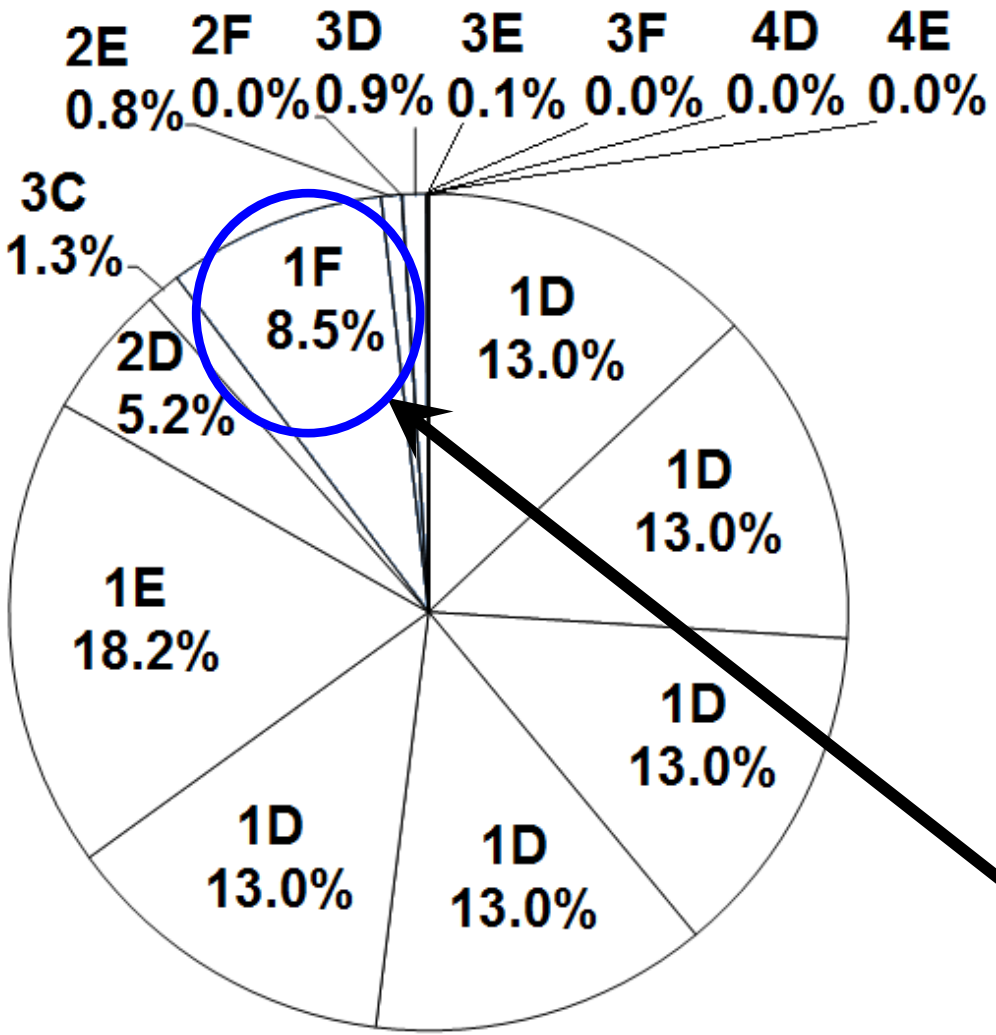
	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Risk Pie Chart by RAC



	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Risk Pie Chart by RAC



	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Topics for this Tutorial

- Purpose of a Hazard Risk Matrix
- Understanding the Attributes of a well-designed risk assessment matrix
- How to Assign a Risk Assessment Code
- Understanding Probability
- Building an Expanded Matrix
- Plotting Accidents on a Matrix
- Using Relative Risk Values
- **Building Hazard Risk Profiles**

Hazard Risk Profile

	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

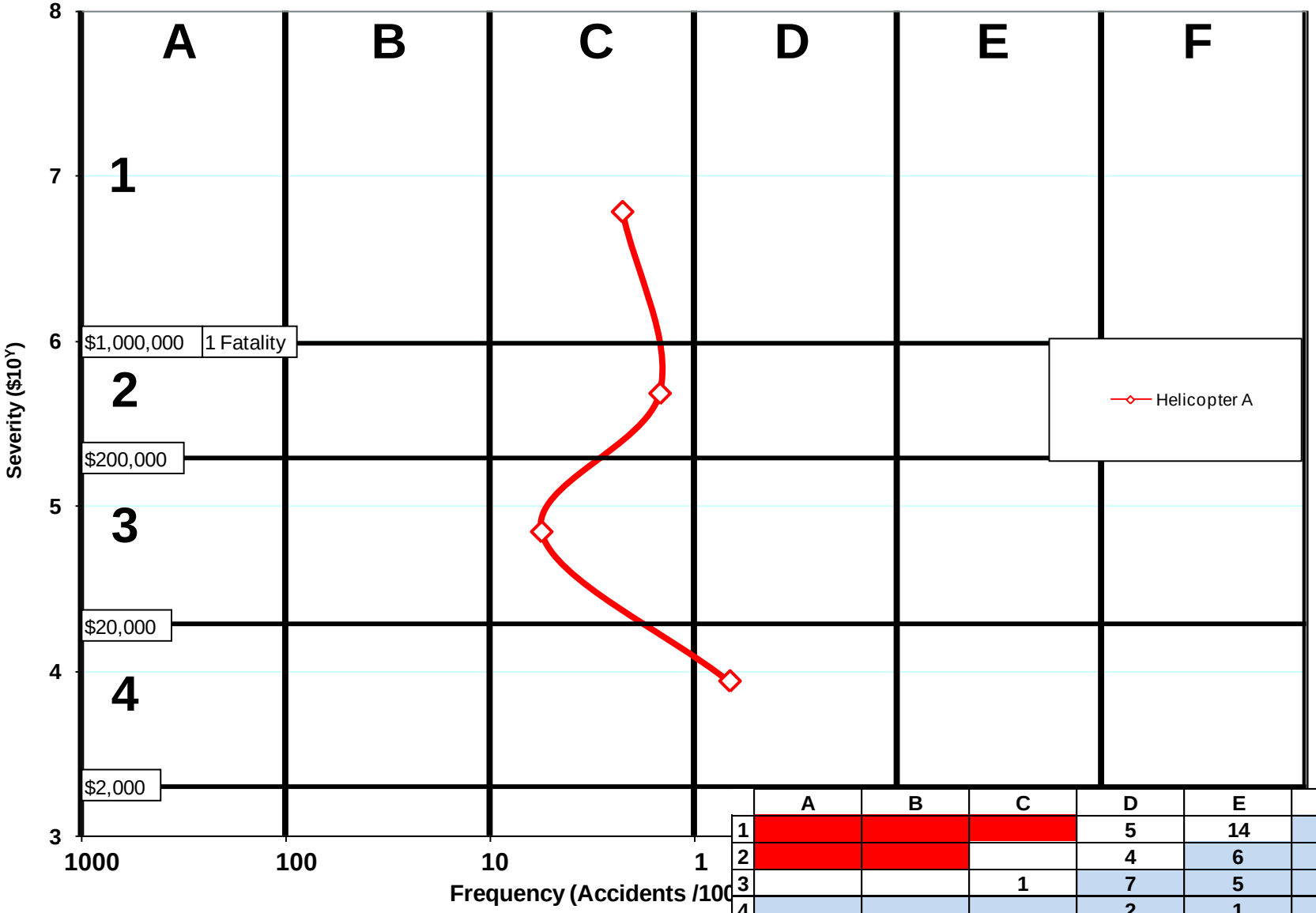
Hazard Risk Profile

		3.16E-04	3.16E-05	3.16E-06	3.16E-07	3.16E-08
	A	B	C	D	E	F
1					14	65
2					6	2
3			1		5	4
4					1	

Hazard Risk Profile

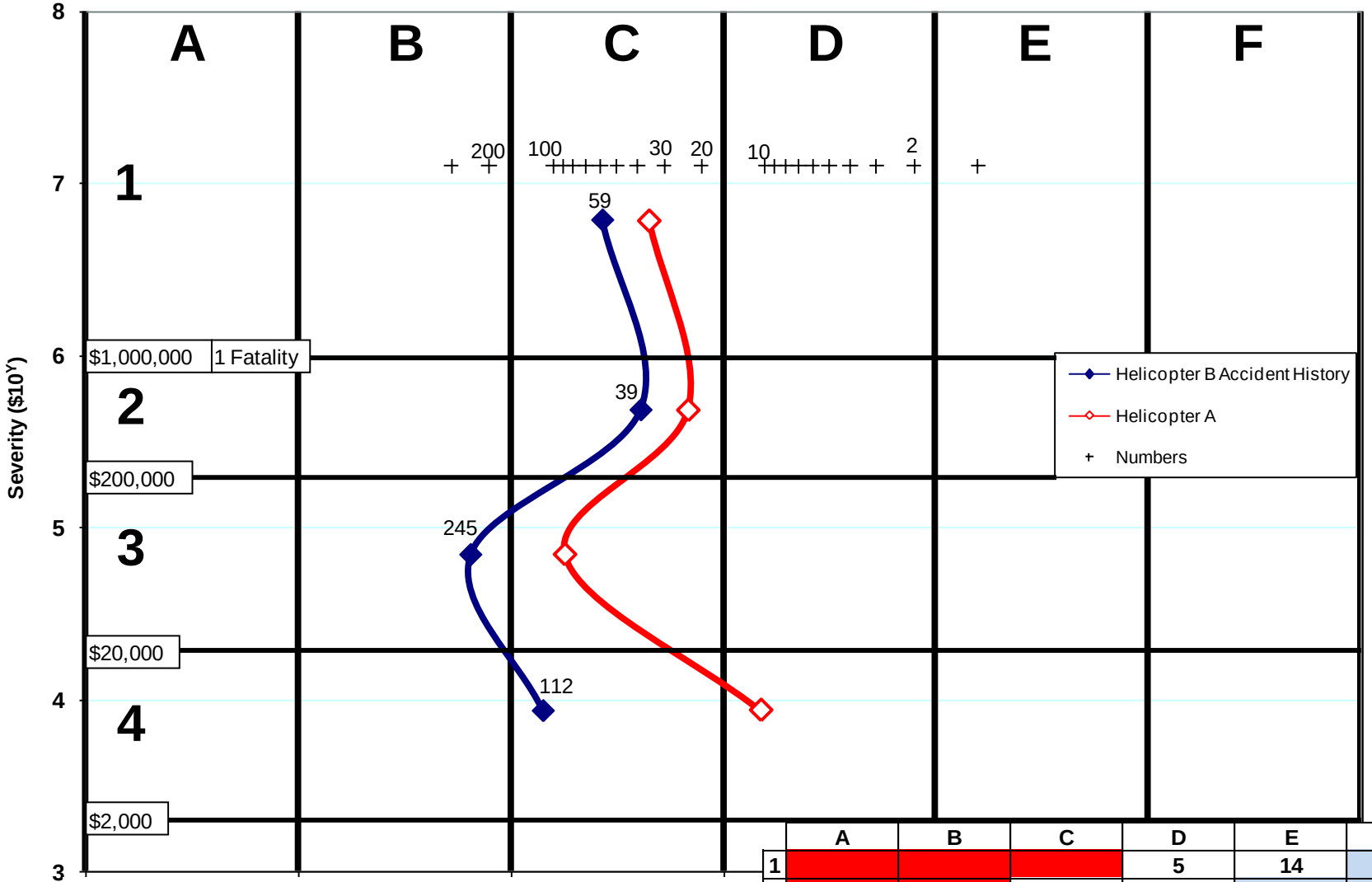
		3.16E-04	3.16E-05	3.16E-06	3.16E-07	3.16E-08
	A	B	C	D	E	F
1	2.23E-05	Sum		5 x 3.16E-06 = 1.58E-05	14 x 3.16E-07 = 4.43E-06	65 x 3.16E-08 = 2.06E-06
2	1.46E-05	Sum		4 x 3.16E-06 = 1.26E-05	6 x 3.16E-07 = 1.90E-06	2 x 3.16E-08 = 6.32E-08
3	5.55E-05	Sum	1 x 3.16E-05 = 3.16E-05	7 x 3.16E-06 = 2.21E-05	5 x 3.16E-07 = 1.58E-06	4 x 3.16E-08 = 1.26E-07
4	6.64E-06	Sum		2 x 3.16E-06 = 6.32E-06	1 x 3.16E-07 = 3.16E-07	

Hazard Risk Profile



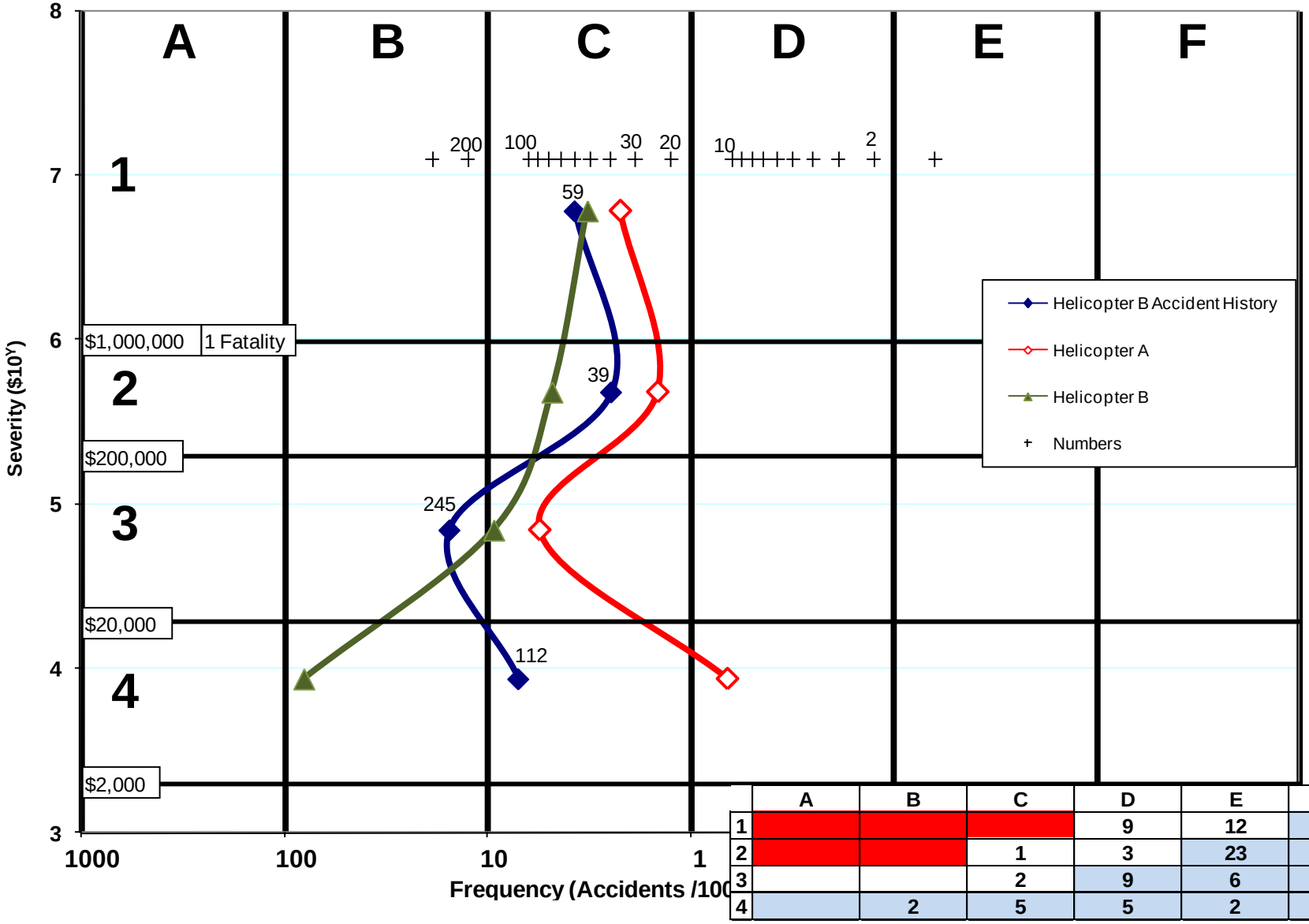
	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Comparing Hazard Profile to Accident History



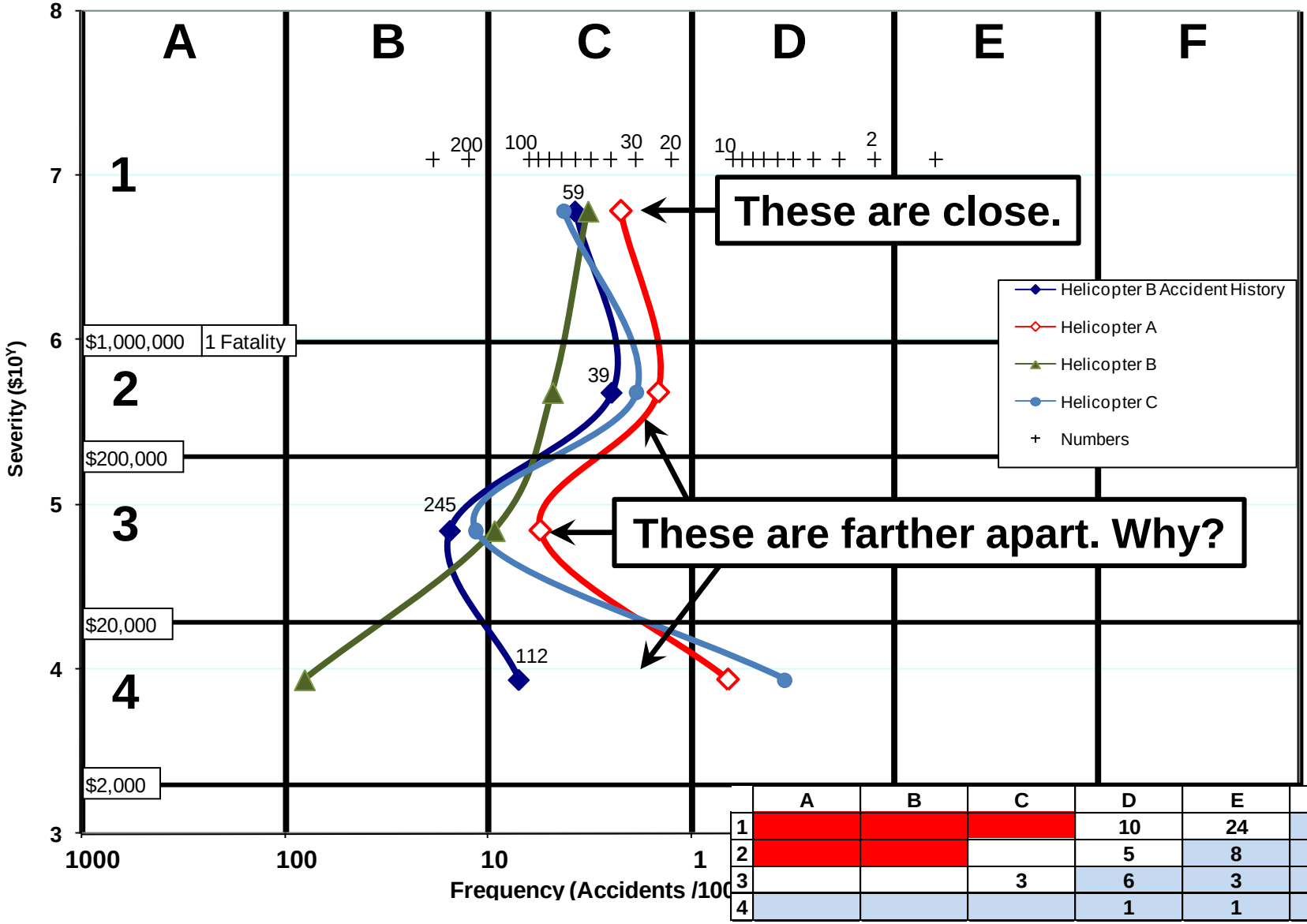
	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Comparing Hazard Profile to Accident History



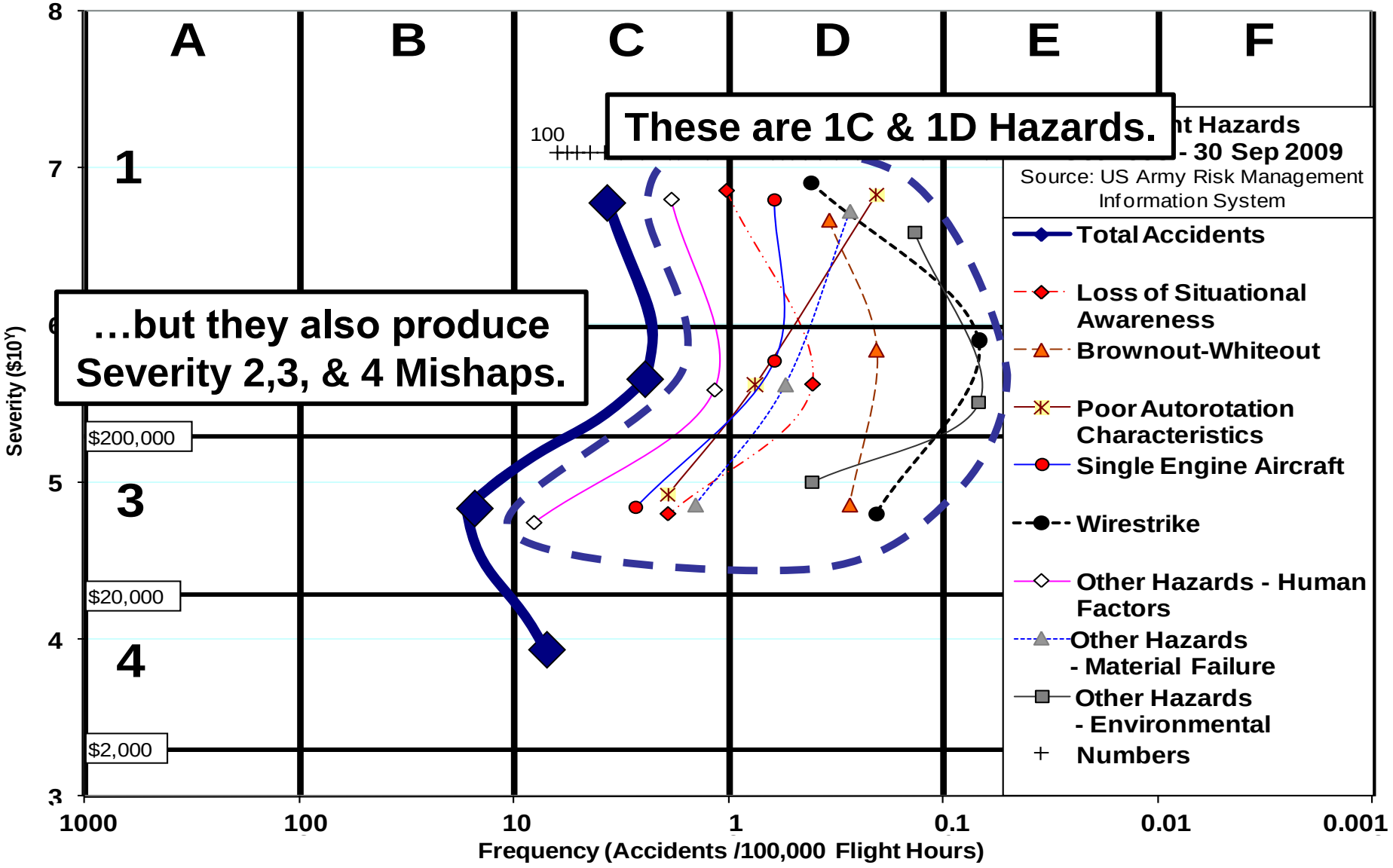
	A	B	C	D	E	F
1				9	12	4
2			1	3	23	
3			2	9	6	1
4		2	5	5	2	

Comparing Hazard Profile to Accident History



	A	B	C	D	E	F
1				10	24	102
2				5	8	8
3			3	6	3	2
4				1	1	

US Army Aviation Mishaps



Missile Risk Matrix

RISK ASSESSMENT MATRIX				
SEVERITY / PROBABILITY *	Catastrophic (1) — 1 Fatal / $10M	Critical (2) — $1M	Marginal (3) — $100K	Negligible (4)
Frequent (A)	High	High	Serious	Medium
Probable (B) 10^{-1}	High	High	Serious	Medium
Occasional (C) 10^{-2}	High	Serious	Medium	Low
Remote (D) 10^{-3}	Serious	Medium	Medium	Low
Improbable (E) 10^{-6}	Medium	Medium	Medium	Low
Eliminated (F)	Eliminated			

Missile Hazard Risk Matrix

RISK ASSESSMENT MATRIX				
SEVERITY / PROBABILITY *	Catastrophic (1) — 1 Fatal / $10M	Critical (2) — $1M	Marginal (3) — $100K	Negligible (4)
Frequent (A)	High	High	Serious	Medium
Probable (B) — 1/10	High	High	Serious	Medium
Occasional (C) — 1/100	High	Serious	Medium	Low
Remote (D) — 1/1,000	Serious	Medium	Medium	Low
Improbable (E) — 1/1,000,000	Medium	Medium	Medium	Low
Eliminated (F)	Eliminated			

Back of the Envelope Calculation

40,000 Shishkebab Missiles

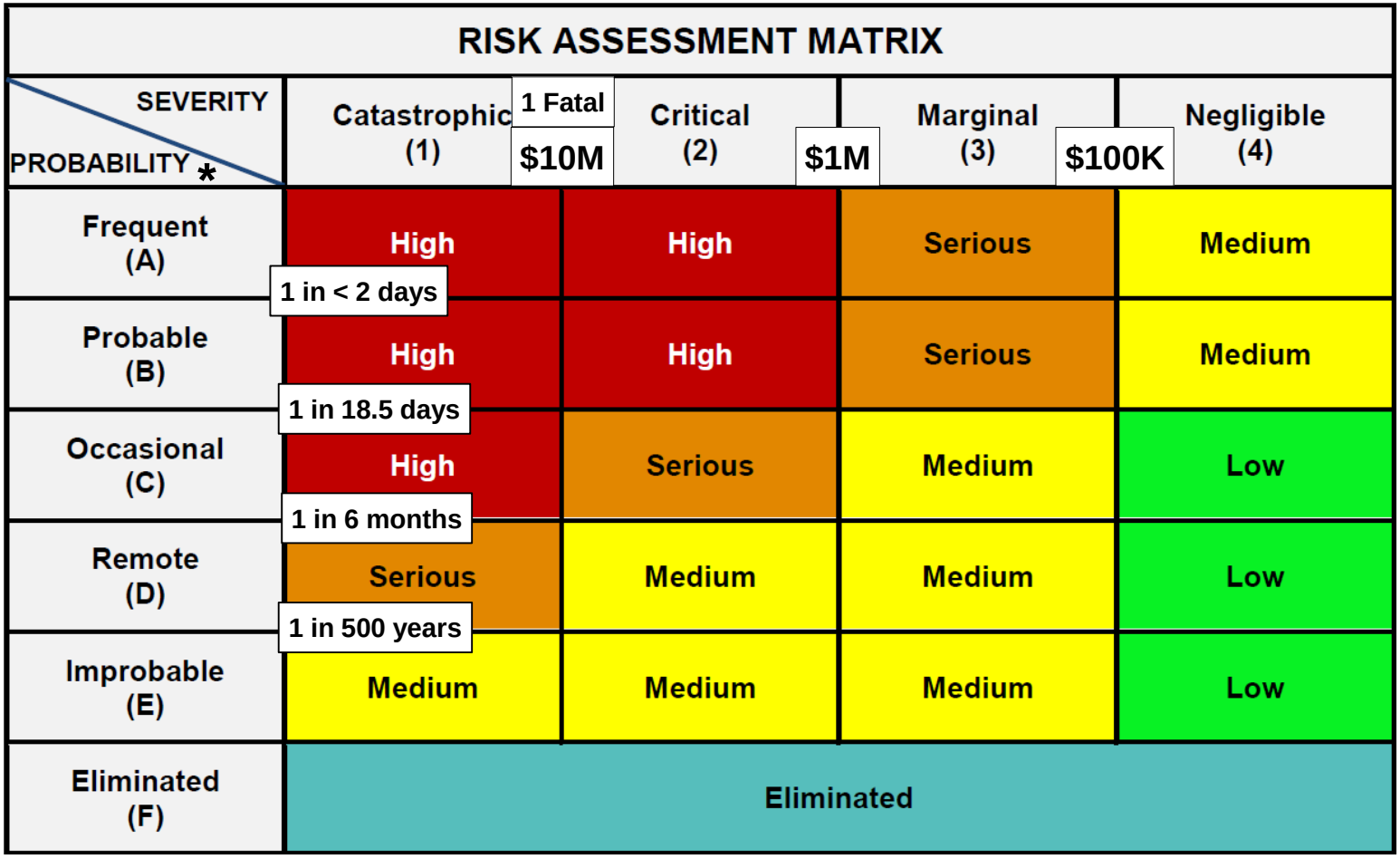
Delivered over 20 years

Assume all fired

1 accident in 1,000,000 firings

$$\frac{\textbf{1 accident}}{\textbf{1,000,000 }\sout{\textbf{firings}}} \times \frac{\textbf{40,000 }\sout{\textbf{firings}}}{\textbf{20 years}} = \frac{\textbf{1 accident}}{\textbf{500 years}}$$

Missile Hazard Risk Matrix



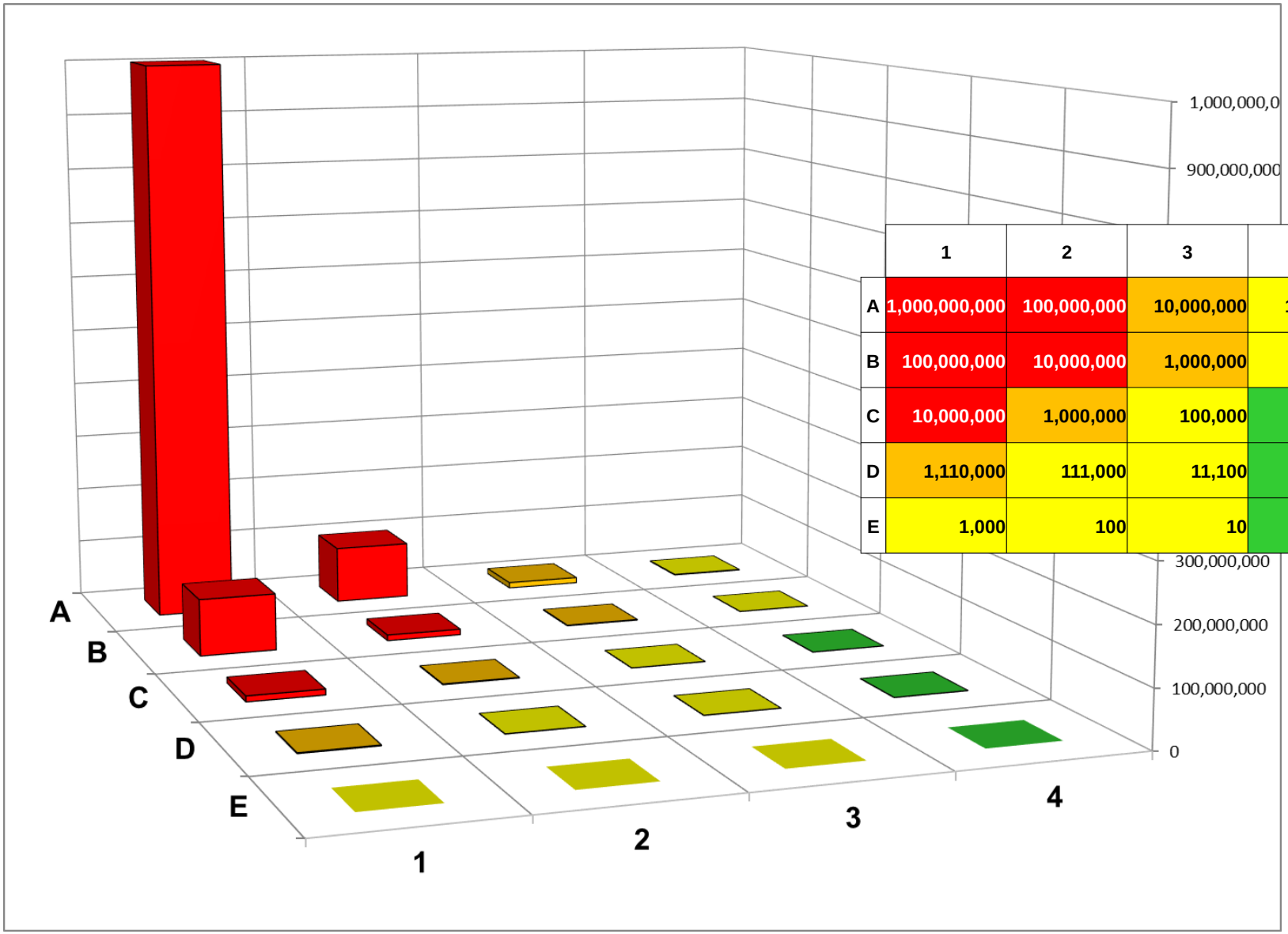
Matrix Relative Risk Values

	1	2	3	4
A	1,000,000,000	100,000,000	10,000,000	1,000,000
	10^{-1}			
B	100,000,000	10,000,000	1,000,000	100,000
	10^{-2}			
C	10,000,000	1,000,000	100,000	10,000
	10^{-3}			
D	1,000,000	100,000	10,000	1,000
	10^{-4}			
	100,000	10,000	1,000	100
	10^{-5}			
	10,000	1,000	100	10
	10^{-6}			
E	1,000	100	10	1

Matrix Relative Risk Values

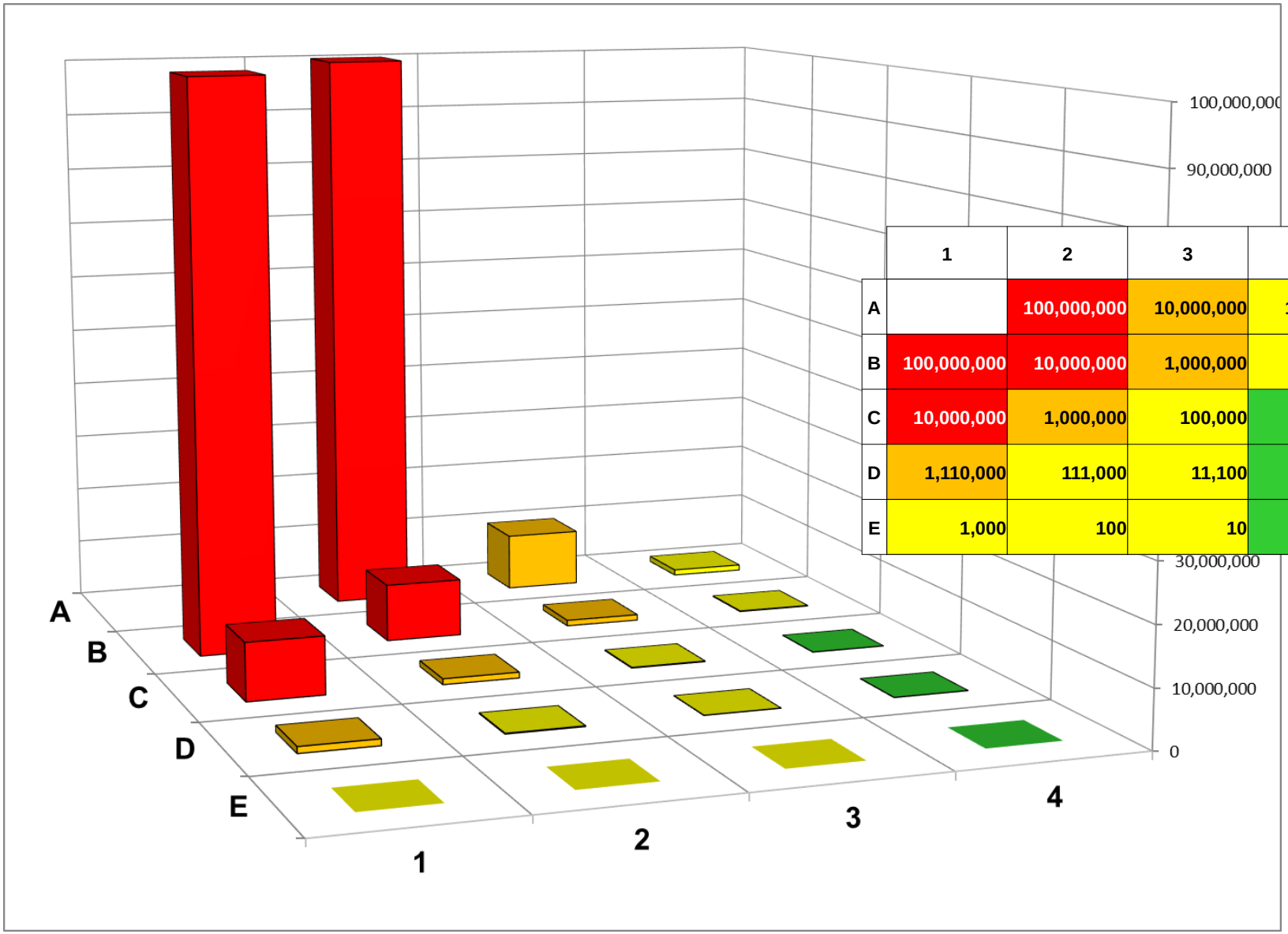
	1	2	3	4
A	1,000,000,000	100,000,000	10,000,000	1,000,000
	10^{-1}			
B	100,000,000	10,000,000	1,000,000	100,000
	10^{-2}			
C	10,000,000	1,000,000	100,000	10,000
	10^{-3}			
D	1,110,000	111,000	11,100	1,110
	10^{-6}			
E	1,000	100	10	1

Matrix Relative Risk Values



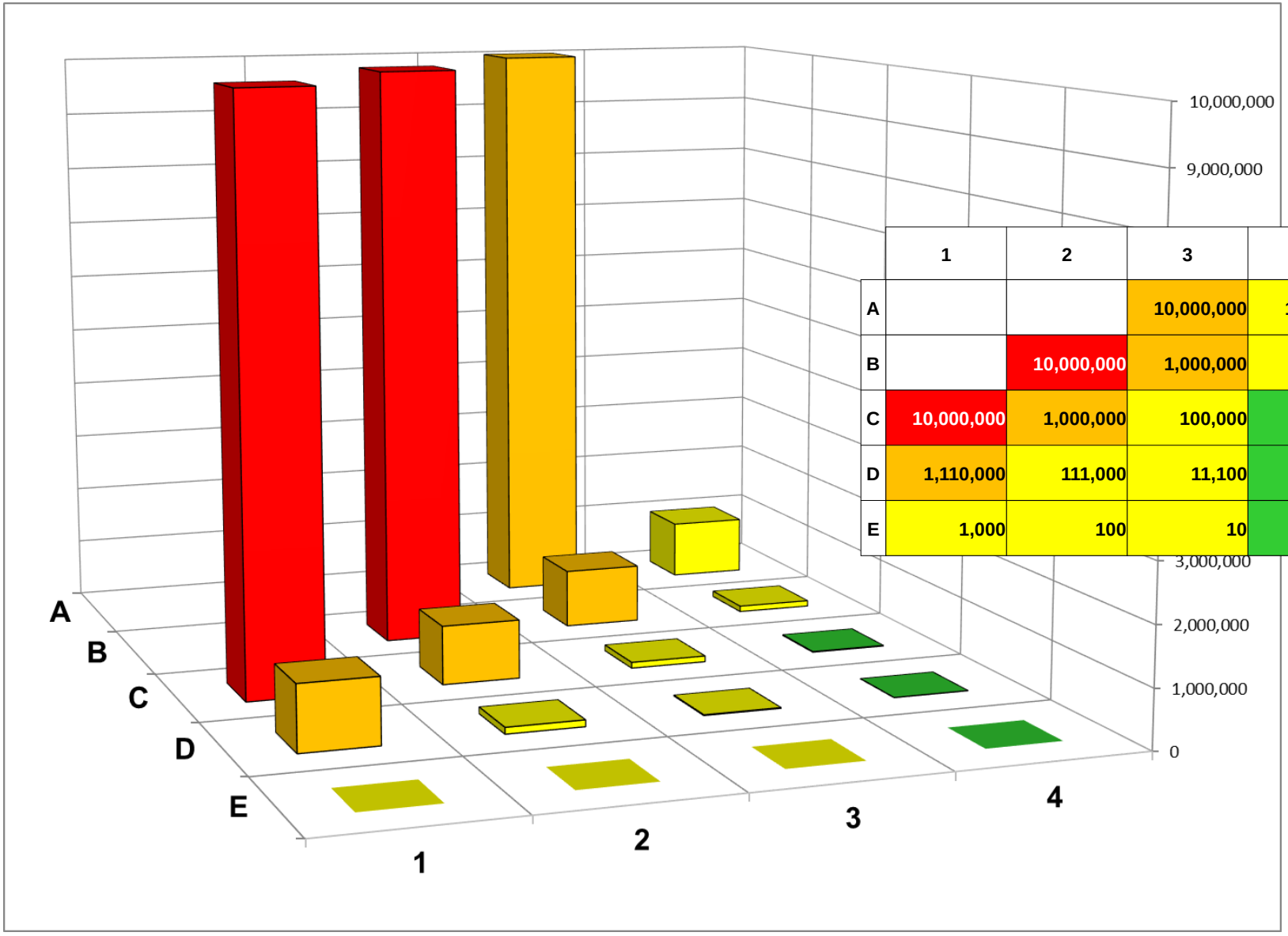
	1	2	3	4
A	1,000,000,000	100,000,000	10,000,000	1,000,000
B	100,000,000	10,000,000	1,000,000	100,000
C	10,000,000	1,000,000	100,000	10,000
D	1,110,000	111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values



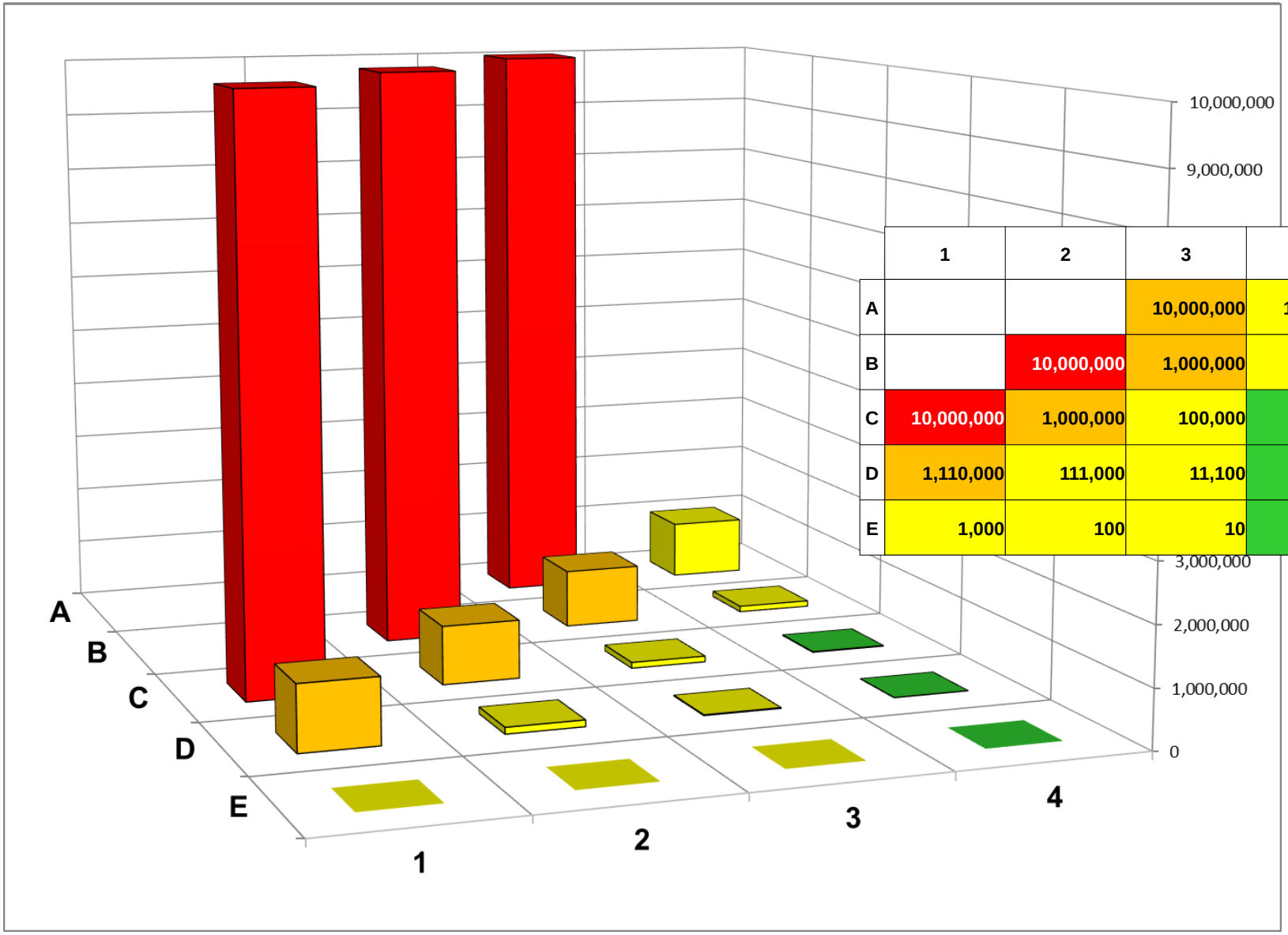
	1	2	3	4
A		100,000,000	10,000,000	1,000,000
B	100,000,000	10,000,000	1,000,000	100,000
C	10,000,000	1,000,000	100,000	10,000
D	1,110,000	111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values



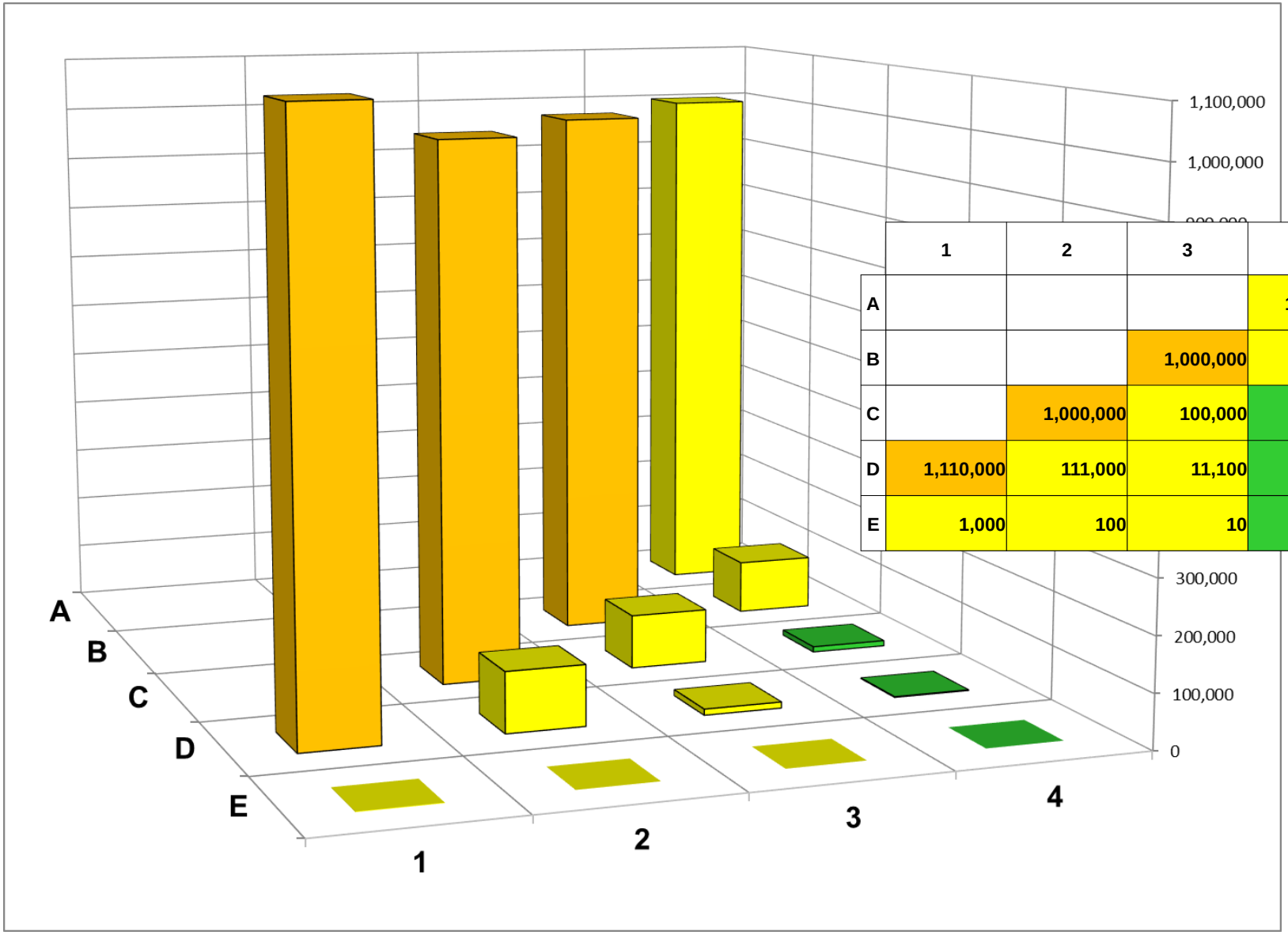
	1	2	3	4
A			10,000,000	1,000,000
B		10,000,000	1,000,000	100,000
C	10,000,000	1,000,000	100,000	10,000
D	1,110,000	111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values



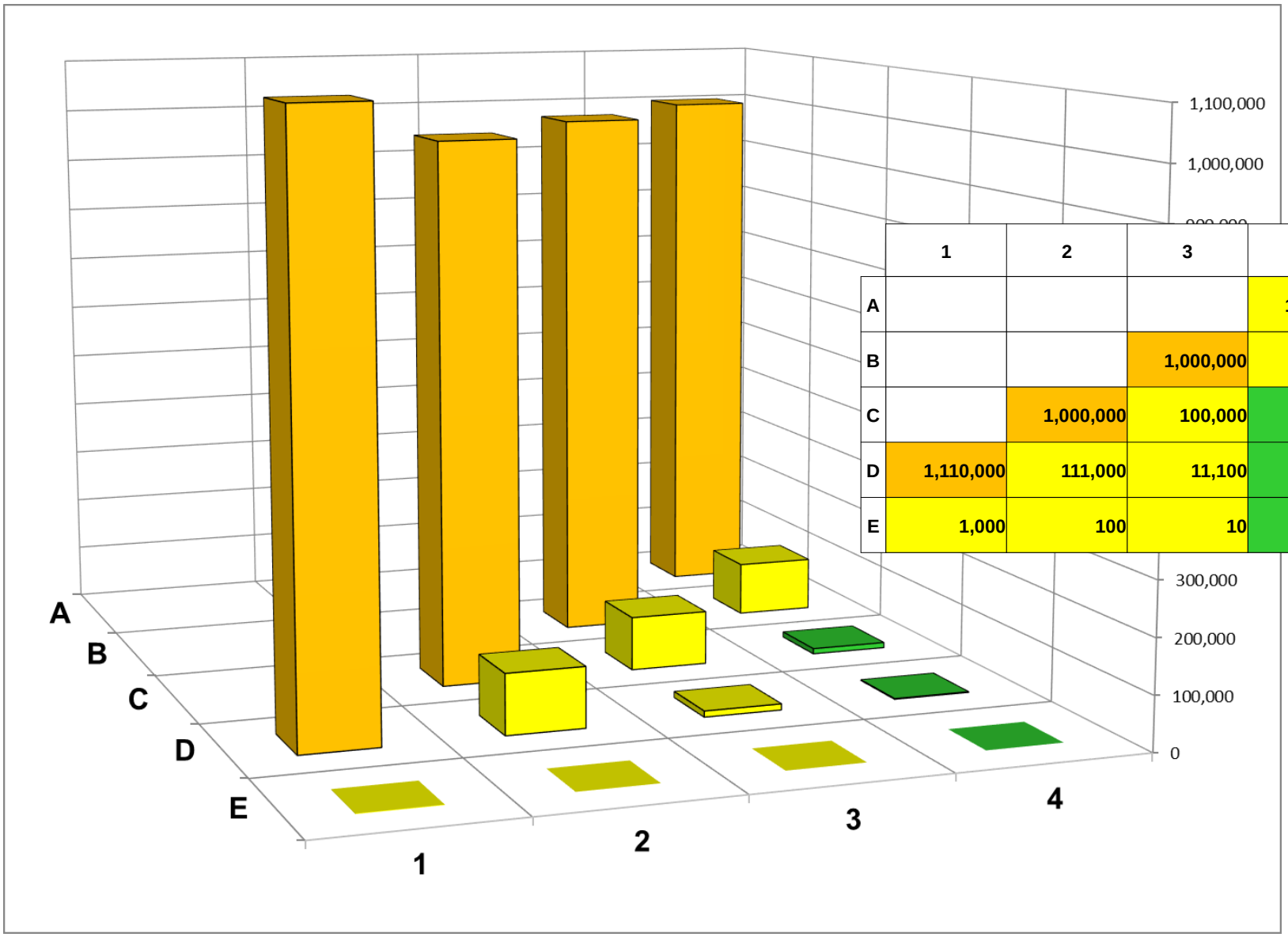
	1	2	3	4
A			10,000,000	1,000,000
B		10,000,000	1,000,000	100,000
C	10,000,000	1,000,000	100,000	10,000
D	1,110,000	111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values



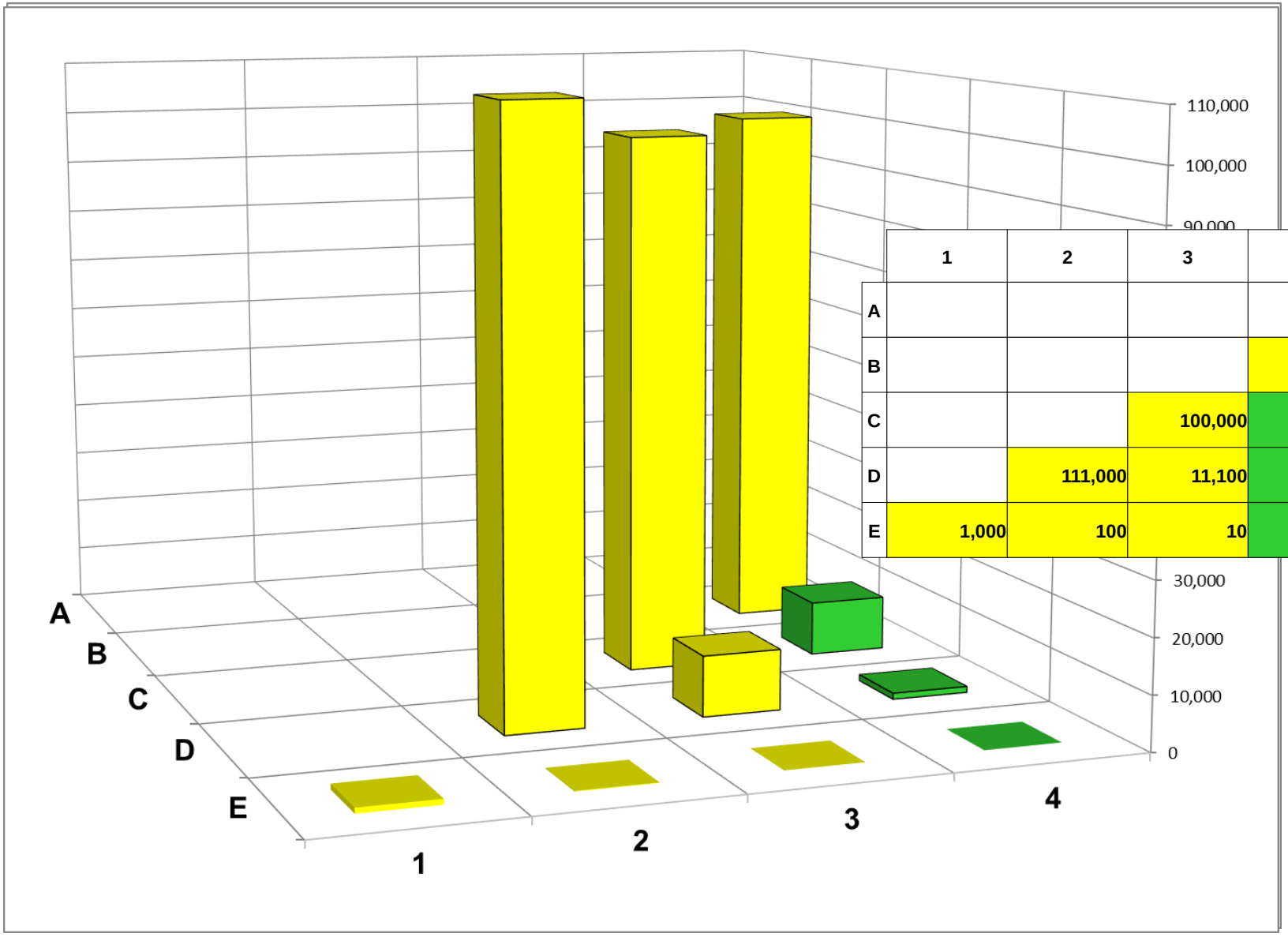
	1	2	3	4
A				1,000,000
B			1,000,000	100,000
C		1,000,000	100,000	10,000
D	1,110,000	111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values



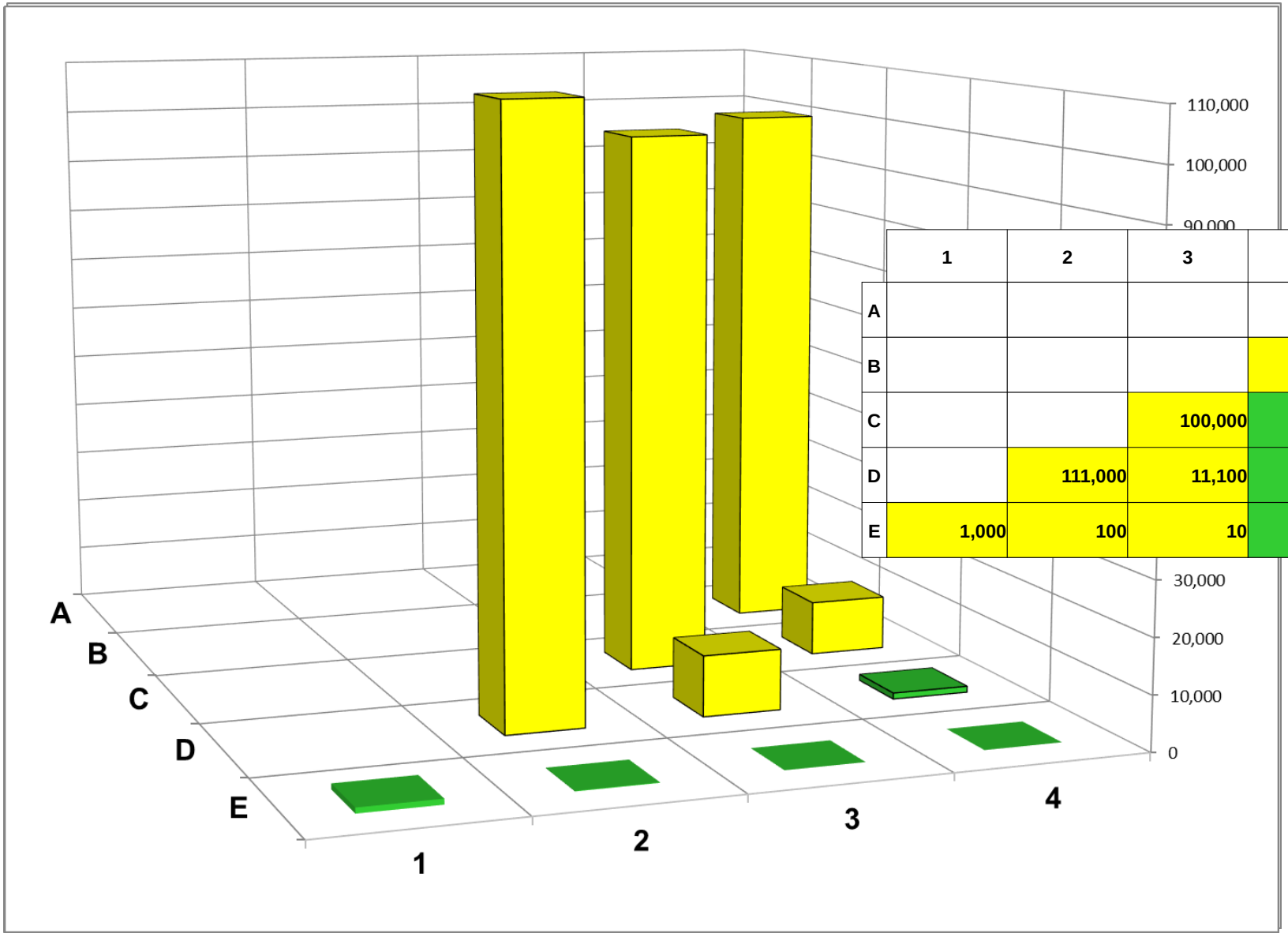
	1	2	3	4
A				1,000,000
B			1,000,000	100,000
C		1,000,000	100,000	10,000
D	1,110,000	111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values



	1	2	3	4
A				
B				100,000
C			100,000	10,000
D		111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values

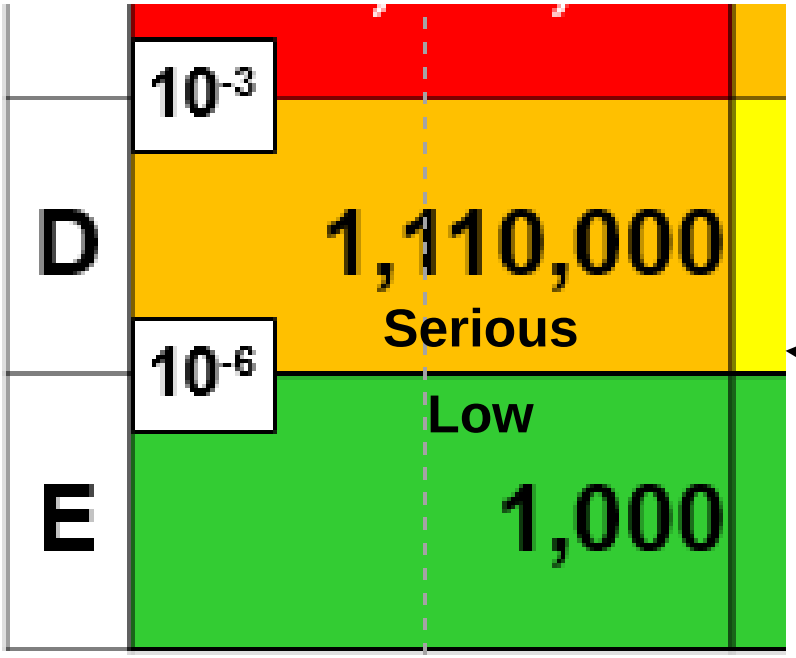


	1	2	3	4
A				
B				100,000
C			100,000	10,000
D		111,000	11,100	1,110
E	1,000	100	10	1

Matrix Relative Risk Values

	1	2	3	4
A	1,000,000,000	100,000,000	10,000,000	1,000,000
	10^{-1}			
B	100,000,000	10,000,000	1,000,000	100,000
	10^{-2}			
C	10,000,000	1,000,000	100,000	10,000
	10^{-3}			
D	1,110,000	111,000	11,100	1,110
	10^{-6}			
E	1,000	100	10	1

Matrix Relative Risk Values



Where is the medium?

Matrix Relative Risk Values

	1	2	3	4
A	10,000,000	1,000,000	100,000	10,000
10^{-3} B	1,000,000	100,000	10,000	1,000
10^{-4} C	100,000	10,000	1,000	100
10^{-5} D	10,000	1,000	100	10
10^{-6} E	1,000	100	10	1

Matrix Relative Risk Values

	1	2	3	4
A	10,000,000 1 in 6 months	1,000,000	100,000	10,000
B	1,000,000 1 in 5 years	100,000	10,000	1,000
C	100,000 1 in 50 years	10,000	1,000	100
D	10,000 1 in 500 years	1,000	100	10
E	1,000	100	10	1

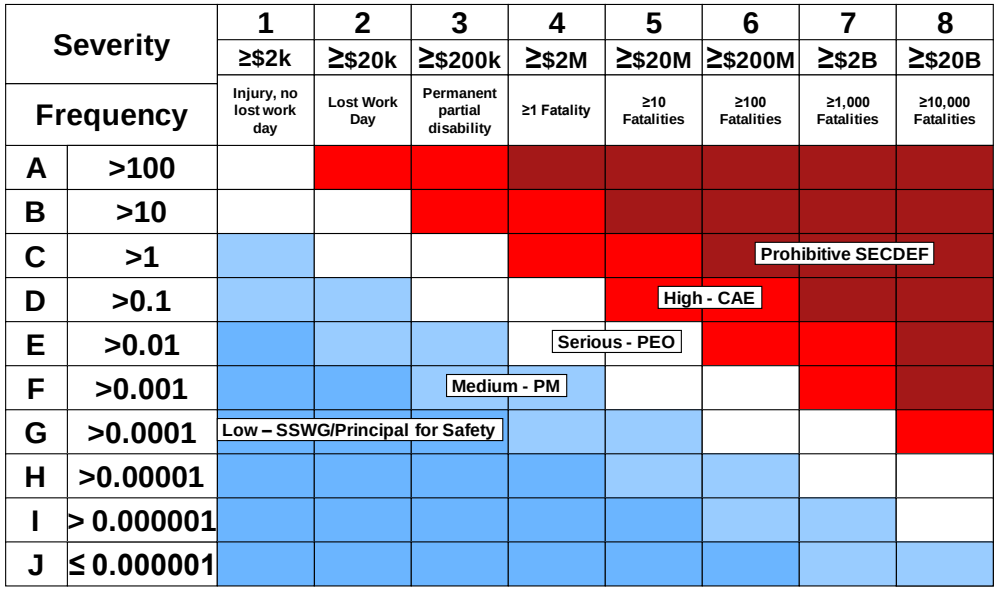
Matrix Relative Risk Values

	1	2	3	4
A	10,000 1 in 6 months	100,000	1,000,000	10,000,000
B	1,000 1 in 5 years	10,000	100,000	1,000,000
C	100 1 in 50 years	1,000	10,000	100,000
D	10 1 in 500 years	100	1,000	10,000
E	1	10	100	1,000

Summary

Summary
Attributes of a well-designed risk assessment matrix

- ✔ Severity scale covers full range of possible outcomes
- ✔ Probability calibrated with reference to an exposure interval
- ✔ Equally proportioned, logarithmic scales (1, 10, 100, 1000…)
- ✔ Cartesian Orientation – Increase up and to the right
- ✔ Risk levels assigned to cells consistent with contours of equal risk



Summary
Attributes of a well-designed risk assessment matrix

- ✔ Sufficient probability categories so highest severity level reach the PM level
- ✔ Frequency category letters increase with decreasing frequency
- ✔ A RAC for hazards whose risk has been eliminated
- ✔ Easily tailored & consistent with other systems within its family of systems
- ✔ Severity Category numbers increase with increasing Severity

Severity		1	2	3	4	5	6	7	8
		≥$2k	≥$20k	≥$200k	≥$2M	≥$20M	≥$200M	≥$2B	≥$20B
Frequency		Injury, no lost work day	Lost Work Day	Permanent partial disability	≥1 Fatality	≥10 Fatalities	≥100 Fatalities	≥1,000 Fatalities	≥10,000 Fatalities
A	>100								
B	>10								
C	>1						Prohibitive SECDEF		
D	>0.1					High - CAE			
E	>0.01				Serious - PEO				
F	>0.001			Medium - PM					
G	>0.0001	Low – SSWG/Principal for Safety							
H	>0.00001								
I	> 0.000001								
J	≤ 0.000001								

How to Determine the Risk Assessment Code (RAC)

To determine the appropriate RAC for a given hazard:

(1) Identify the full range of potential outcomes for the hazard (death, injury, system loss, environmental impact, and monetary loss). The range of outcomes will often span more than one severity category.

(2) For each severity category associated with this range of severity, determine the associated probability category.

(3) Determine which severity-probability pair has the greatest risk. This pair is the RAC assigned to the hazard.

(4) If two or more severity-probability pairs are equal as the greatest risk, select the one with the greatest severity.

Summary Understanding Probability

Math Definition:

- **Repeat a random experiment "n" number of times.**
- **If a specific outcome has occurred "f" times in these n trials, the number "f" is the frequency of the outcome.**
- **The ratio f/n is the relative frequency of the outcome.**
- **A relative frequency is usually very unstable for small values of "n," but it tends to stabilize about some number "p" as "n" increases.**
- **The number "p" is the probability of the outcome.**

$$p = f / n$$

for very large values of n

Simple example:

Probability of rolling a "3" with one die.

Roll #1 - "5", f/n = 0

Roll #2 - "2", f/n = 0

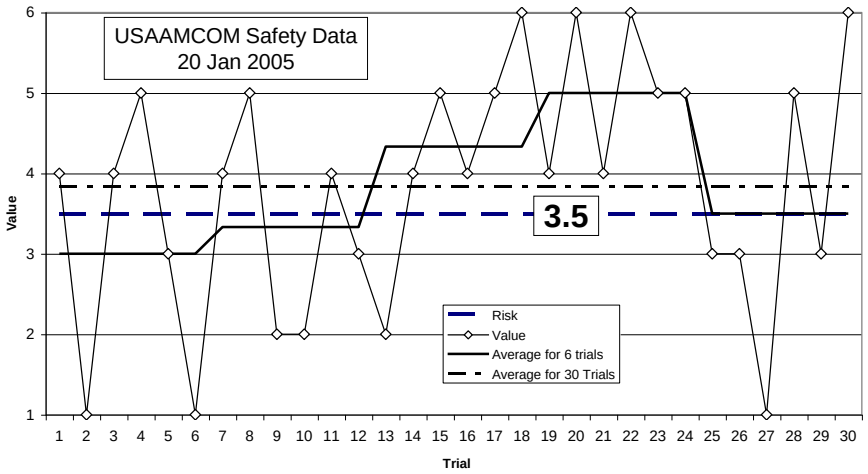
Roll #3 - "3", f/n = 1/3 = .333…

Roll #4 - "4", f/n = 1/4 = .25

Roll #1,000: 163 "3"s, f/n = 163/1000 = .163

Rolls approach infinity f/n = .166666….

Roll a single die 30 times. The expected value of each roll is 3.5. What you actually get is somewhat different.



Hazard: AH-64 strikes wire results in Class A mishap

Probability: 4.406E-06 occurrences per flight hour

1 Flight Hr, no mishap, rate = 0

1,000 Flight Hrs, no mishap, rate = 0

176,182 Flight Hrs, 1 mishap, rate = 5.676E-06 /flt hr

274,539 Flight Hrs, 2 mishaps, rate = 7.285E-06 /flt hr

700,462 Flt Hrs, 3 mishaps, rate = 4.283E-06 /flt hr

10,000,000 Flt Hrs, 46 mishaps, rate = 4.600E-06 /flt hr

1,000,000,000 Hrs, 4407 mishaps, rate = 4.407E-06 /flt hr

Flight hours approach infinity, rate = 4.406E-06 /flt hr

Summary Expanded Matrix

Applying Probability Classifications to a military helicopter

Fleet Size = 368 aircraft

Utilization = 240 hours/year

Life = 20 years/aircraft

Aircraft Life = 240 x 20
= 4,800 hours

Fleet Exposure Hours = 368 x 240 x 20
= 1,776,400 hours

Fleet Hours per Year = 368 x 240
= 88,320 hours

US Army PEO Aviation Expanded Matrix

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	Events per Year	Years per Event	Event per Fleet Life	Fleet Life per Event
Frequent A	10^{-3}	1,000	100	88.32	0.0113	1,060	0.000944
Probable B	10^{-4}	10,000	10	8.832	0.113	105.98	0.00944
Occasional C	10^{-5}	100,000	1	0.8832	1.13	10.598	0.0944
Remote D	10^{-6}	1,000,000	0.1	0.0883	11.3	1.0598	0.944
Improbable E	10^{-7}	10,000,000	0.01	0.00883	113	0.106	9.44
Very Improbable F	0		0	0		0	
Zero Risk 0R							

Numbers greater than 1 are easier to comprehend

29

16

Input
Calculated

Assumptions	
Fleet Size:	368 aircraft
Utilization:	240.0 hours/yr
Aircraft Life:	12 years
Calculations	
Aircraft Exposure Hours:	2,880 hours
Fleet Exposure Hours:	1,059,840 hours
Fleet Hours per Year:	88,320 hours

	Events per Flight Hour	Flight Hours per Event	Events per 100,000 Flt Hrs	1 Catastrophic ($10M)	2 Critical ($1M)	3 Marginal ($100K)	4 Negligible	Fleet-wide: Events per Year	Years per Event	Event per Fleet Life	Fleet Life per Event
Frequent A	10^{-3}	1,000	100	1A (High AAE)	2A	3A	4A	88.32	0.0113	1,060	0.000944
Probable B	10^{-4}	10,000	10	1B	2B	3B	4B	8.832	0.113	105.98	0.00944
Occasional C	10^{-5}	100,000	1	1C	2C (Serious PEO)	3C	4C	0.8832	1.13	10.598	0.0944
Remote D	10^{-6}	1,000,000	0.1	1D	2D	3D	4D	0.0883	11.3	1.0598	0.944
Improbable E	10^{-7}	10,000,000	0.01	1E	2E (Medium PM)	3E	4E	0.00883	113	0.106	9.44
Very Improbable F	0		0	1F	2F (Low PM)	3F	4F	0		0	
Zero Risk 0R											

Summary

Accidents on a Matrix

Based on this relationship between mishap risk and mishap loss, we can plot mishap histories on a risk matrix as follows:

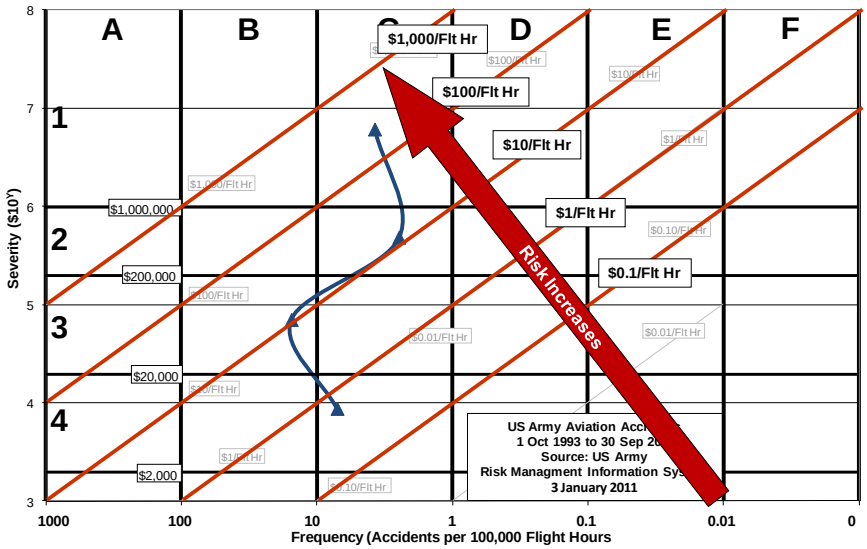
$$\text{Severity} = \frac{\text{Total Cost from Class A mishaps}}{\text{Total Number of Class A mishaps}}$$

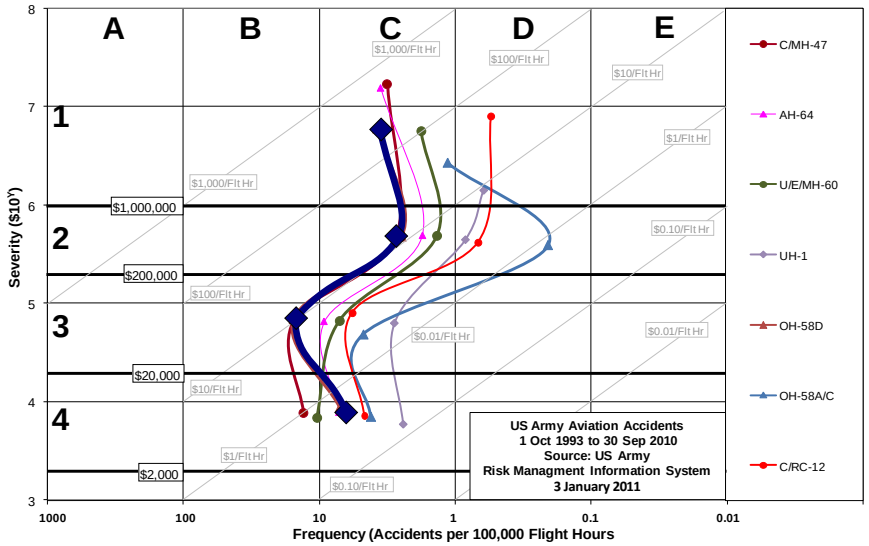
$$= \frac{\$1{,}305{,}079{,}886}{83} = \$\ 15{,}723{,}854$$

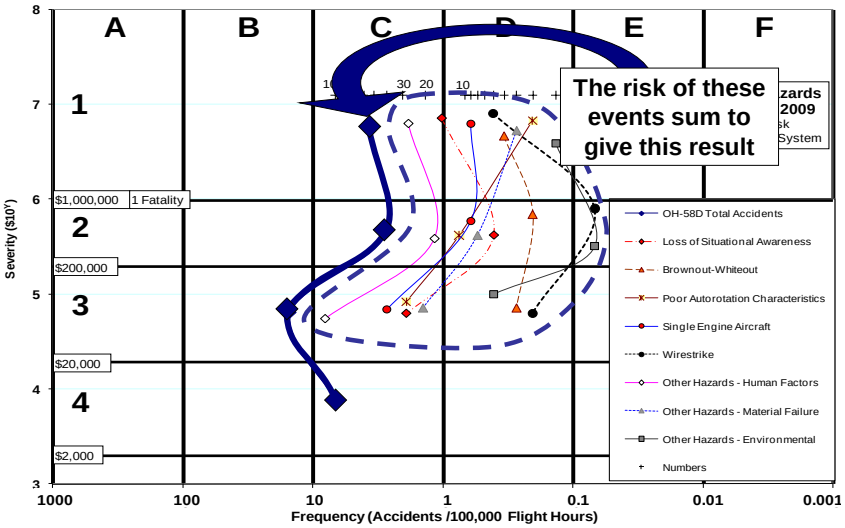
$$\text{Probability} = \frac{\text{Total Number of Class A mishaps}}{\text{Total Hours Flown}}$$

$$= \frac{83}{2{,}351{,}860} = 3.529 \text{ mishaps / 100,000 Flt Hrs}$$

21







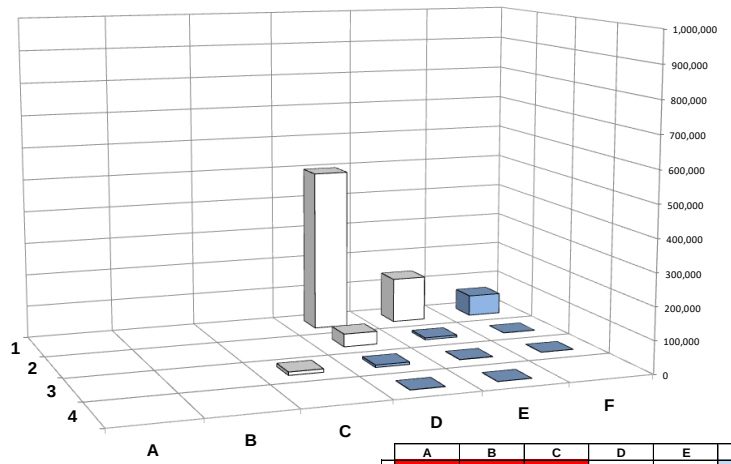
Summary

	A	B	C	D	E	F
1	100,000,000	10,000,000	1,000,000	100,000	10,000	1,000
2	10,000,000	1,000,000	100,000	10,000	1,000	100
3	1,000,000	100,000	10,000	1,000	100	10
4	100,000	10,000	1,000	100	10	1

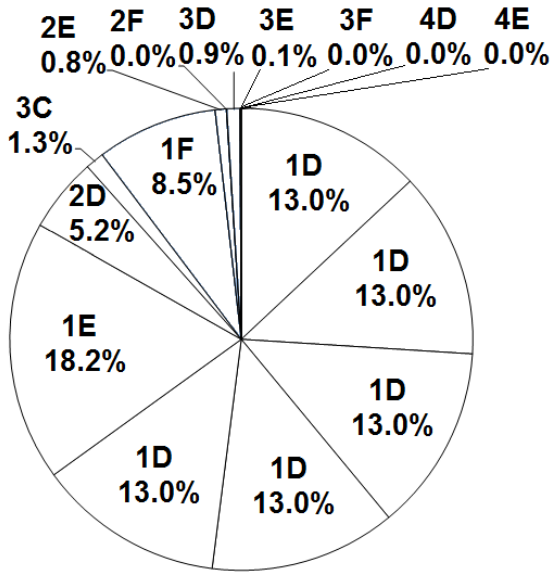
Relative Risk Values (Clemens)

	A	B	C	D	E	F
1				500,000	140,000	65,000
2				40,000	6,000	200
3			10,000	7,000	500	40
4				200	10	

Helicopter A



	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	



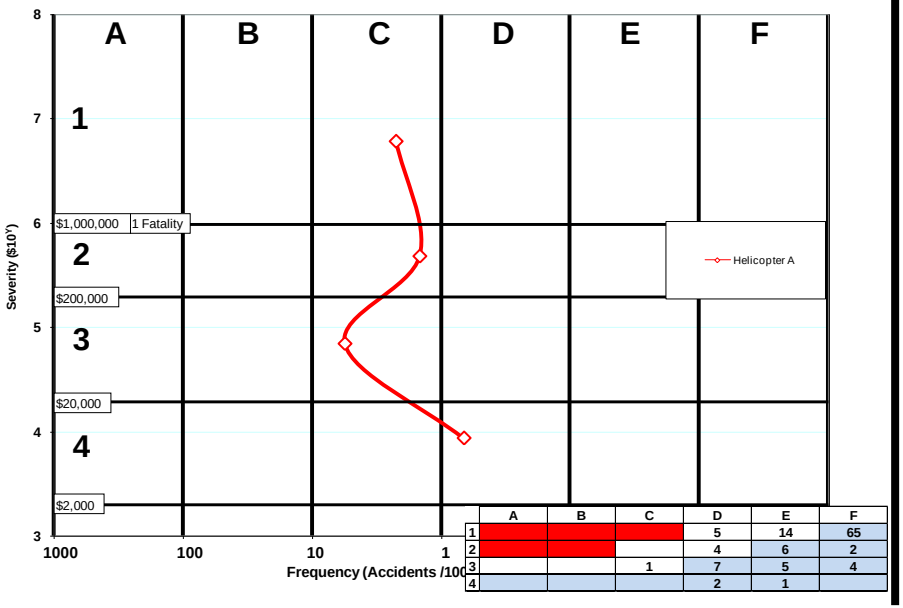
	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	

Summary

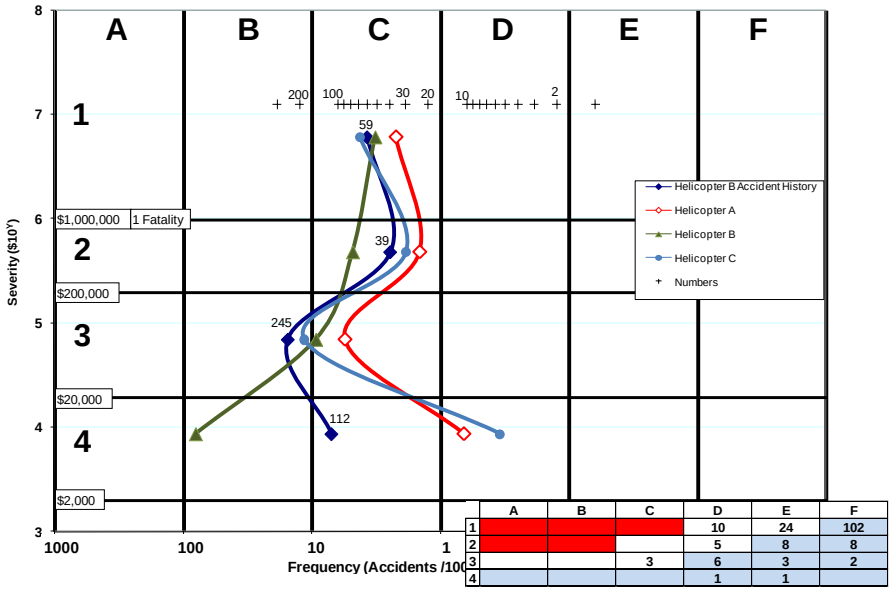
Hazard Risk Profile

	3.16E-04 A	3.16E-05 B	3.16E-06 C	3.16E-07 D	3.16E-08 E	F
1					14	65
2					6	2
3			1		5	4
4					1	

	A	3.16E-04 B	3.16E-05 C	3.16E-06 D	3.16E-07 E	3.16E-08 F
1	2.23E-05	Sum		5 x 3.16E-06 = 1.58E-05	14 x 3.16E-07 = 4.43E-06	65 x 3.16E-08 = 2.06E-06
2	1.46E-05	Sum		4 x 3.16E-06 = 1.26E-05	6 x 3.16E-07 = 1.90E-06	2 x 3.16E-08 = 6.32E-08
3	5.55E-05	Sum	1 x 3.16E-05 = 3.16E-05	7 x 3.16E-06 = 2.21E-05	5 x 3.16E-07 = 1.58E-06	4 x 3.16E-08 = 1.26E-07
4	6.64E-06	Sum		2 x 3.16E-06 = 6.32E-06	1 x 3.16E-07 = 3.16E-07	



	A	B	C	D	E	F
1				5	14	65
2				4	6	2
3			1	7	5	4
4				2	1	



	A	B	C	D	E	F
1				10	24	102
2				5	8	8
3			3	6	3	2
4				1	1	

Summary

Missile Risk Matrix

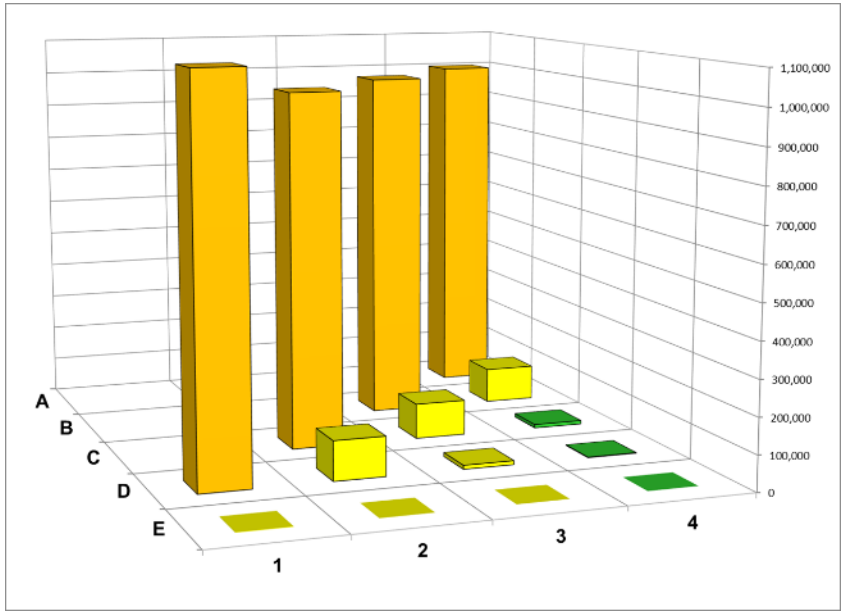
RISK ASSESSMENT MATRIX				
SEVERITY / PROBABILITY *	Catastrophic (1) 1 Fatal $10M	Critical (2) $1M	Marginal (3) $100K	Negligible (4)
Frequent (A) 10^{-1}	High	High	Serious	Medium
Probable (B) 10^{-2}	High	High	Serious	Medium
Occasional (C) 10^{-3}	High	Serious	Medium	Low
Remote (D) 10^{-6}	Serious	Medium	Medium	Low
Improbable (E)	Medium	Medium	Medium	Low
Eliminated (F)	Eliminated			

Back of the Envelope Calculation

40,000 Shishkebab Missiles
Delivered over 20 years
Assume all fired
1 accident in 1,000,000 firings

$$\frac{\text{1 accident}}{\text{1,000,000 ~~firings~~}} \times \frac{\text{40,000 ~~firings~~}}{\text{20 years}} = \frac{\text{1 accident}}{\text{500 years}}$$

	1	2	3	4
A	1,000,000,000	100,000,000	10,000,000	1,000,000
	10^{-1}			
B	100,000,000	10,000,000	1,000,000	100,000
	10^{-2}			
C	10,000,000	1,000,000	100,000	10,000
	10^{-3}			
D	1,000,000	100,000	10,000	1,000
	10^{-4}			
	100,000	10,000	1,000	100
	10^{-5}			
	10,000	1,000	100	10
	10^{-6}			
E	1,000	100	10	1



Take-aways

- High degree of precision? – No
- Gets hazards to the correct cell of the matrix
- Confidence that overall assessment ≈ reality
- Helps communicate risk to the risk acceptor
- Very useful for programs with:
  - Reasonably good accident data for analysis
  - A well-designed matrix
- Just one of many tools for managing system safety risk

End of Presentation

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